

# Laser Interferometer Gravitational – wave Observatory LIGO

some case studies in precision engineering

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Collaboration

American Society for Precision  
Engineering

2006 Spring Topical Meeting

May 2, 2006

# Direct detection of gravitational waves from astrophysical sources

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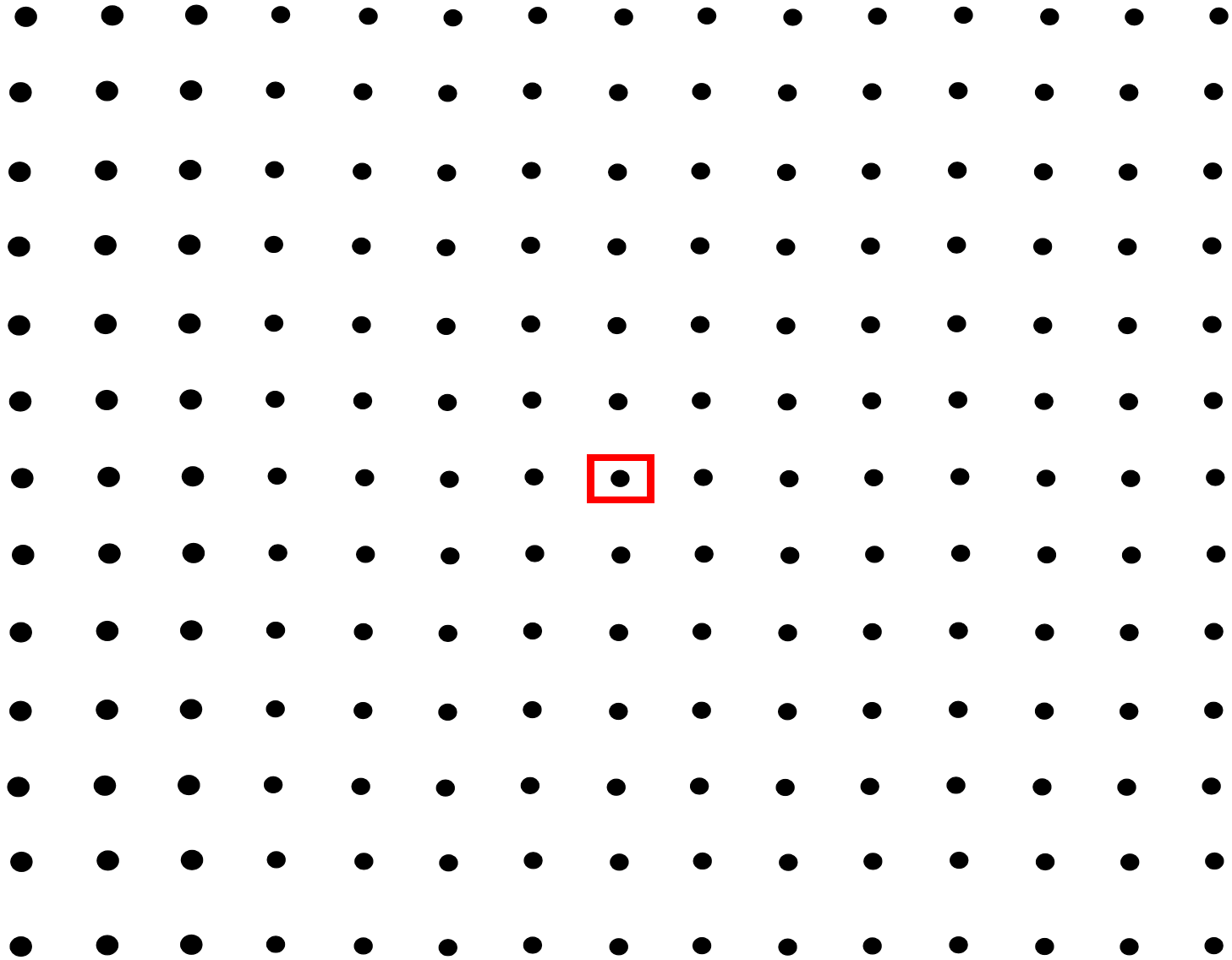
## □ Physics

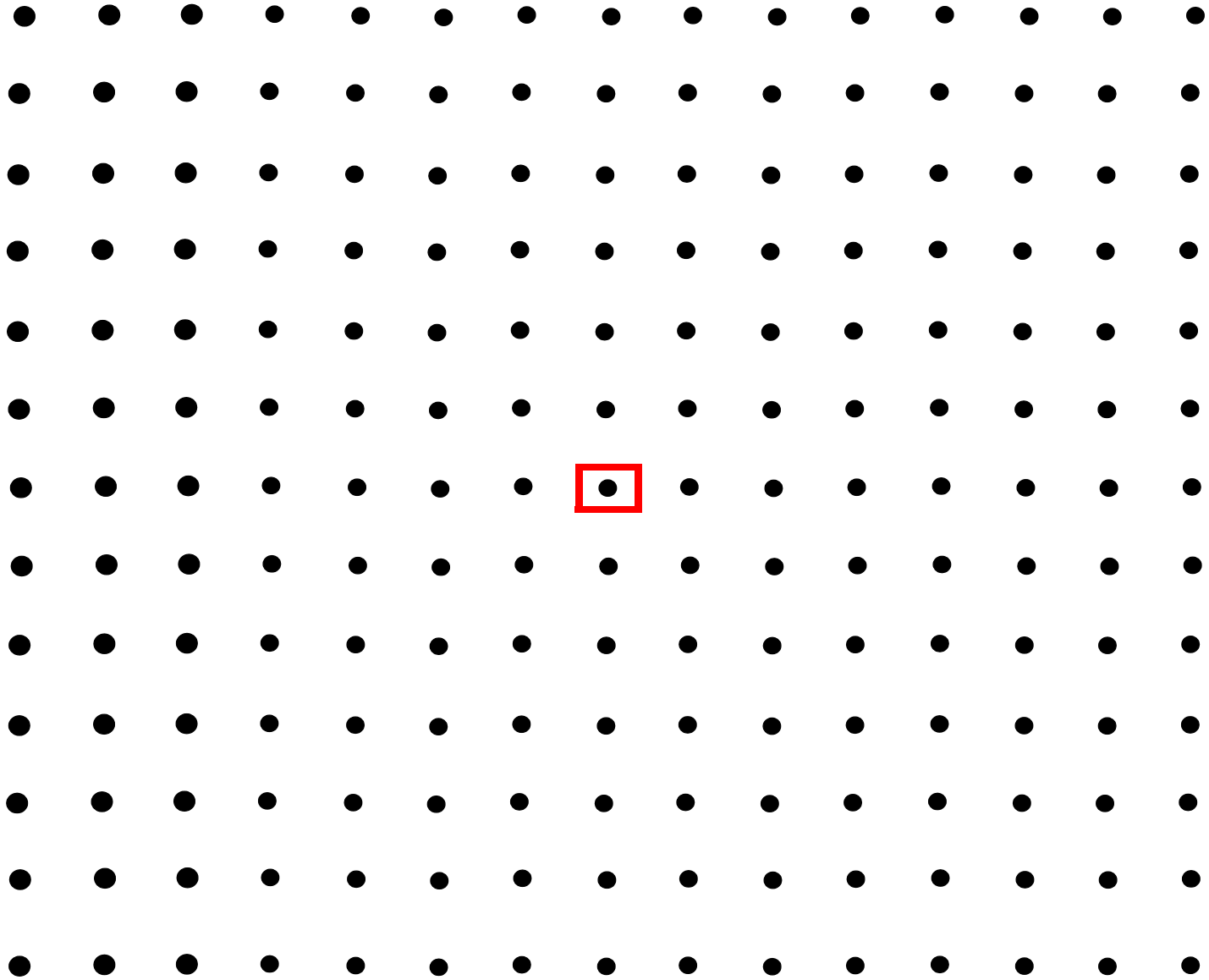
- » Observations of gravitation in the strong field, high velocity limit
- » Determination of wave kinematics – polarization and propagation
- » Tests for alternative relativistic gravitational theories

## □ Astrophysics

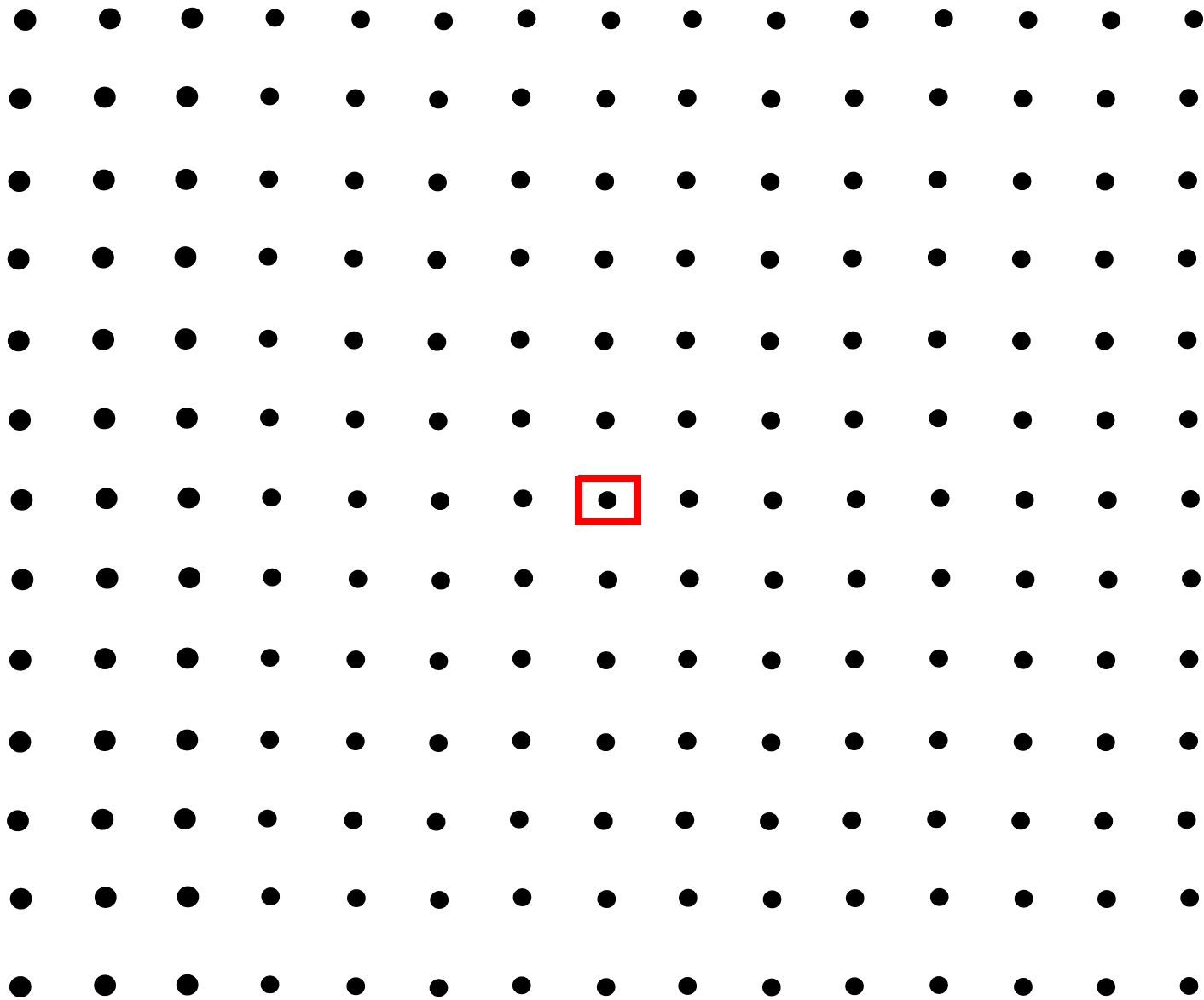
- » Measurement of coherent inner dynamics – stellar collapse, pulsar formation....
- » Compact binary coalescence – neutron star/neutron star, black hole/black hole
- » Neutron star equation of state
- » Primeval cosmic spectrum of gravitational waves

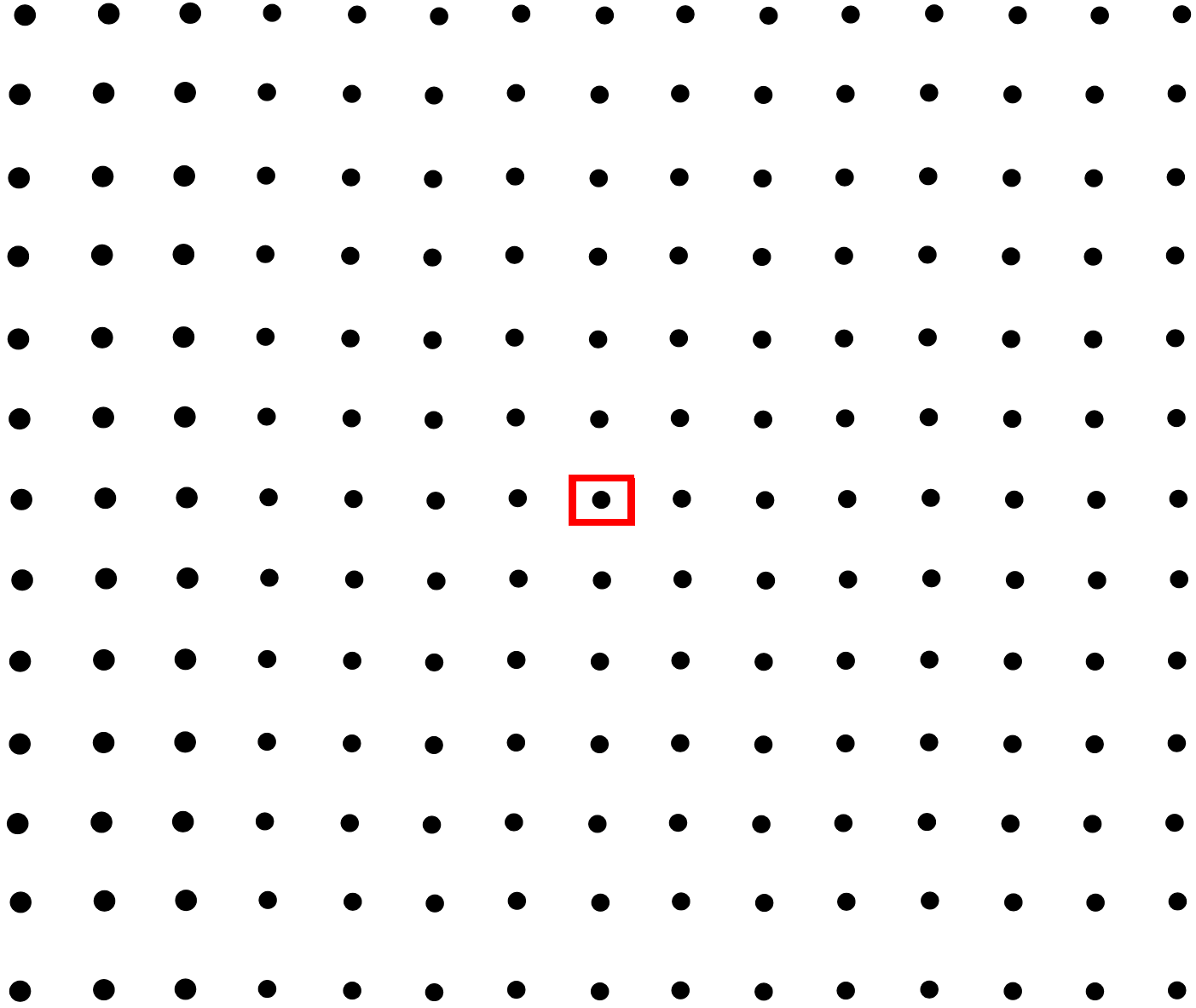
## □ Gravitational wave survey of the universe

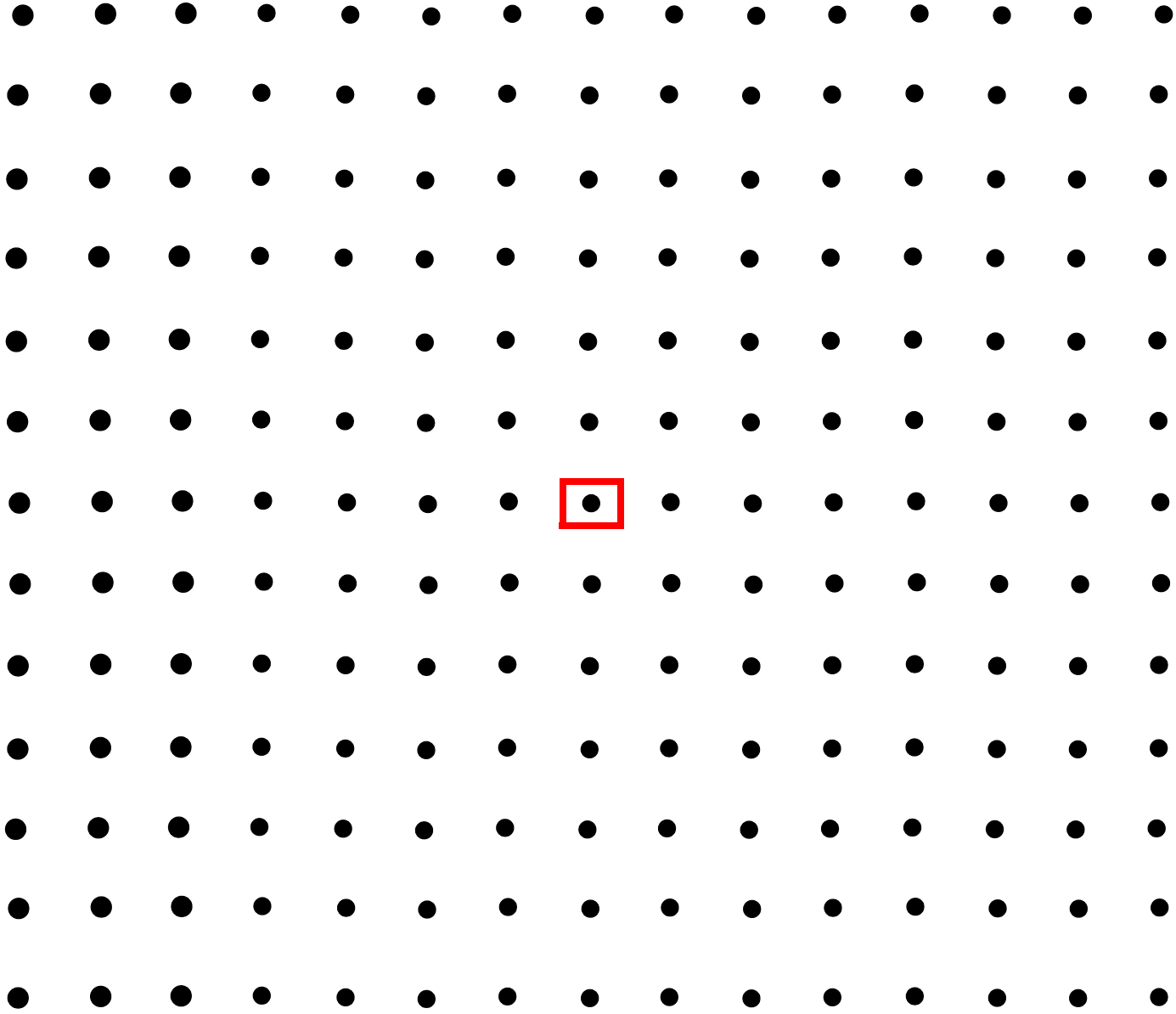


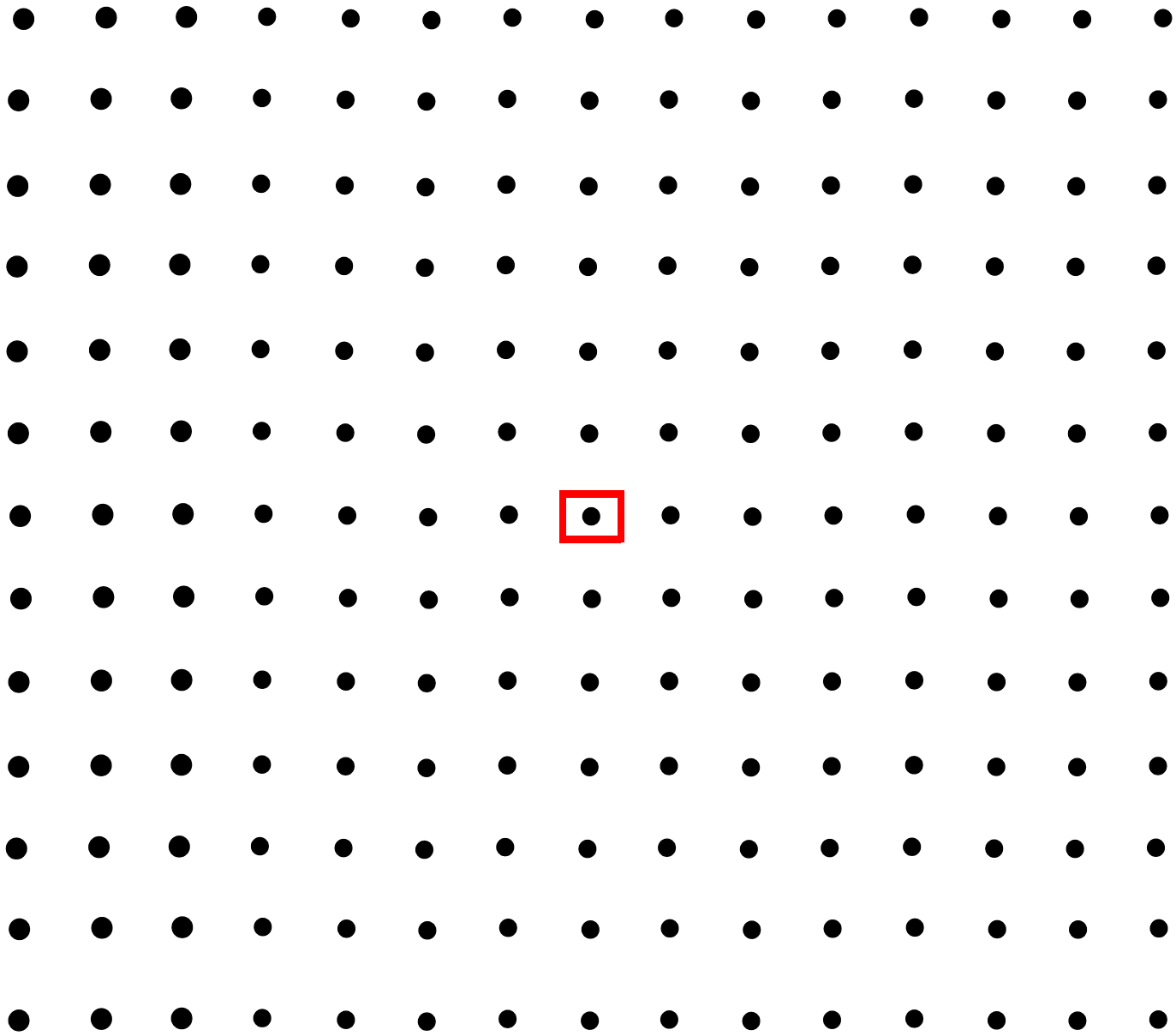


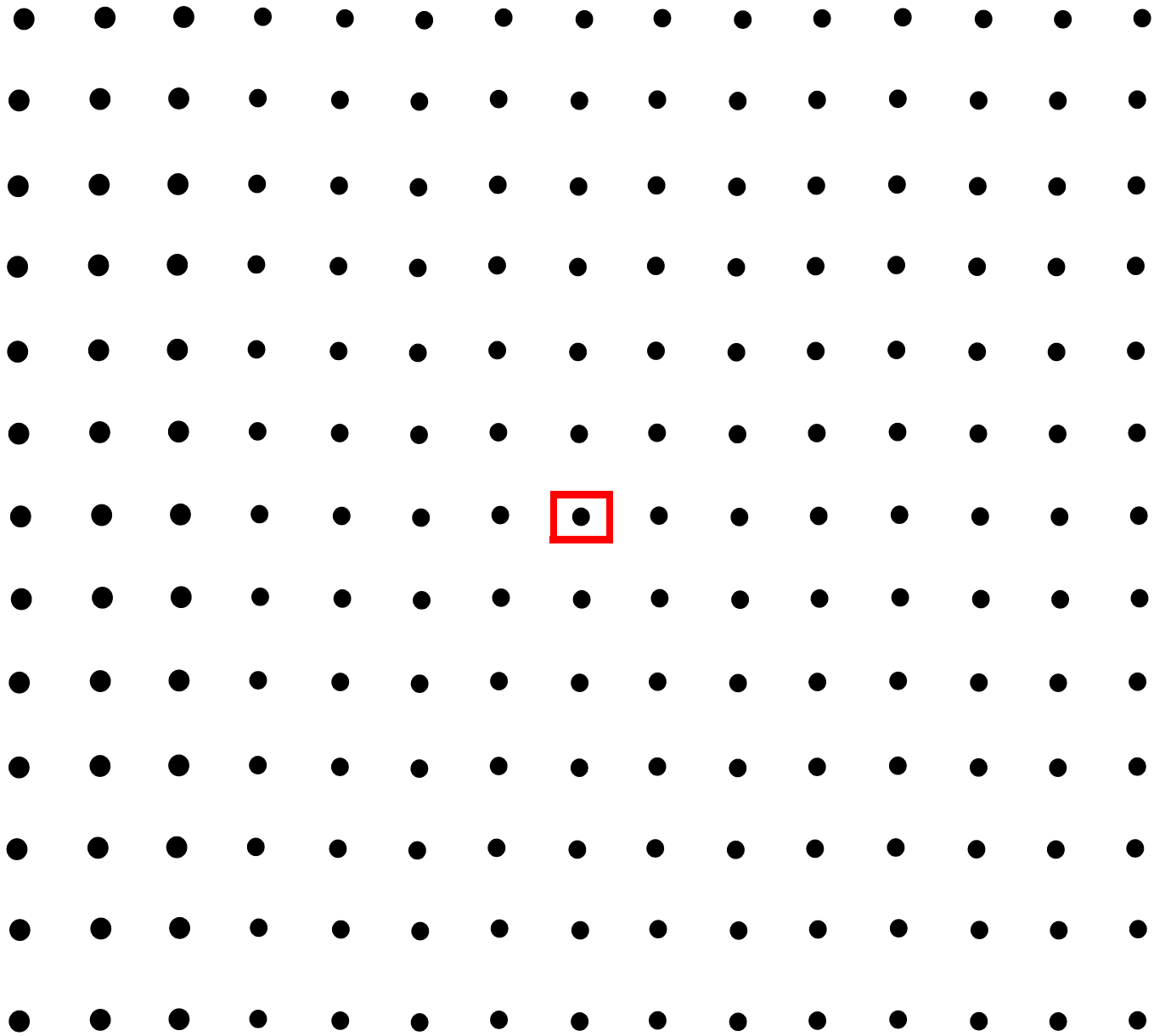


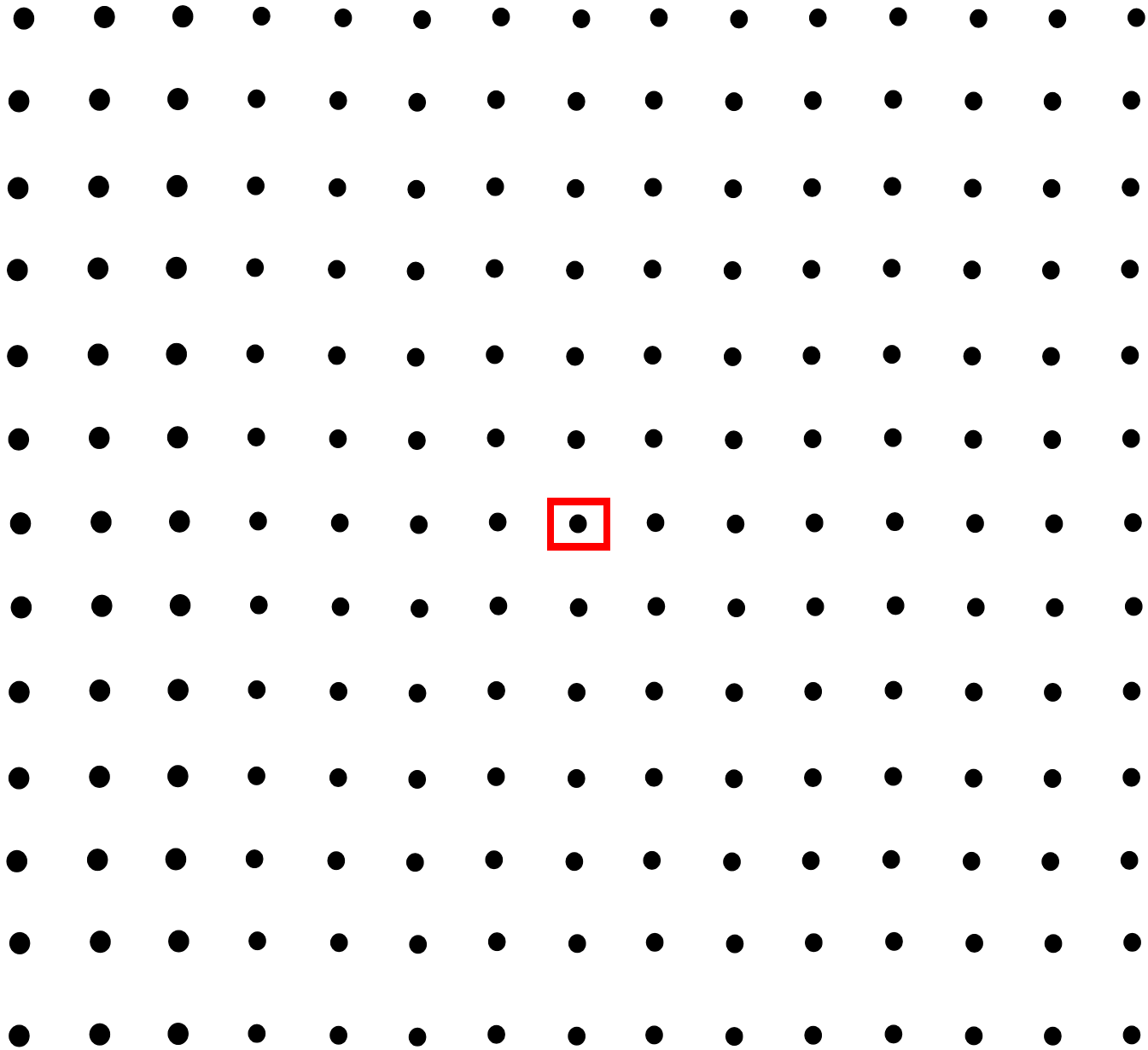


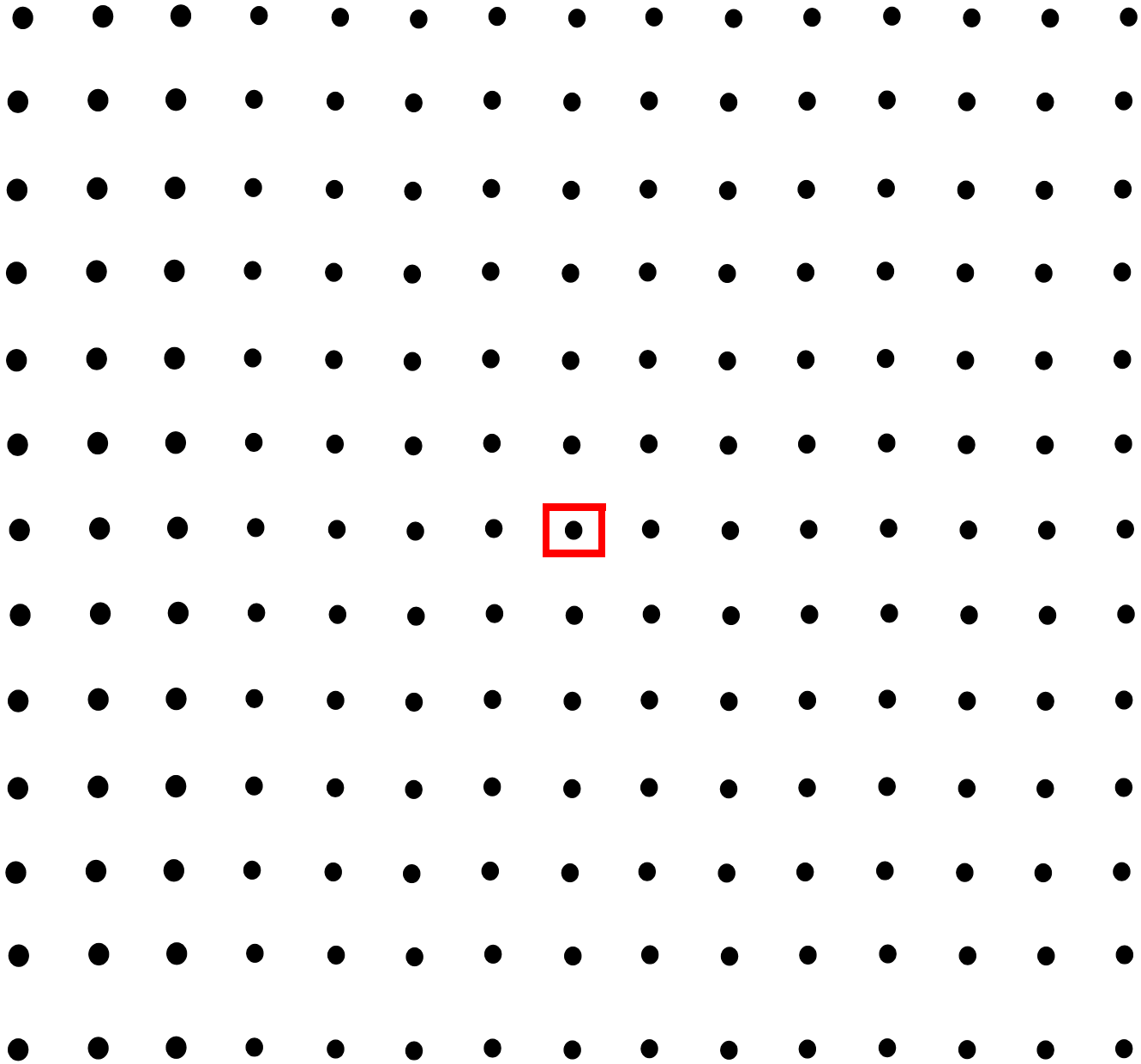


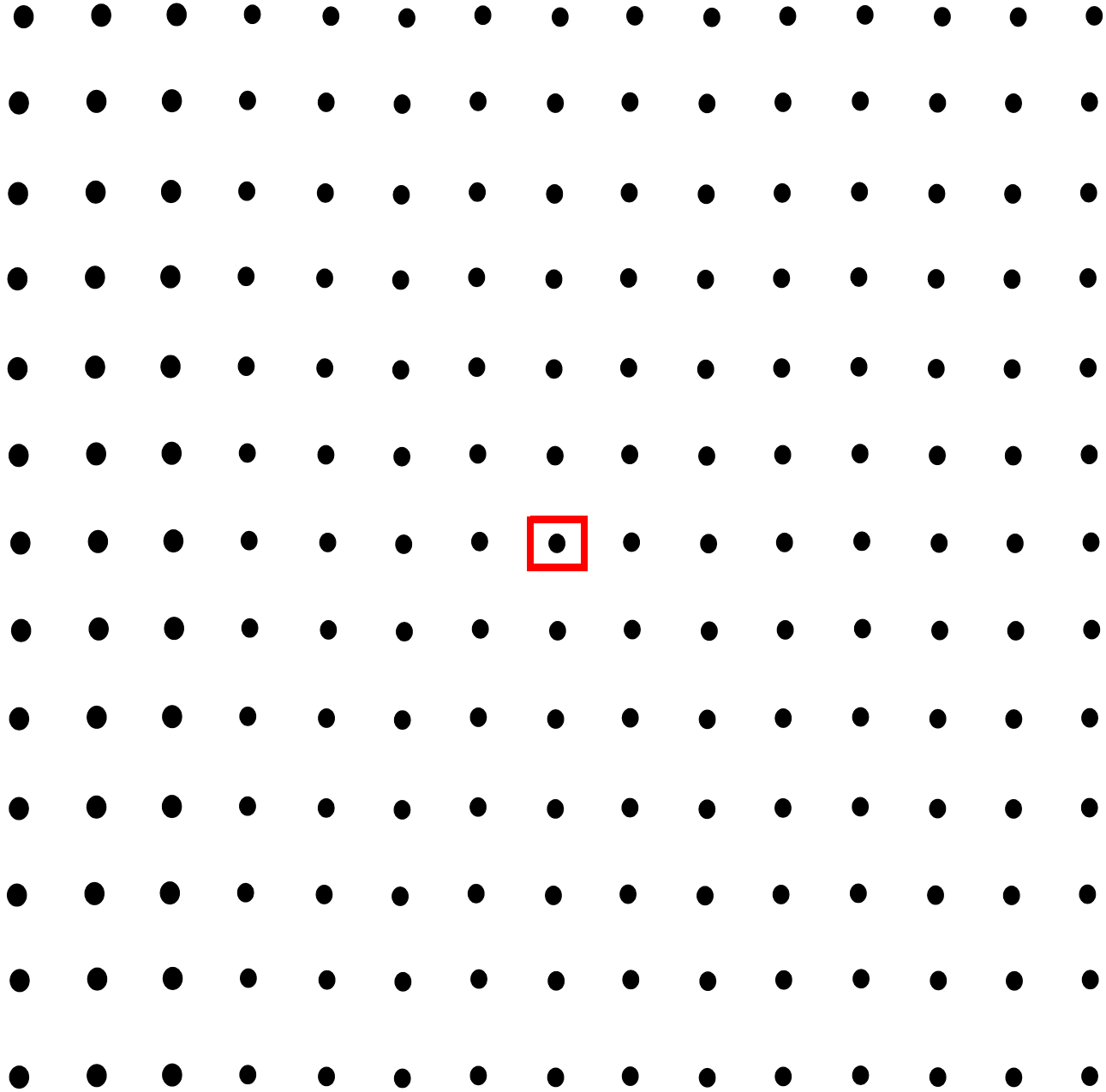




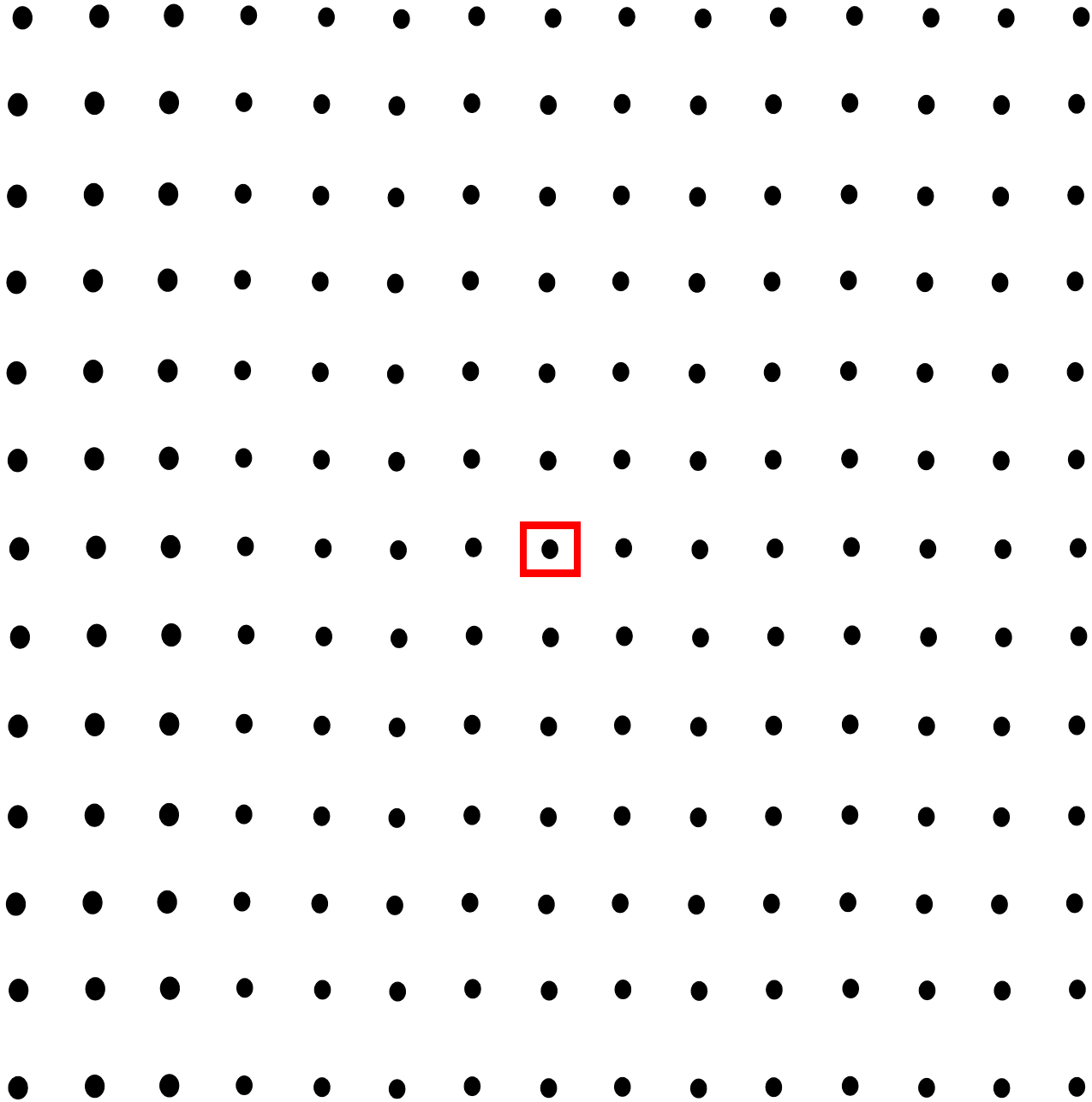


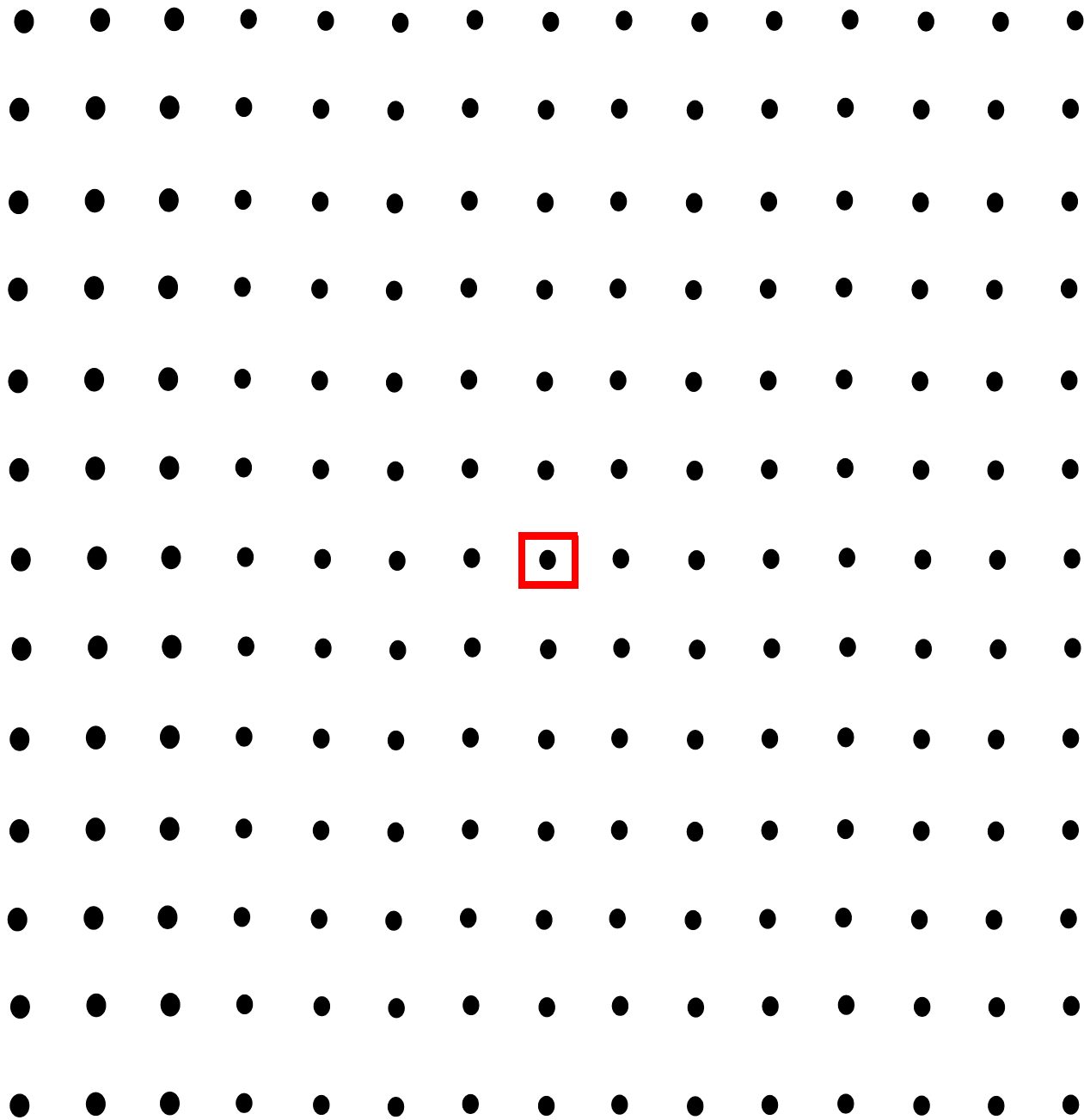


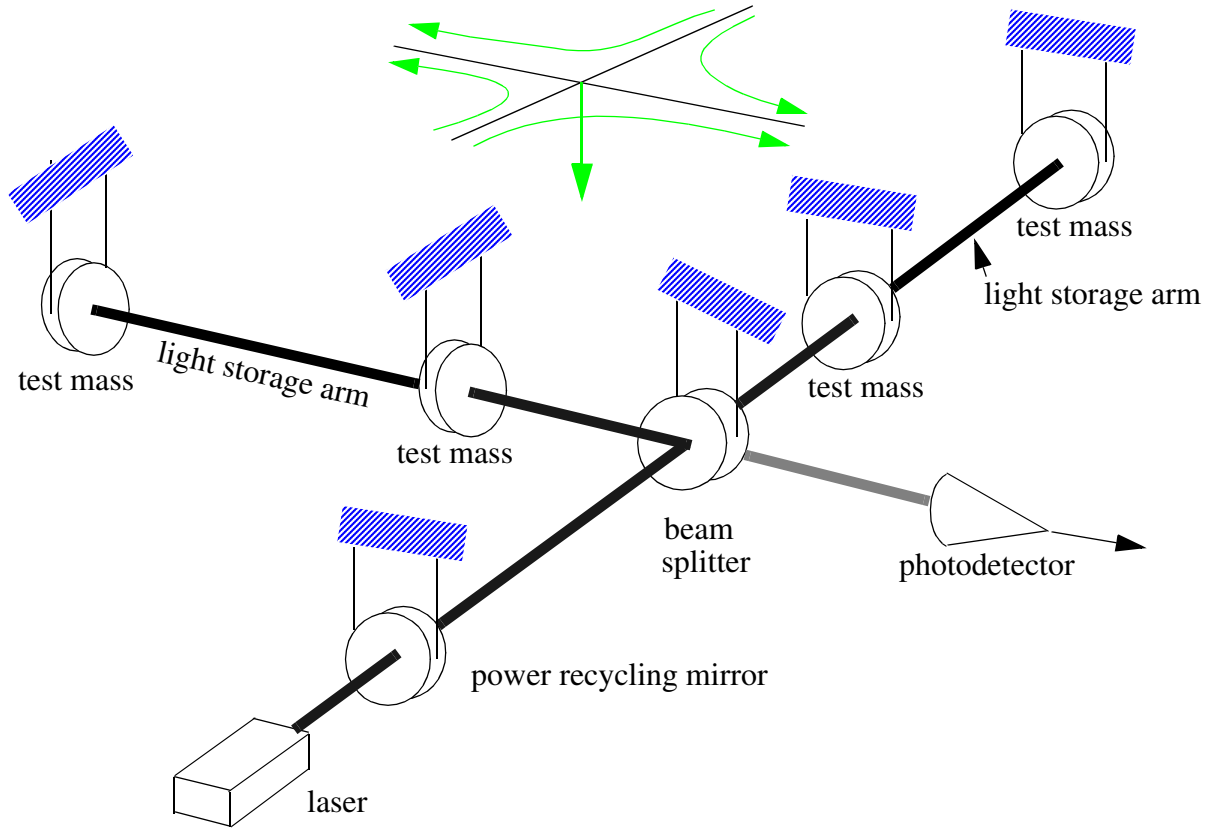












# Measurement challenge

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- Needed technology development to measure:

$$h = \Delta L/L < 10^{-21}$$

$$\Delta L < 4 \times 10^{-18} \text{ meters}$$

# FRINGE SENSING

wavelength  $1 \times 10^{-6} \text{ m}$

$$h = \frac{x}{L} \sim \frac{\lambda}{Lb \sqrt{N\tau}}$$

arm length = 4000 m

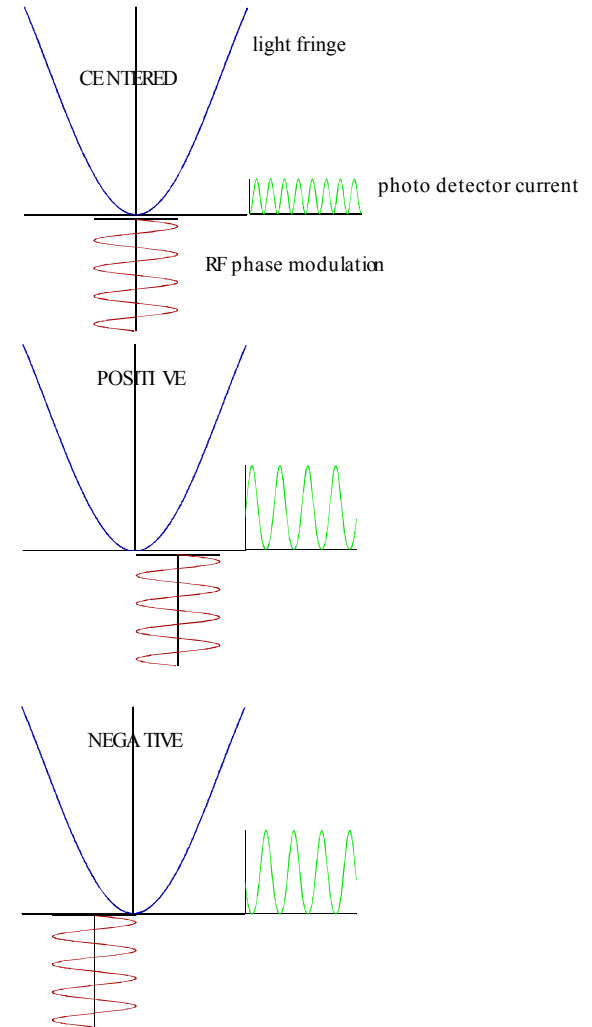
equivalent # of passes = 100

integration time

number of quanta/second at the beam splitter

300 watts at beam splitter =  $10^{21}$  identical photons/sec

$$h = 6 \times 10^{-22} \quad \text{integration time } 10^{-2} \text{ sec}$$



# PENDULUM THERMAL NOISE

Pendulum Brownian motion

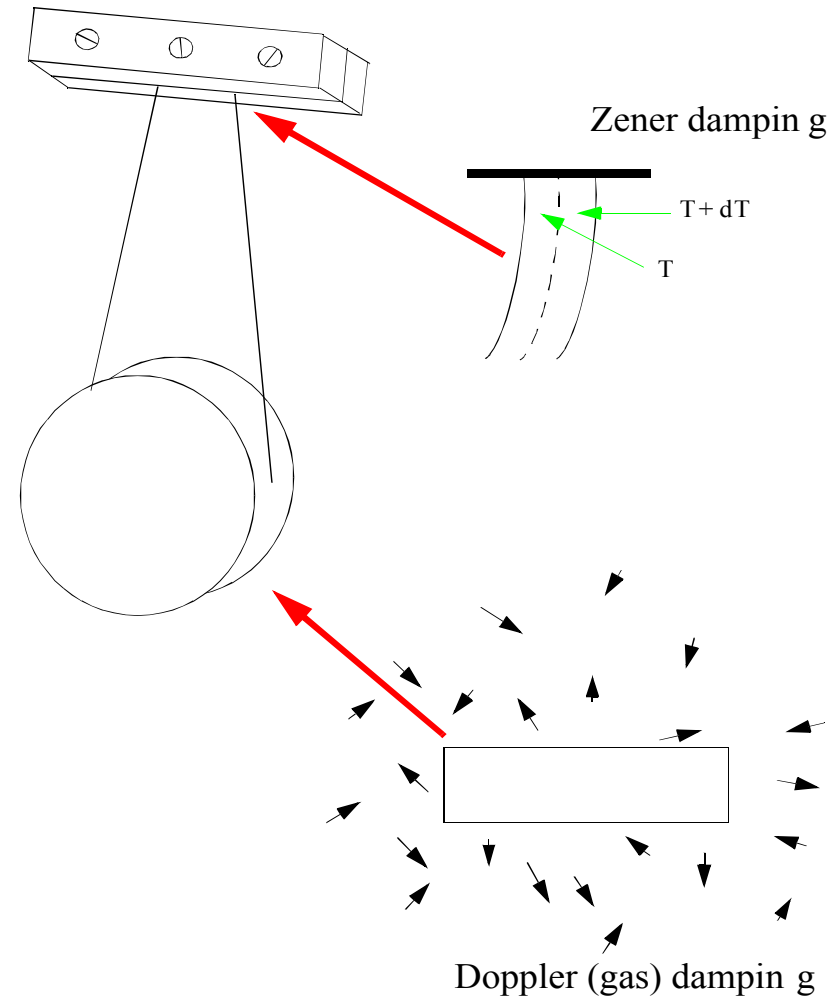
Dissipation leads to fluctuations

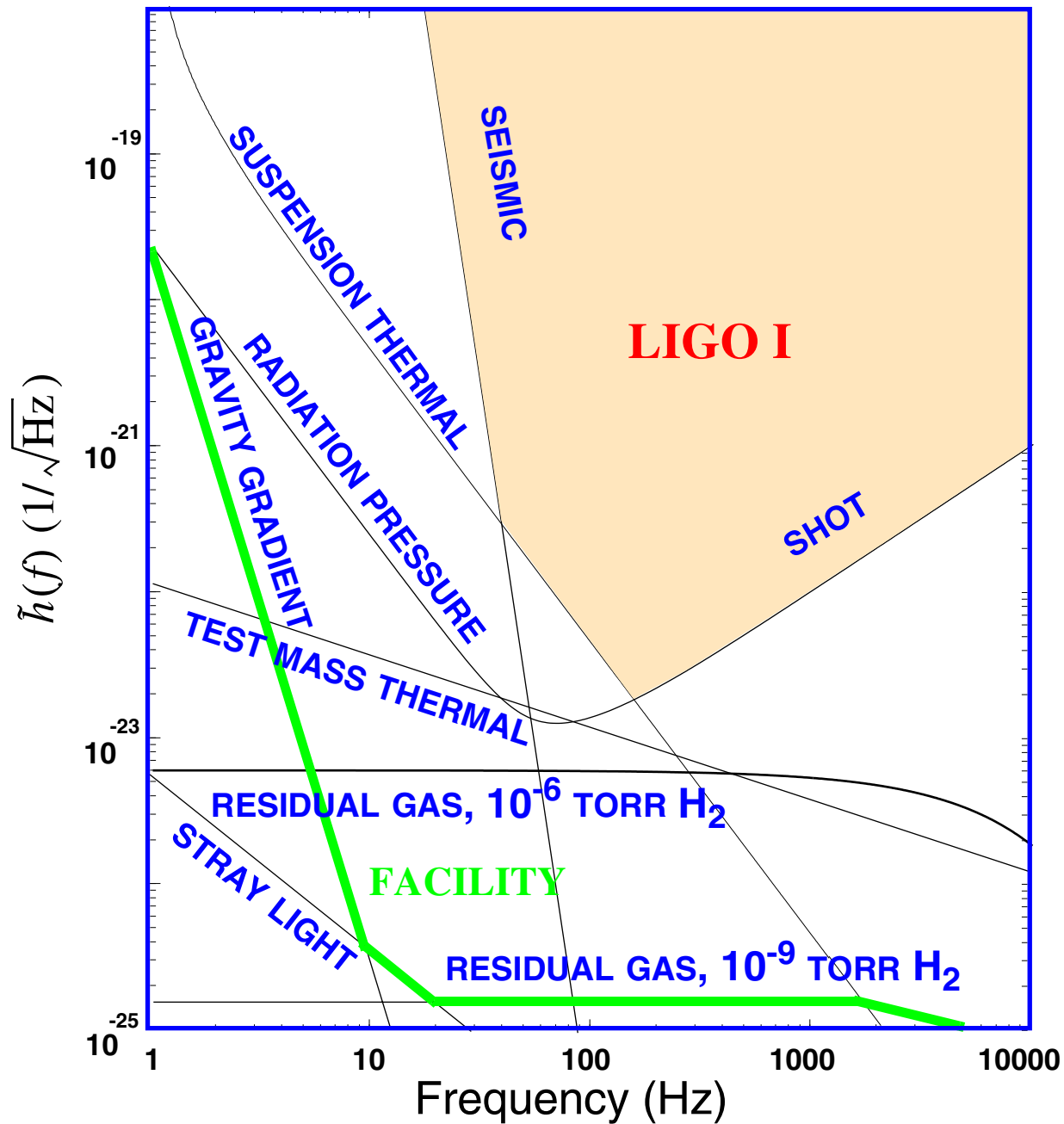
$T_c$  = coherence or damping time  
=  $Q \times$  period of oscillator

Exchange with surroundings:

$$E(\text{thermal}) = \frac{kT t}{T_c}$$

Large  $T_c \Rightarrow$  smaller fluctuations

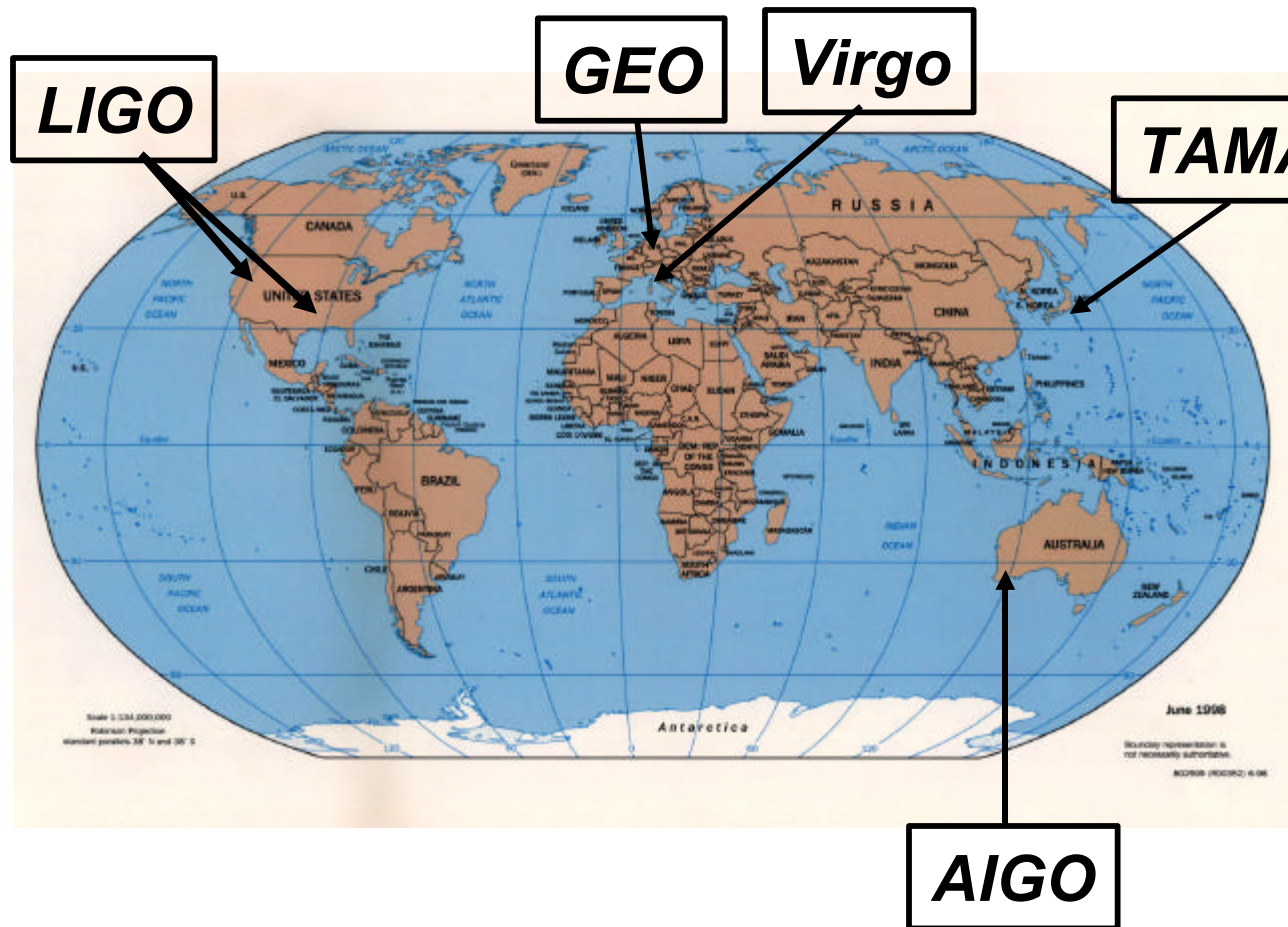




# Interferometers

## *international network*

Simultaneously detect signal (within msec)



detection  
confidence

locate the  
sources

decompose the  
polarization of  
gravitational  
waves





# LIGO Observatory Facilities



***LIGO Hanford Observatory [LHO]***

*26 km north of Richland, WA*

2 km + 4 km interferometers in same vacuum envelope

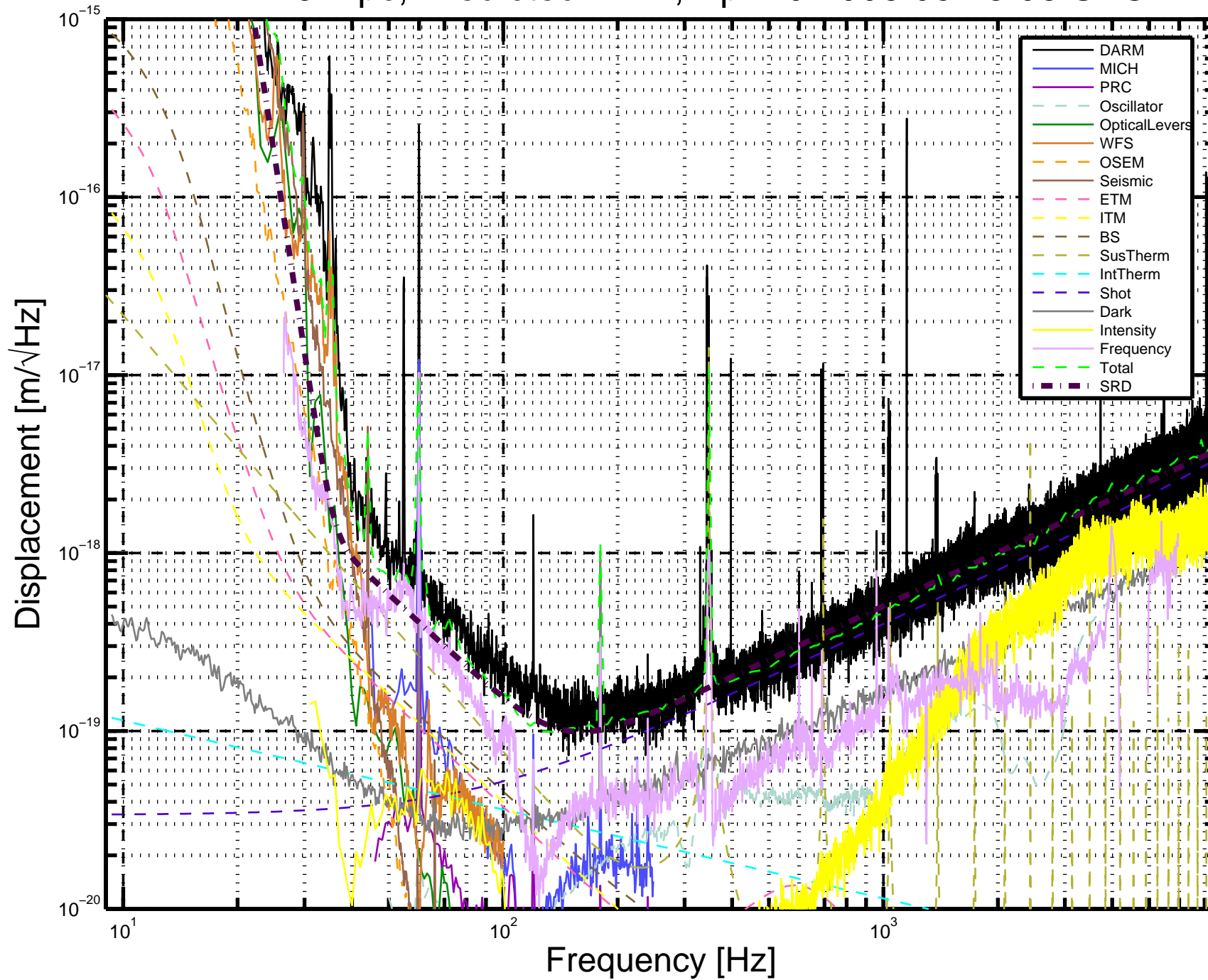


***LIGO Livingston Observatory [LLO]***

*42 km east of Baton Rouge, LA*

Single 4 km interferometer

L1: 11.5 Mpc, Predicted: 14.2, Apr 20 2006 09:13:06 UTC



# Classes of sources

- **Compact binary inspiral: template search**
  - BH/BH
  - NS/NS and BH/NS
- **Low duty cycle transients: wavelets, T/f clusters**
  - Supernova
  - BH normal modes
  - Unknown types of sources
- **Periodic CW sources**
  - Pulsars
  - Low mass x-ray binaries (quasi periodic)
- **Stochastic background**
  - Foreground sources : gravitational wave radiometry
  - Cosmological isotropic background

# Engineering and Technical Challenges

- Large scale economical vacuum system
- Low loss and spatial distortion optics
- Control of optical scattering
- Unprecedented laser frequency and amplitude stabilization
- Control of thermal (Brownian) noise
- High performance vibration isolation
- High speed digital control system
- \* *LIGO research benefited industry*



# LIGO

## *beam tube*



- LIGO beam tube under construction in January 1998
- 65 ft spiral welded sections
- girth welded in portable clean room in the field

1.2 m diameter - 3mm stainless  
50 km of weld

**NO LEAKS !!**

*vacuum equipment*



## Substrates: $\text{SiO}_2$

25 cm Diameter, 10 cm thick

Homogeneity  $< 5 \times 10^{-7}$

Internal mode Q's  $> 2 \times 10^6$

## Polishing

Surface uniformity  $< 1 \text{ nm rms}$

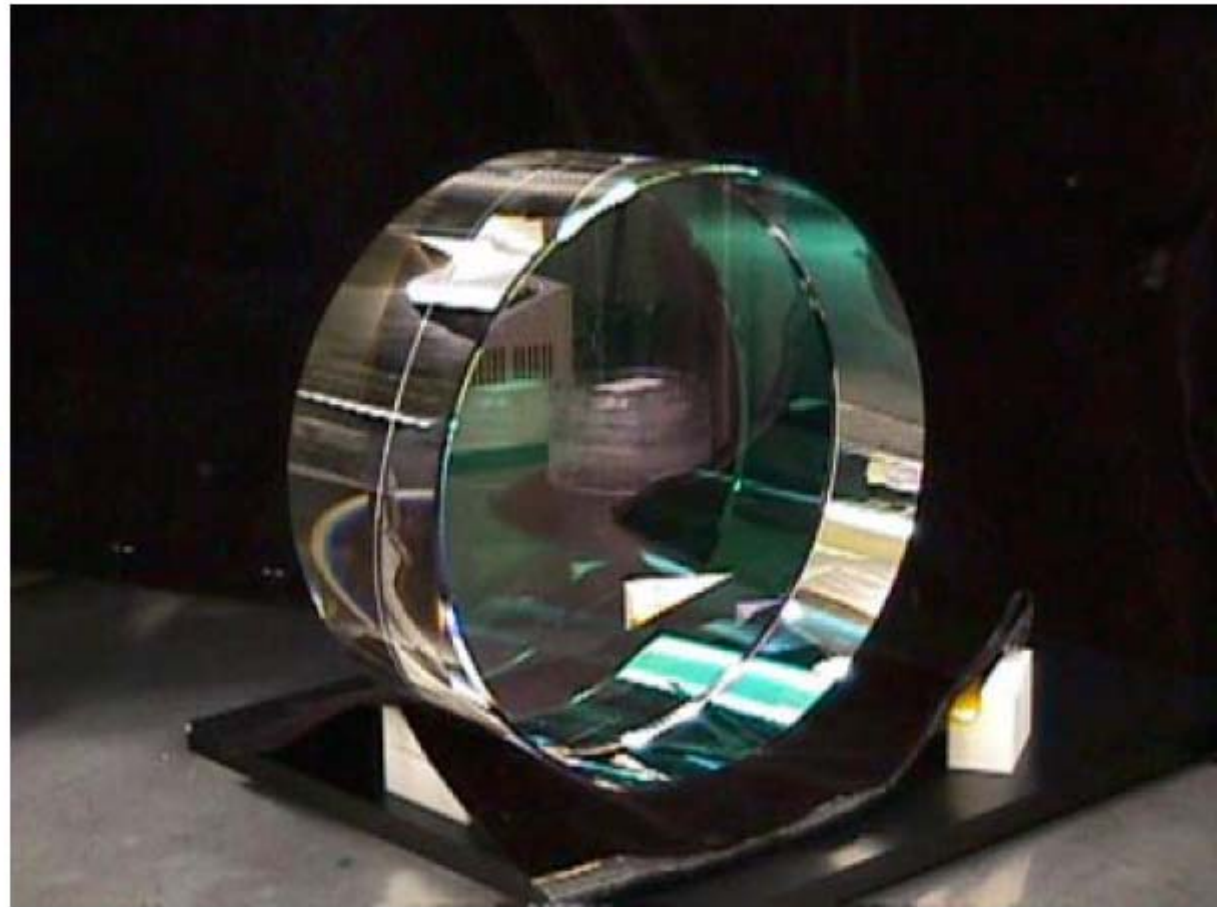
radii of curvature matched  $< 3\%$

## Coating

Scatter  $< 50 \text{ ppm}$

Absorption  $< 2 \text{ ppm}$

Uniformity  $< 10^{-3}$





# LIGO

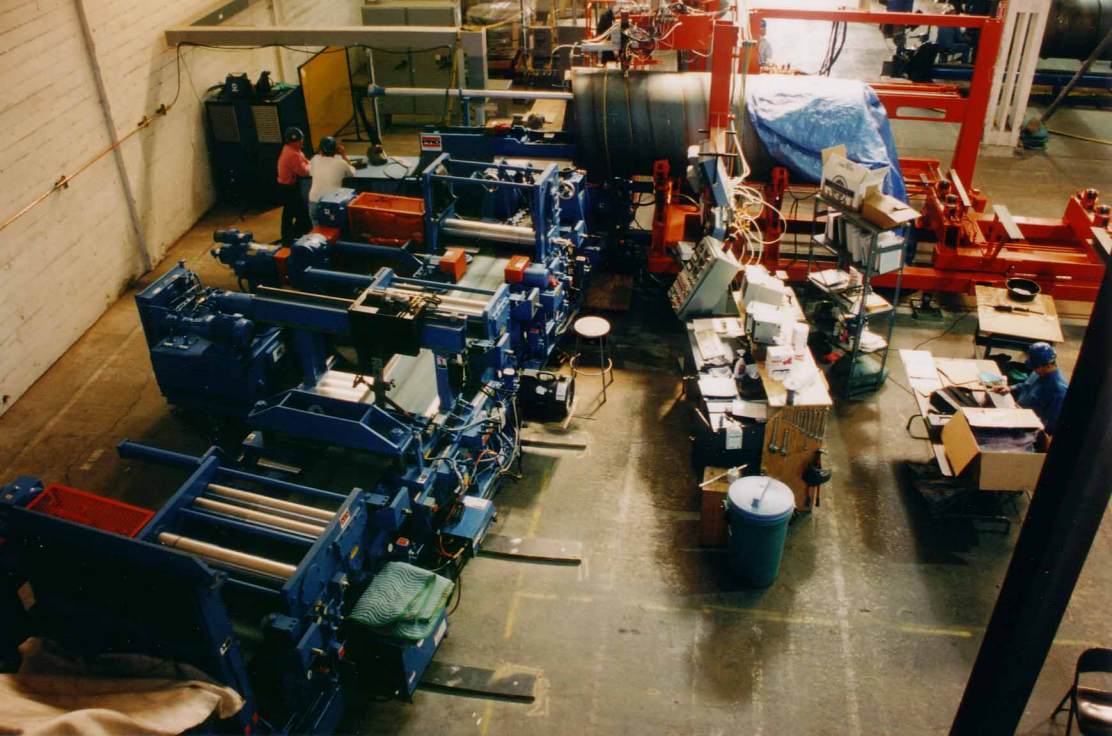


## Core Optics *installation and alignment*



# LIGO Beam Tubes

- Interaction region between gravitational waves and laser interferometers
  - ›› 16 km of vacuum tubing at two sites
  - ›› initial detectors require  $10^{-7}$  torr
  - ›› ultimate detectors require  $10^{-10}$  torr
  - ›› needs to be economical
    - minimal pumping, exploit passive nature of system
    - new welding techniques - continuous spiral weld in 304L
    - low outgassing materials - air bake to reduce hydrogen outgassing, total low 150C bake to reduce water and heavier molecule outgassing
    - mass production cleaning
    - global positioning system alignment









OVER SIZE LOAD

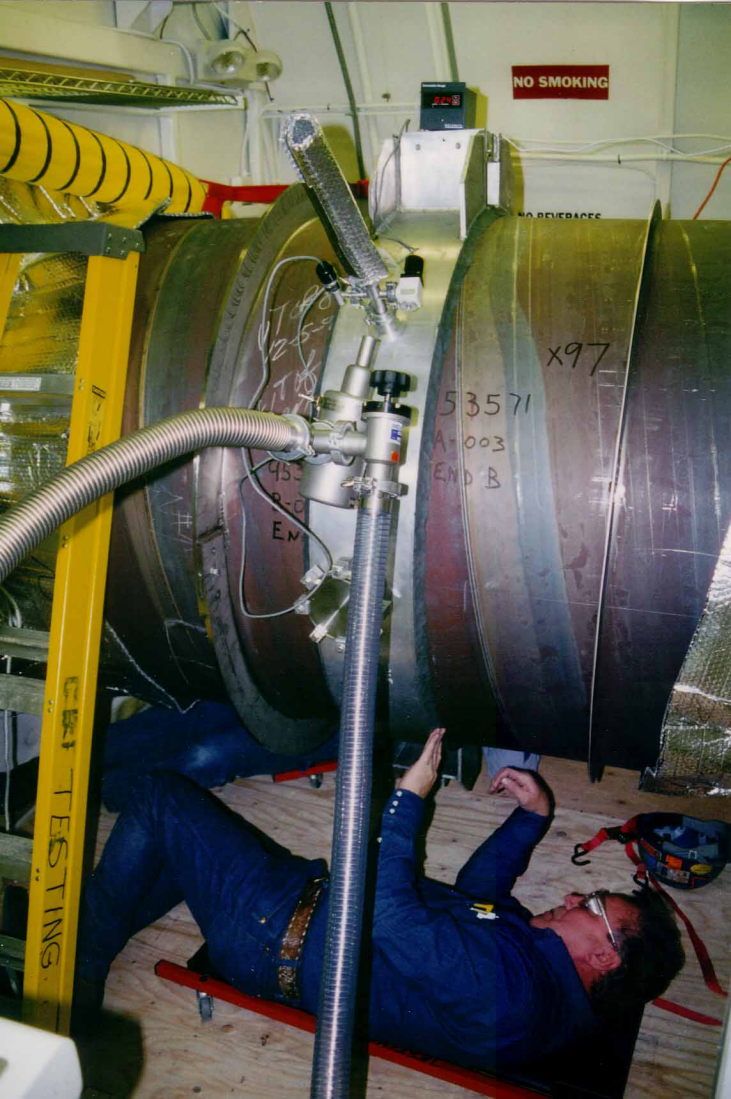
Lampson  
CPT

CPT



NO SMOKING

NO BEVERAGES



x97

53571  
A-003  
END B

T80  
255  
T80  
455  
R-0  
EM

TESTING



SA 11 8



# BEAM TUBE SCIENTIFIC REQUIREMENTS

- VACUUM REQUIREMENTS

- ›› Residual gas
  - Leak requirements
- ›› Contamination
- ›› Operational requirements
  - Pump down time
  - Isolation from chambers
  - Reliability

- MECHANICAL AND OPTICAL REQUIREMENTS

- ›› Clear Aperture
- ›› Forward and Backscatter from walls and baffles
- ›› Motion of tube walls and baffles

# BEAM TUBE REQUIREMENTS

- LEAK LIMITS

- ›› Component Level

- $1 \times 10^{-10}$  torr liters/sec

- ›› 2 km module with 2500 liter/sec end pumps

- $1 \times 10^{-9}$  torr liters/sec

- CONTAMINATION ON OPTICS

- ›› less than 1 monolayer of hydrocarbon/month

# BEAM TUBE REQUIREMENTS

- OPERATIONAL REQUIREMENTS

- ›› Time to reach required pressure < 2 months
- ›› Capability to isolate beamtubes from chambers
- ›› Reliability: leak free state for > 20 years

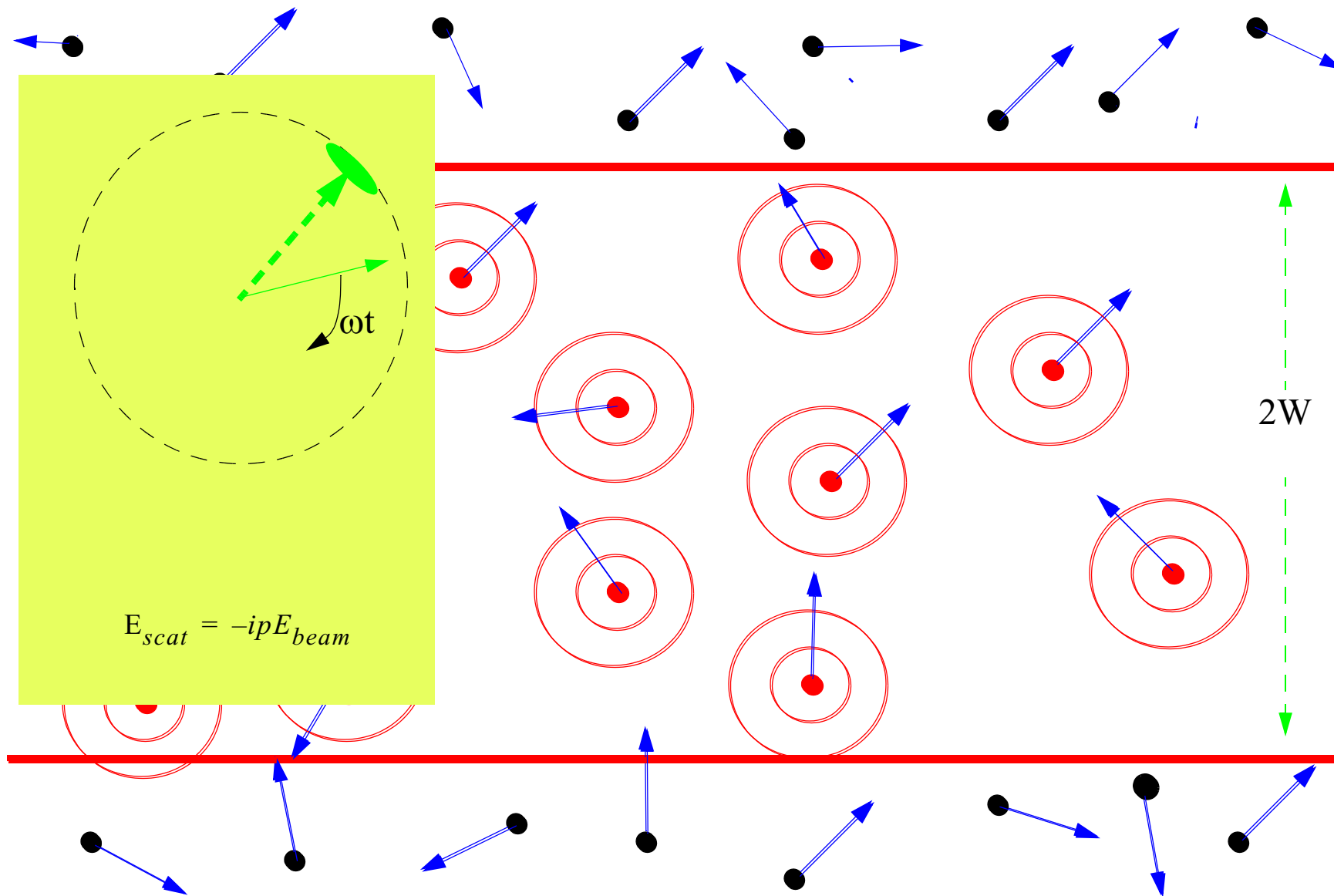
- MECHANICAL AND OPTICAL  
REQUIREMENTS

- ›› Unobstructed aperture 1 meter
- ›› Backscatter from baffles and tube between 0.5 to 1 micron wavelengths <  $2 \times 10^{-3} \text{ sr}^{-1}$  for angles of incidence greater than 45 degrees
- ›› Motion of tubes at baffles not to exceed 2 x the ambient seismic noise except in narrow bands

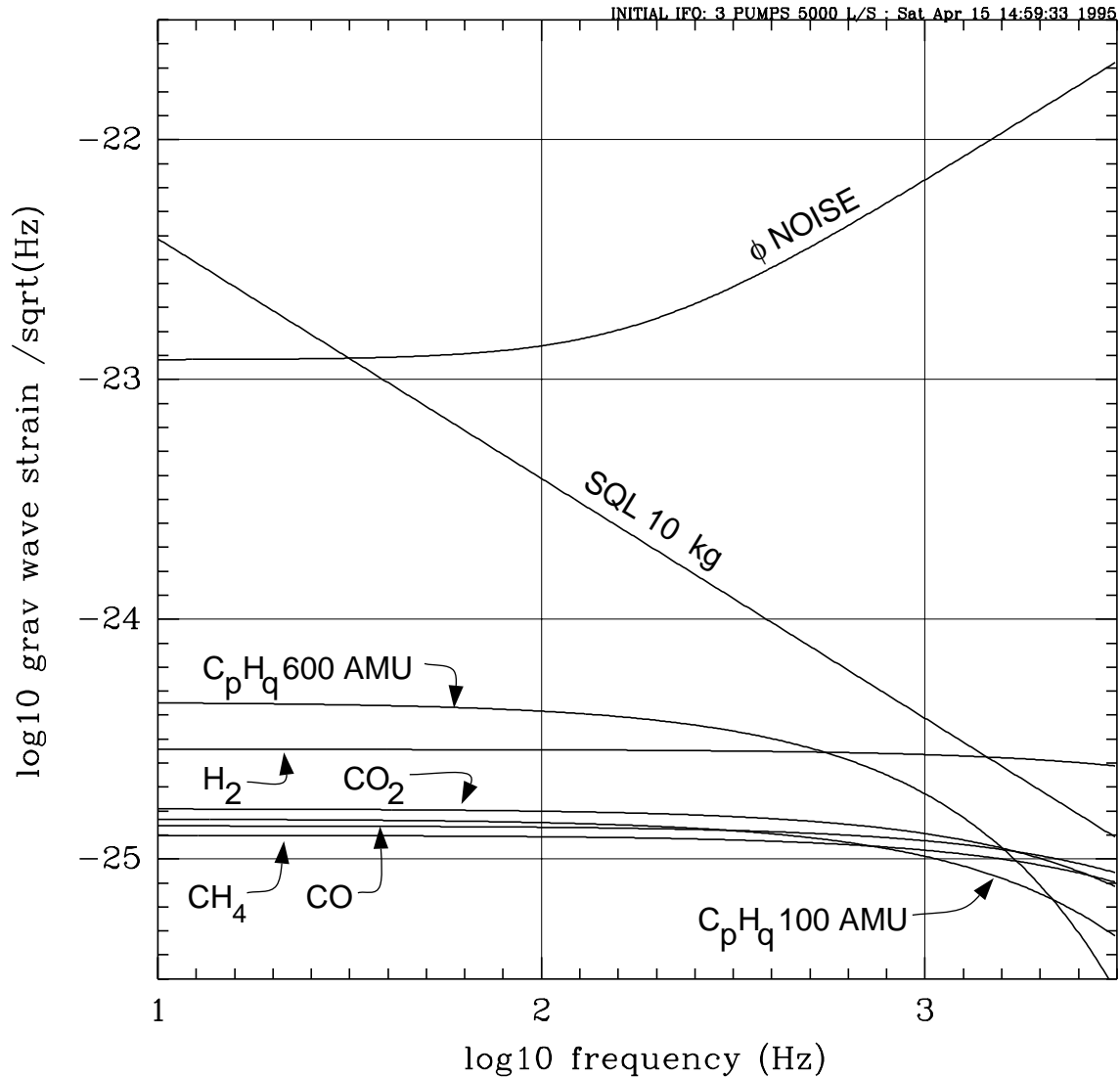
# Beam Tube Properties

module length	2 km
25 cm diameter pump ports/module	9
radius of beam tube	62 cm
volume of module	$4.831 \times 10^6$ liters
area of module	$1.55 \times 10^8$ cm <sup>2</sup>
initial pumping speed/surface area	$1.94 \times 10^{-5}$ liters/sec/cm <sup>2</sup>
length/short section	$1.90 \times 10^3$ cm
wall thickness	$3.23 \times 10^{-1}$ cm
stiffener ring spacing	76 cm
stiffening ring width	$4.76 \times 10^{-1}$ cm
stiffening ring height	4.45 cm
expansion joint wall thickness	$2.67 \times 10^{-1}$ cm
expansion joint convolutions	9
expansion joint longitudinal spring rate	$1.5 \times 10^9$ dynes/cm

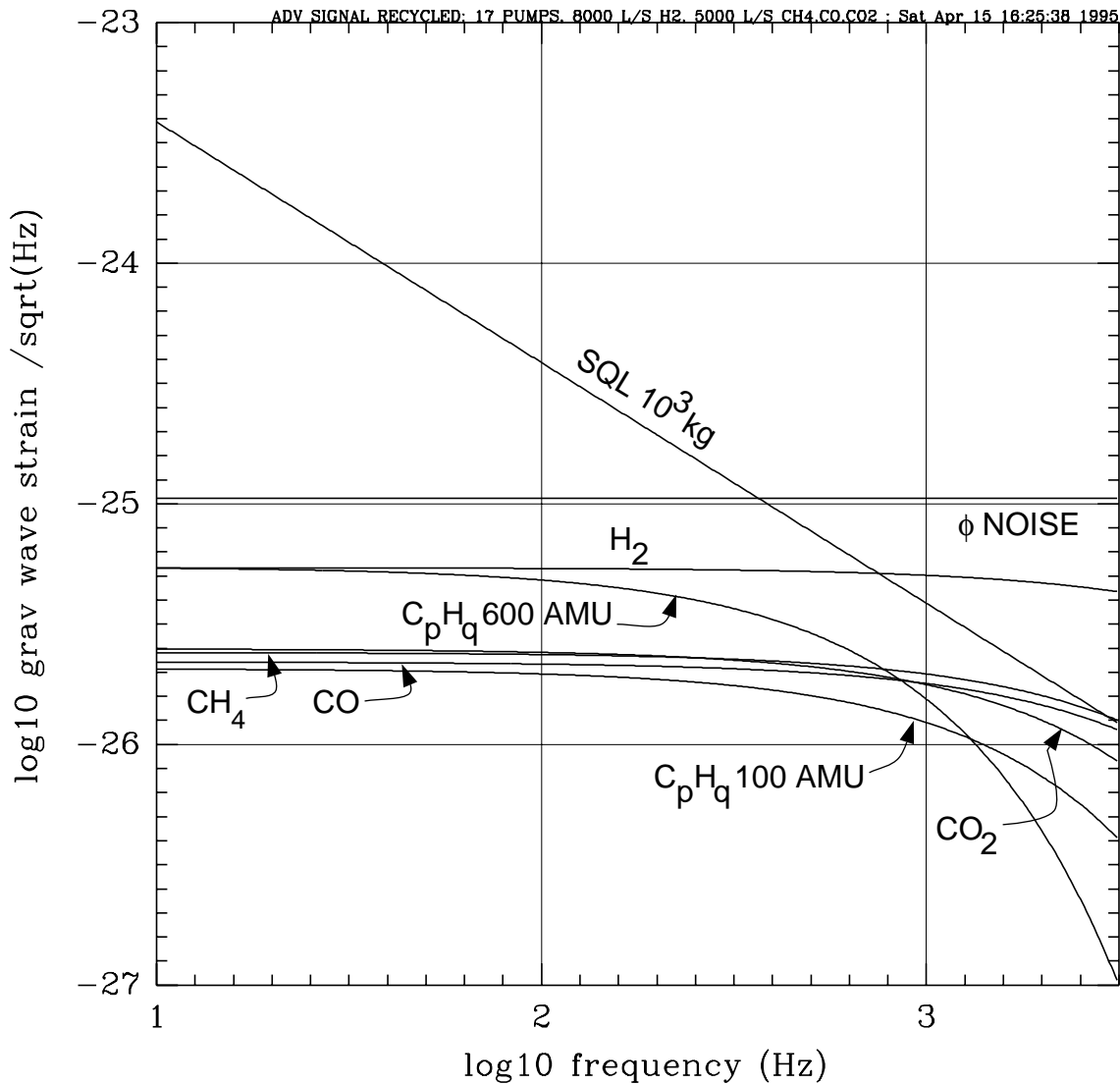
# Phase noise from molecular scattering



# Initial Interferometer Noise Budget



# Advanced Interferometer Noise Budget



Advanced amplitude recycled interferometer parameters:

$$A_m = 10^{-5}$$

$$P_{in} = 100 \text{ W}$$

$$P_{circ} \sim 1 \text{ MW}$$

$$\epsilon_{opt} = 0.3$$

$$\lambda = 1.06 \mu$$

# BEAM TUBE BAKEOUT

- Requirements and goals

- ›› Initial interferometer residual gas phase noise (100Hz)

$$h(f) < 5 \times 10^{-24}$$

- ›› Advanced interferometer residual gas phase noise (100Hz)

$$h(f) < 1.5 \times 10^{-25}$$

- ›› Relation between pressure and phase noise

$$h(f) = 4.8 \times 10^{-21} R \left( \frac{x}{H_2} \right) \sqrt{\langle P(\text{torr}) \rangle_L}$$



# BEAM TUBE BAKEOUT

**Table 1: Residual gas phase noise factor and average pressure**

<b>Gas Species</b>	<b>R(x/H<sub>2</sub>)</b>	<b>Requirement (torr)</b>	<b>Goal (torr)</b>
H <sub>2</sub>	1.0	1×10 <sup>-6</sup>	1×10 <sup>-9</sup>
H <sub>2</sub> O	3.3	1×10 <sup>-7</sup>	1×10 <sup>-10</sup>
N <sub>2</sub>	4.2	6×10 <sup>-8</sup>	6×10 <sup>-11</sup>
CO	4.6	5×10 <sup>-8</sup>	5×10 <sup>-11</sup>
CO <sub>2</sub>	7.1	2×10 <sup>-8</sup>	2×10 <sup>-11</sup>
CH <sub>4</sub>	5.4	3×10 <sup>-8</sup>	3×10 <sup>-11</sup>
AMU 100 hydrocarbon	38.4	7.3×10 <sup>-10</sup>	7×10 <sup>-13</sup>
AMU 200 hydrocarbon	88.8	1.4×10 <sup>-10</sup>	1.4×10 <sup>-13</sup>
AMU 300 hydrocarbon	146	5×10 <sup>-11</sup>	5×10 <sup>-14</sup>
AMU 400 hydrocarbon	208	2.5×10 <sup>-11</sup>	2.5×10 <sup>-14</sup>
AMU 500 hydrocarbon	277	1.4×10 <sup>-11</sup>	1.4×10 <sup>-14</sup>
AMU 600 hydrocarbon	345	9.0×10 <sup>-12</sup>	9.0×10 <sup>-15</sup>

# BEAM TUBE BAKEOUT

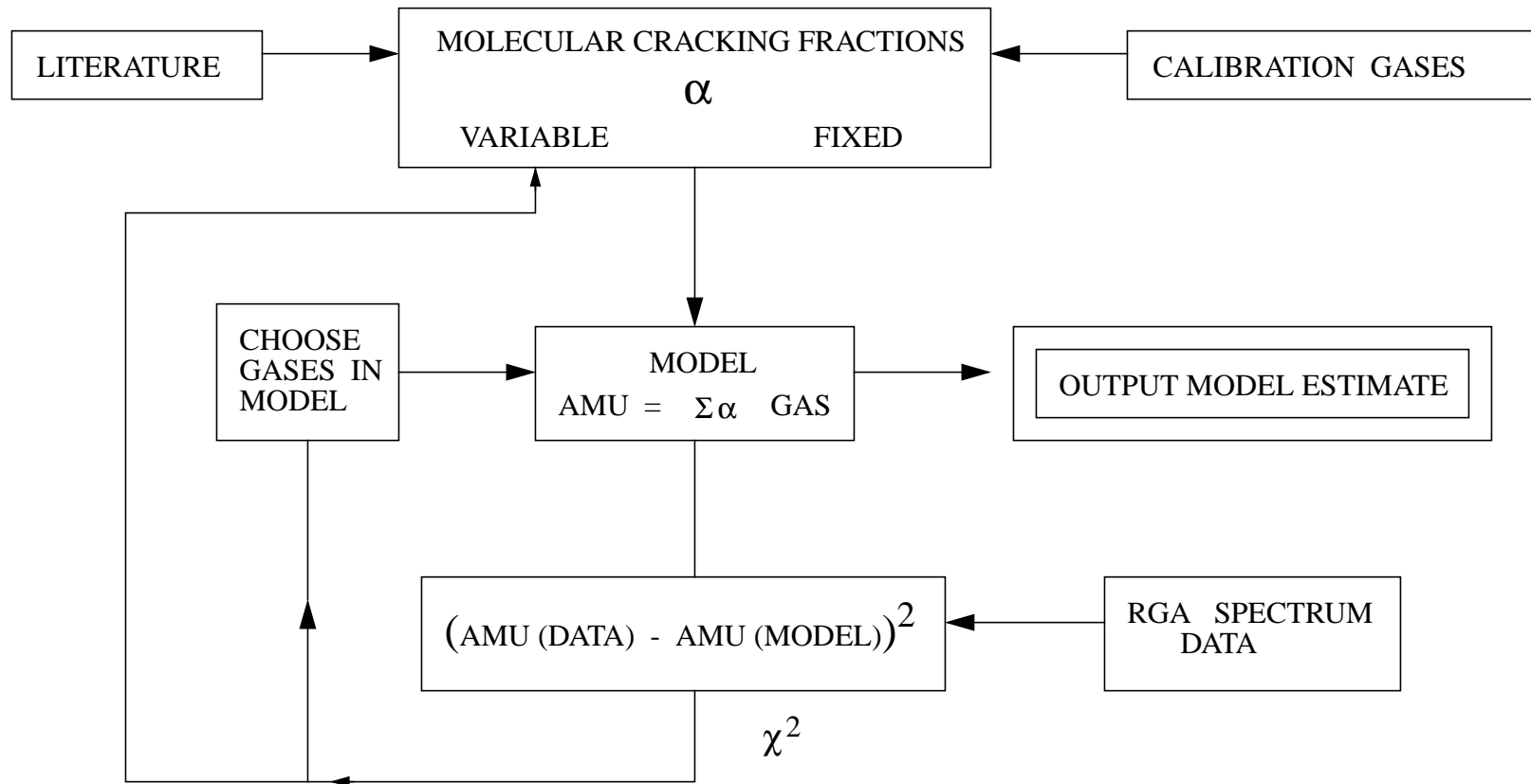
- Average pressure and outgassing rate

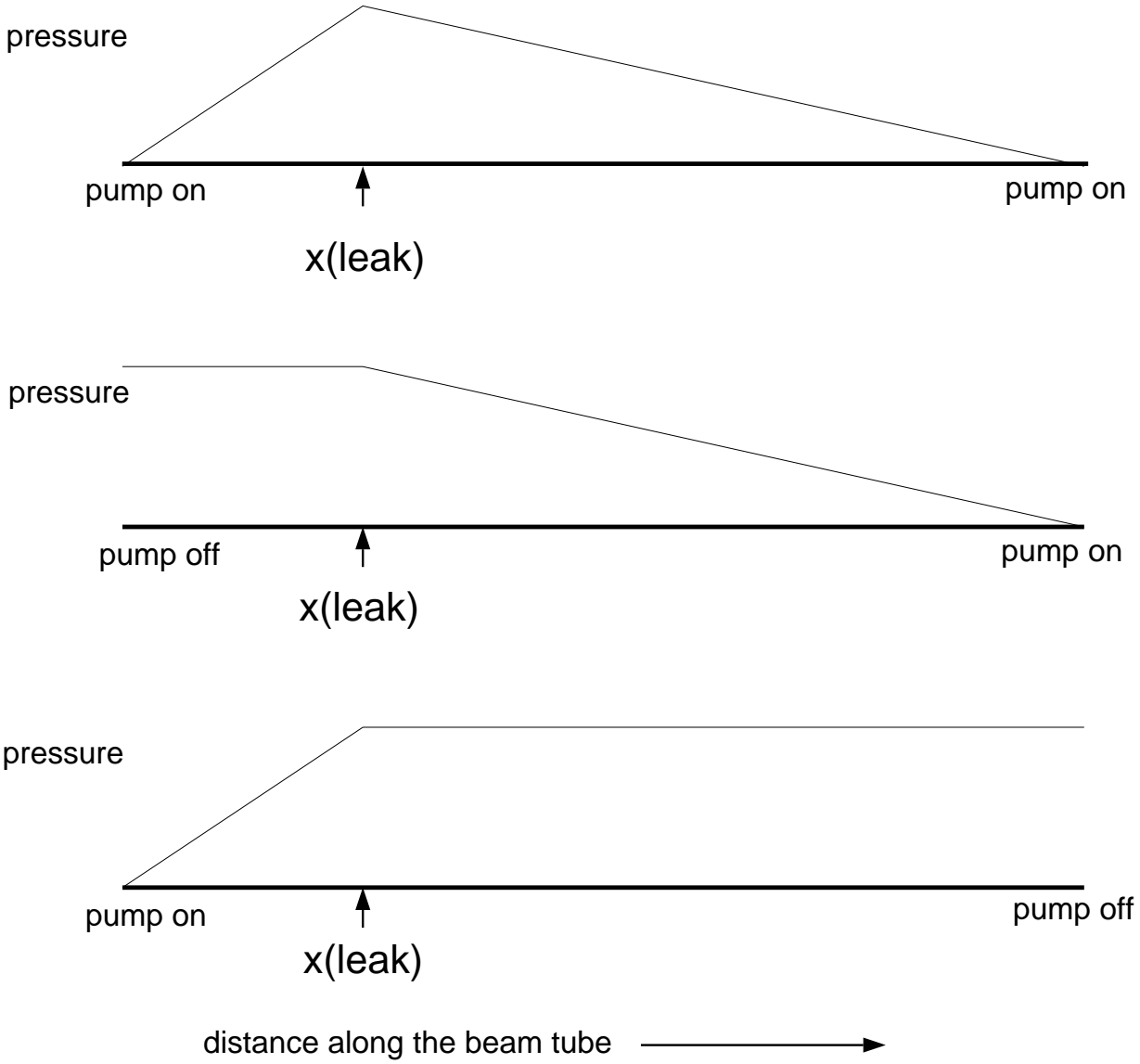
$$\langle p \rangle_L = J \left[ \frac{2\pi a L}{nF} + \frac{L^2}{4va^2(n-1)^2} \right]$$

- Outgassing rate vs temperature and time

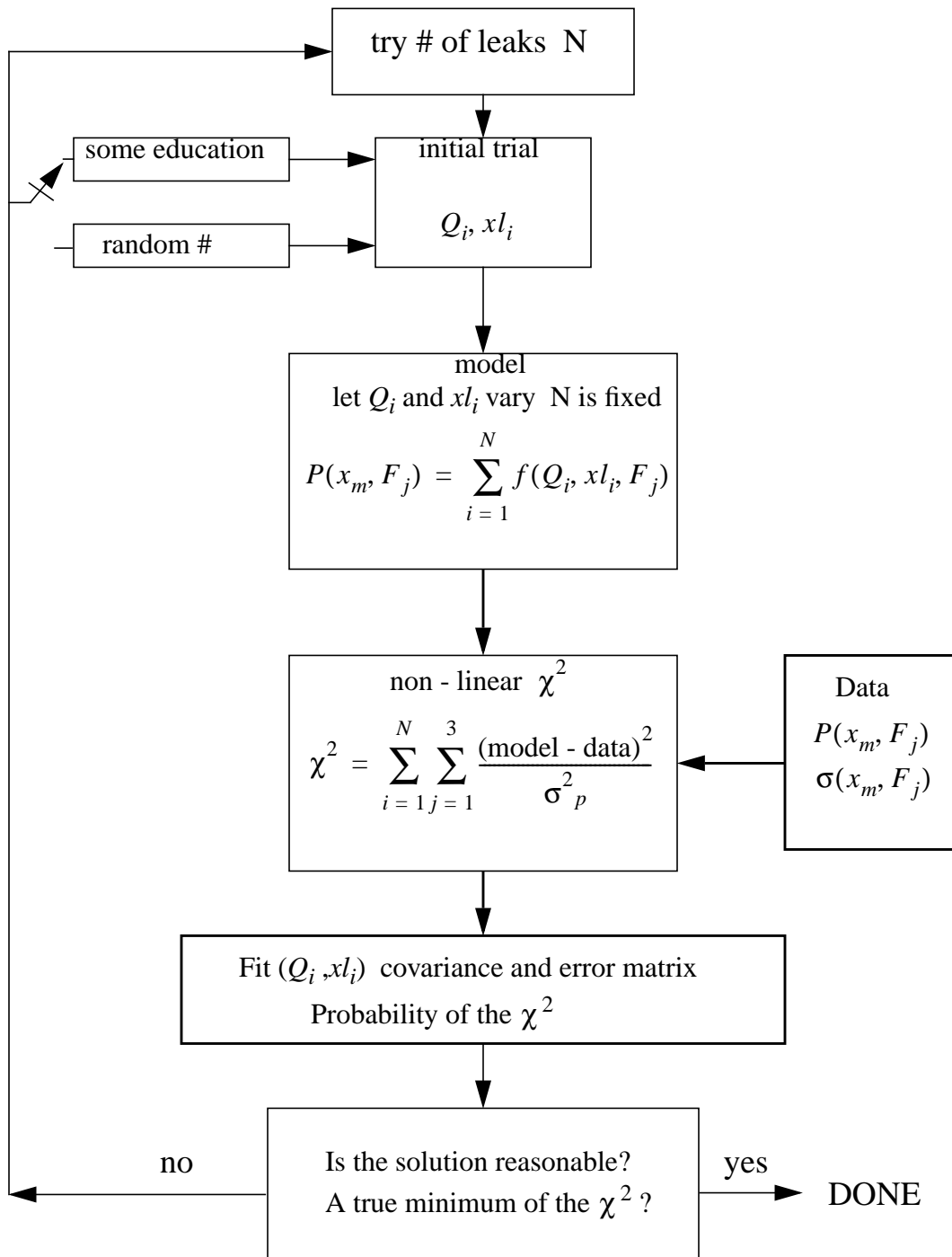
$$J(T) = ae^{-\frac{T_0}{T}}$$

- ›› Typical:  $5000 < T_0 < 10000$  K
- ›› Time dependence
  - $1/t$  surface adsorption with distribution of binding site energies
  - $(1/t)^{0.5}$  diffusion followed by evaporation





Leak pressure profiles in tube



Leak localization algorithm

# Beam Tube Cleaning

- Cleaning steps

- ›› Hot water and detergent - Mirachem 500 spray wash

- 30/1 water/Mirachem - 500

- 1 cc/ cm<sup>2</sup>

- ›› Steam rinse

- 2 cc/ cm<sup>2</sup>

- 7 - 8.5 atmospheres pressure

- 58 - 65 C surface temperature of steel

- ›› Applied by rotating wand that traverses the tube longitudinally at 20 cm / minute

- Surface analysis

- ›› Fourier Transform Infrared Spectroscopy FTIR

- Sample taken by pouring 2 - isopropanol in strip down tube

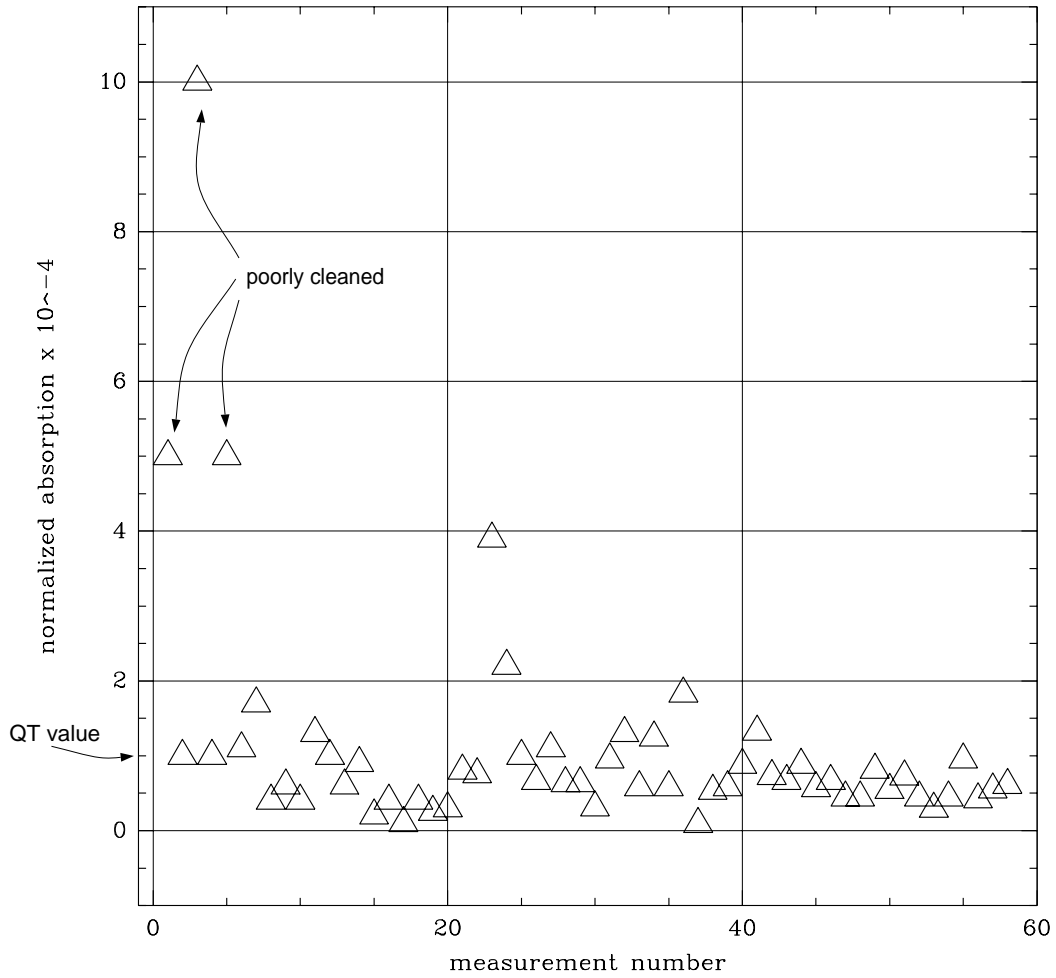
- Analysis made in professional testing laboratory



# Beam Tube Cleaning

- ›› Auger electron spectroscopy
  - Sample strips placed in tube
  - Analysis made in surface measurement lab after cleaning
  - Sensitive to elemental carbon
  - Useful to determine state of rinse by measurement of sodium and calcium
- ›› Water drop adhesion tests
  - Qualitative but can be made on location
  - Useful in diagnosis of oil layers (poor adhesion) and incomplete rinse of detergent (super adhesion and wetting).





Normalized absorption  $z$  at 2950 cm<sup>-1</sup>

$$z = \frac{(\ln(I/I_0)_{\text{sample}} - \ln(I/I_0)_{\text{reference}}) \times \text{KBr area} \times \text{sample volume in tube}}{\text{sample volume evaporated on KBr} \times \text{area of tube exposed}}$$

Typical values:

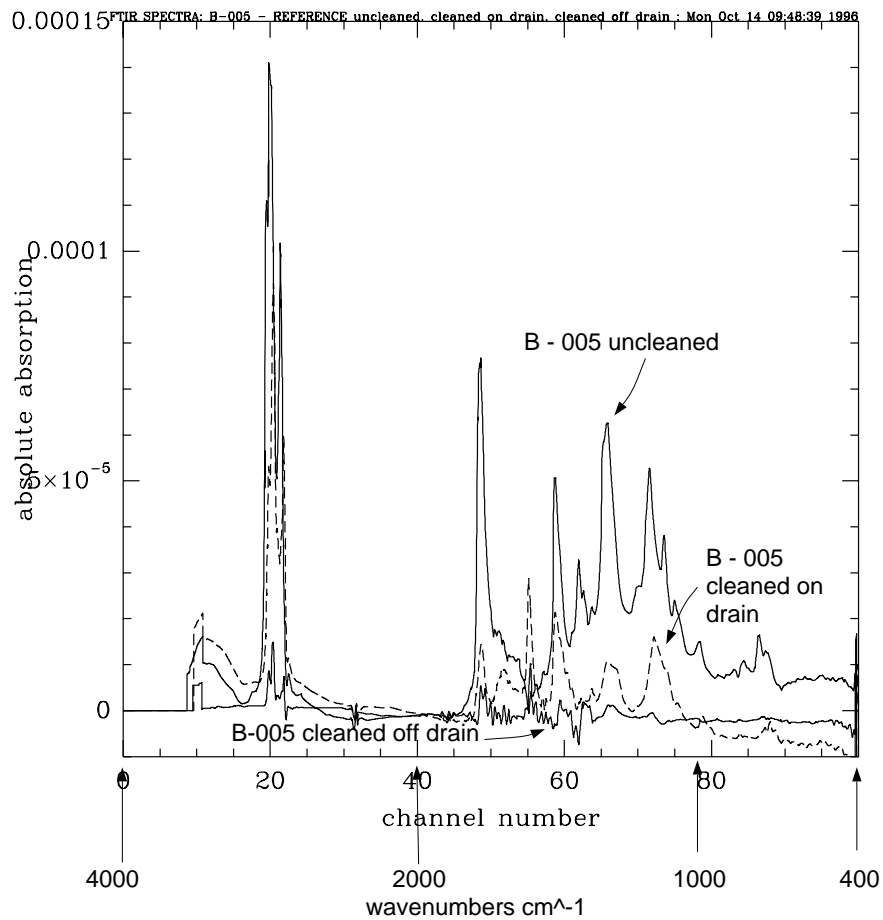
Area of tube exposed =  $2 \times 10^4$  cm<sup>2</sup>

Sample volume in tube = 2 liters

Sample evaporated = 200 cc

KBr area = 0.6 cm<sup>2</sup>

$z \approx 1 \times 10^{-4}$  corresponds to 0.1 monolayer of 100 amu hydrocarbon



Spectra of tube B-005 uncleaned, and cleaned with sample taken along and off the drain line. The off drain sample is more characteristic of the average wall condition. The spectra have had the reference spectrum of the isopropanol subtracted, hence the negative values of the absorption.

**Table 1: Auger analysis 270 ev Carbon line given in terms of  $10^3$  counts in 1.64 minutes vs  $A^+$  milling time**

<i>tube # or surface</i>	<i>condition</i>	<i>0 min</i>	<i>1 min</i>	<i>2 min</i>	<i>3 min</i>	<i>4 min</i>
22B	uncl	57.4	24.3	16.5	11.8	10.8
22B	cl	26.1	8.1	6.5	4.4	5.1
B-005	uncl	59.5	17.6	10.6	8.3	7.1±1.0
B-005	cl 1	24.3	5.2	2.3	1.0±1.0	0.0±1.0
B-005	cl 2	21.9	6.7	2.1	1.0±1.0	0.0±1.0
Oxidized	super cl	35.1	22.1	3.0	2.7±1.0	2.4±1.0
smooth	super cl	27.9	2.9	0.0±1.0		
rough	oily	61.9	64.9	63.2	62.3	62.3

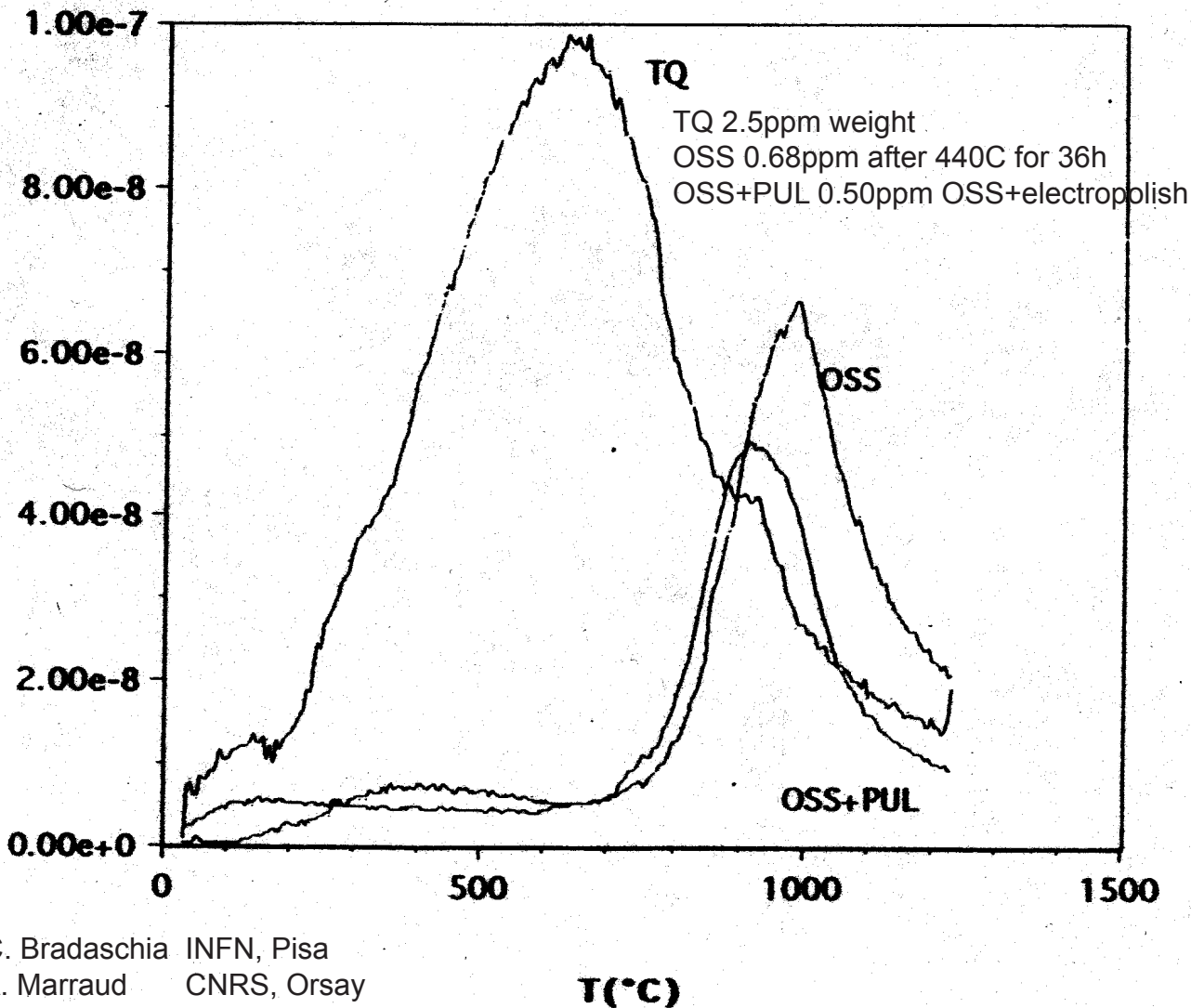
Conditions:

Incident electron energy = 5kV  
 Incident electron current = 100nA  
 Ion milling energy = 2kV  
 Ion current density =  $10\mu A/cm^2$

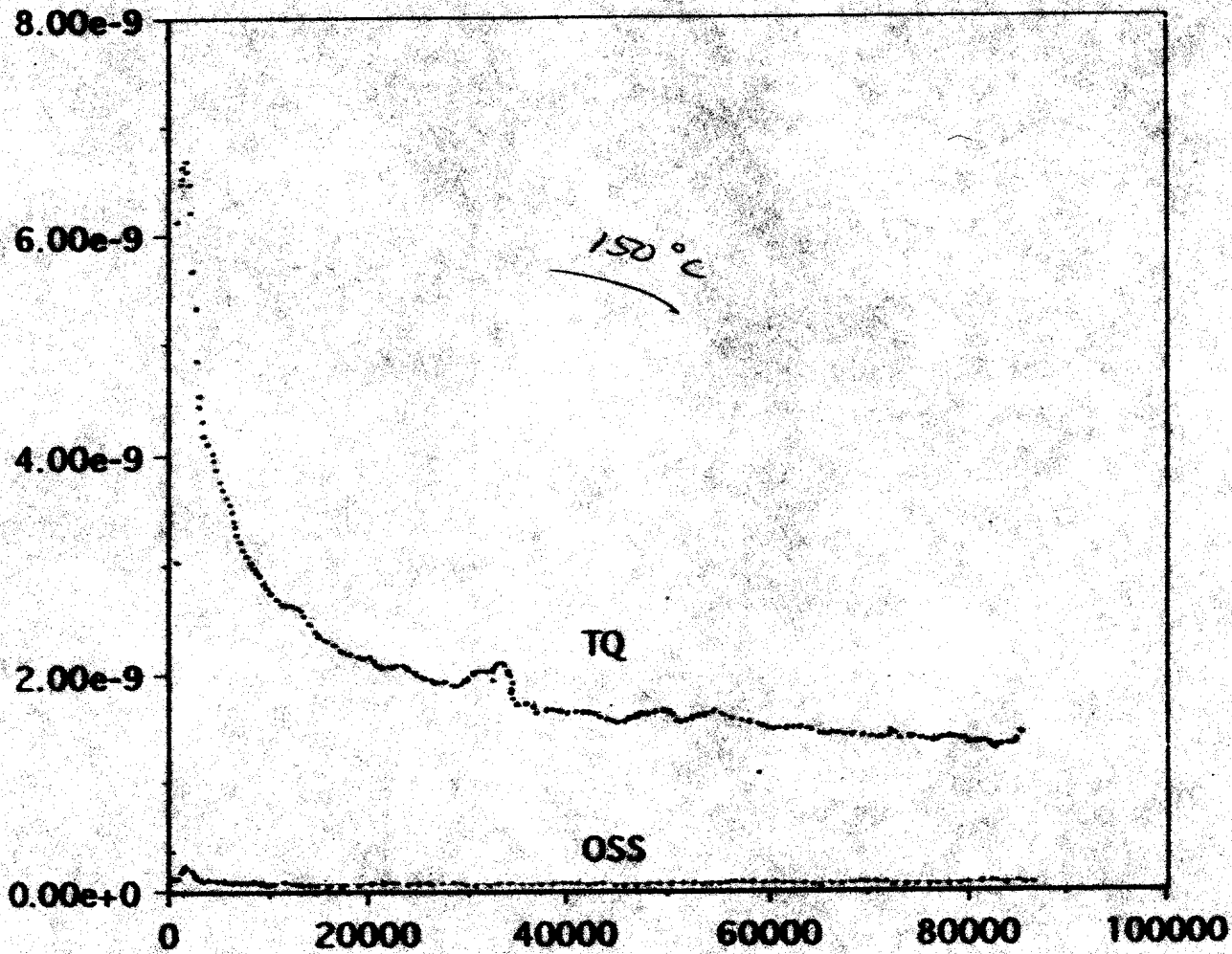
$5 \times 10^4$  counts of 270 ev electrons in 1.64 sec of acquisition time corresponds to 1 monolayer of carbon bearing molecule

# Hydrogen Reduction

- Dry air bake at 454C for 36 hours
  - Reduced 1 micron reflectivity of 304 L
  - Max temperature to minimize Carbide formation
- Mechanism:
  - tight (20000K) and loose (5000K) H binding sites
  - reduce density of loosely bound H and J(300K)
  - surface important for recombination (Myers)
  - Oxide layer not a significant factor
- Avoid reintroduction in welding
  - Dry purge gas until weld is cool
  - Clean weld rod

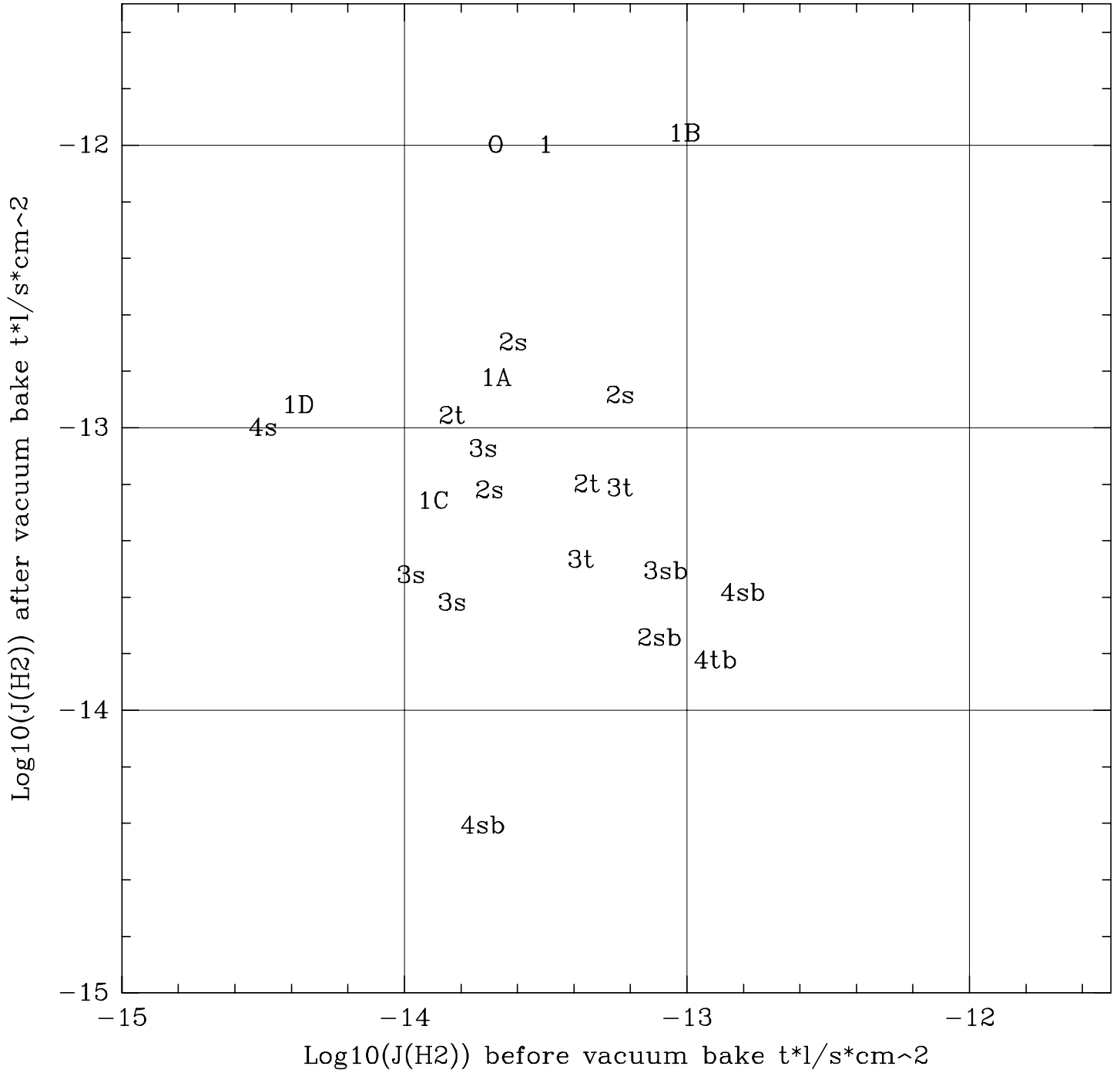


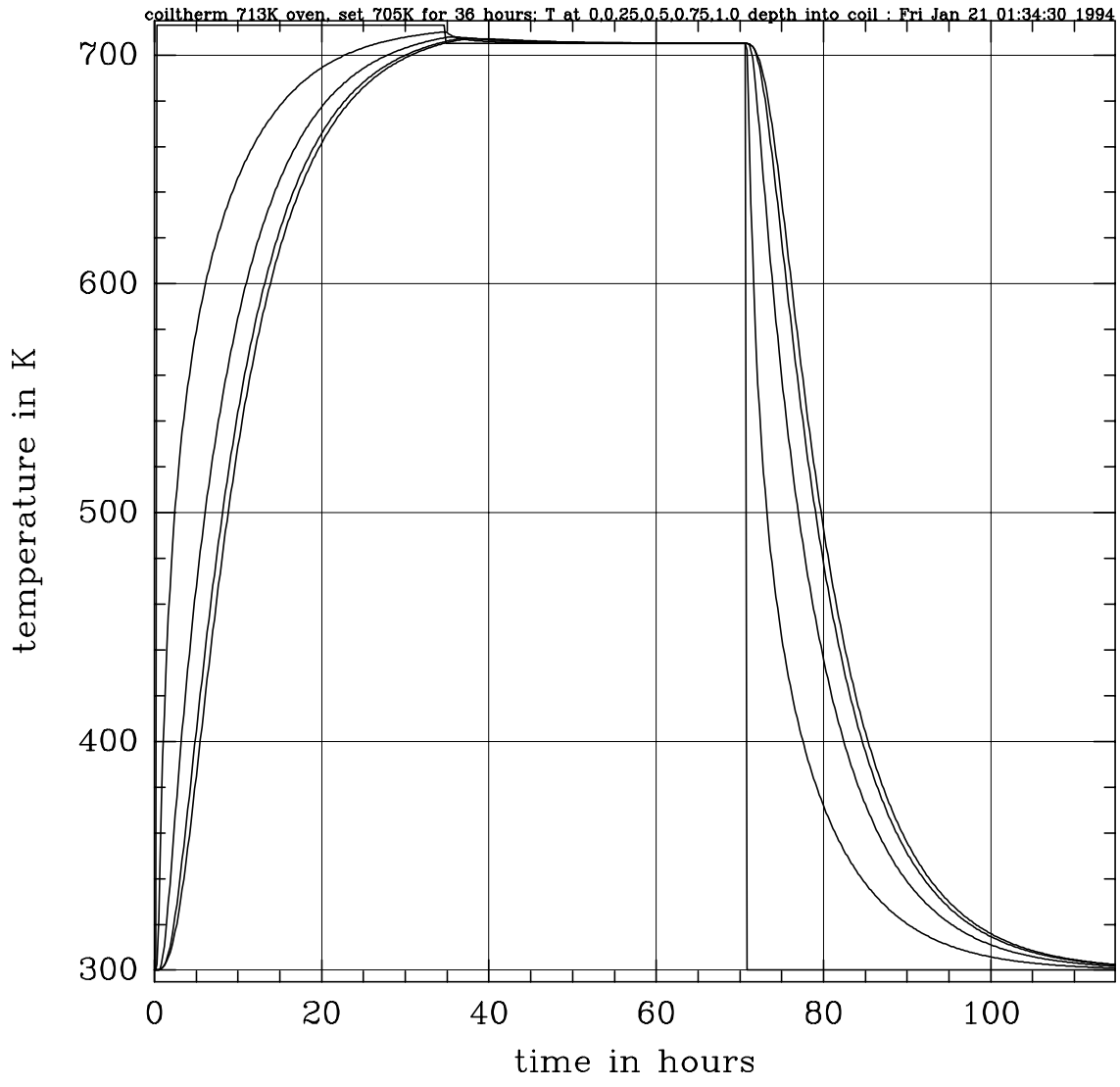
C. Bradaschia INFN, Pisa  
A. Marraud CNRS, Orsay



C. Bradaschia INFN, Pisa  
A. Marraud CNRS, Orsay

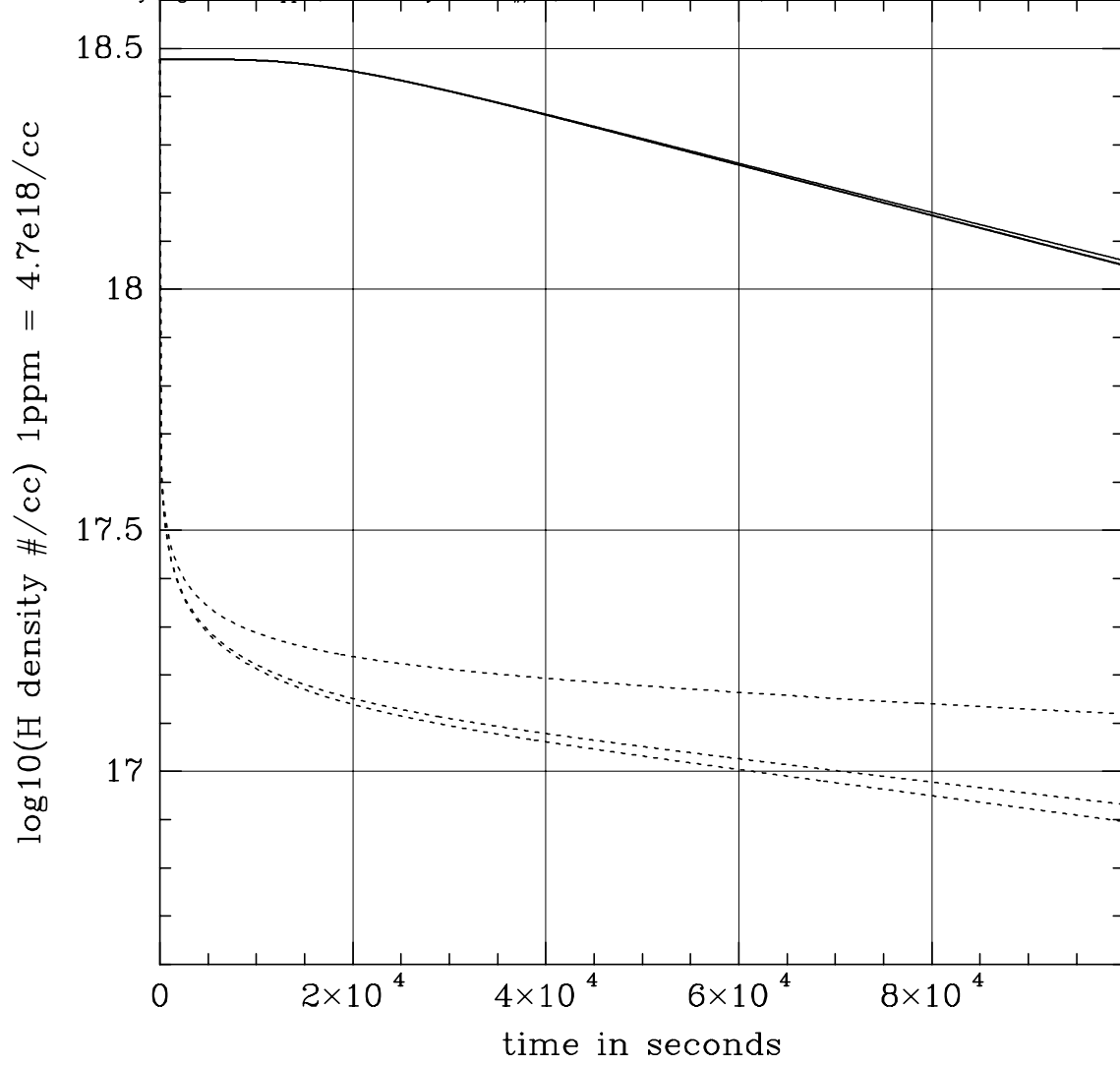
$t(s)$





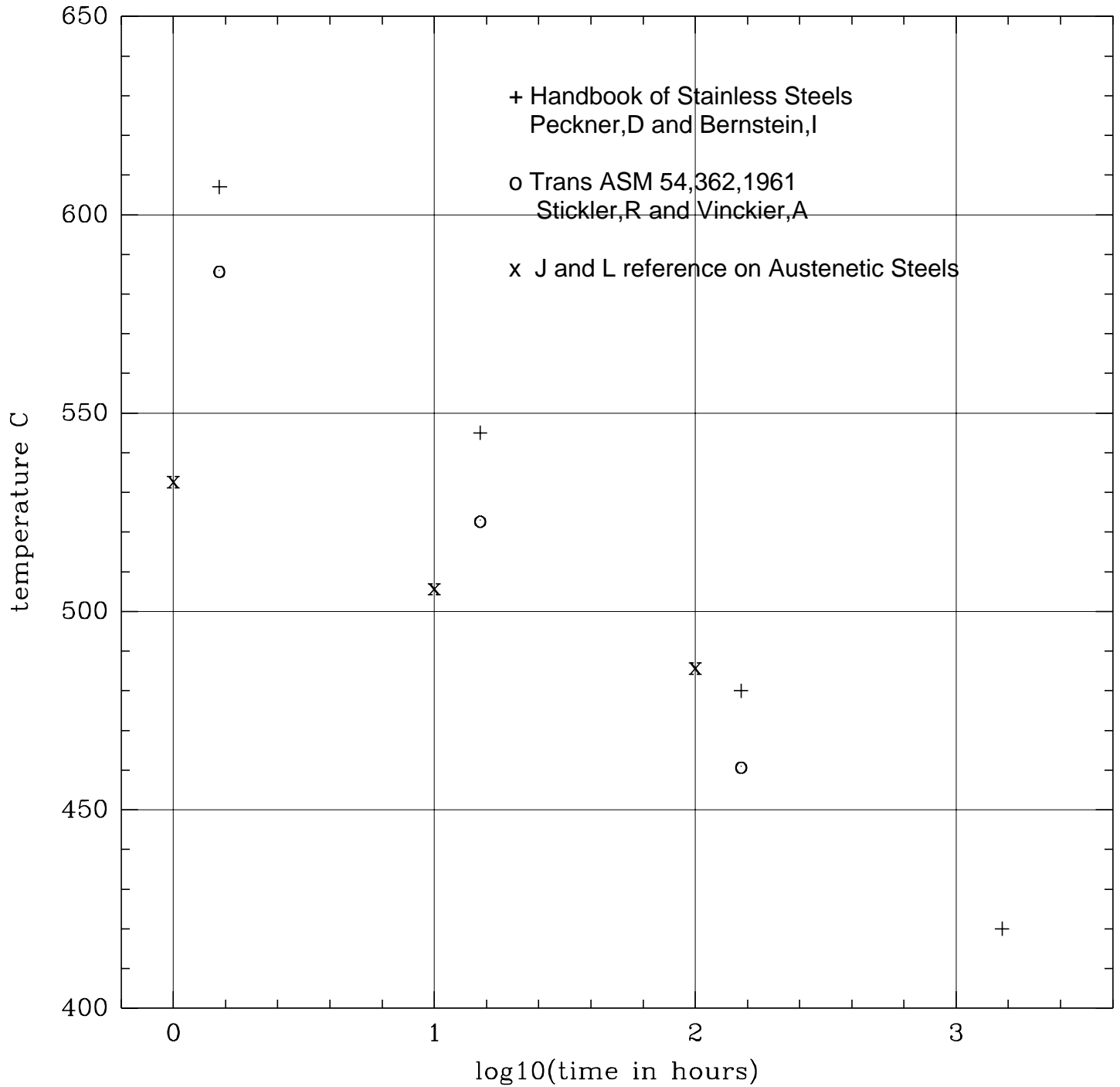


initial mobile hydrogen = 0.64 ppm, H2O density = 5e17 #/cc, T = 723K, solid inside, dots outside : Sat Dec 25 22:42:56 1993



Chromium Carbide formation boundary temperature vs time at temperature  
From several sources

Carbide Precipitation Boundary 304 SS .038 - .03% Carbon : Wed Mar 9 23:04:48 1994



## Heuristic Statistical Mechanics Model

Dubinin-Radushkevich (DR) equilibrium surface coverage:

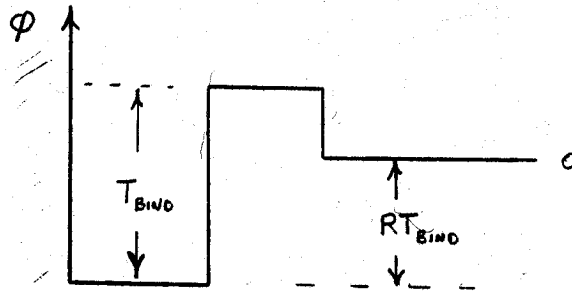
$$\frac{\sigma}{\sigma_m} = e^{-(T/T_0)^2 \ln^2(P/P_0)}$$

DR site distribution function:

$$\theta(T_{bind}) = (2T_{bind}/T_0^2) e^{-(T_{bind}/T_0)^2}$$

$$\int_0^\infty \theta(T_{bind}) \delta T_{bind} = 1$$

Heuristic surface potential:



Emission time:

$$\tau_{emit}(T_{bind}) = \tau_0 e^{T_{bind}/T}$$

Adsorption time:

$$\tau_{ads} = \frac{4n\sigma_0}{\alpha p v_{th} (1 + (1 - R)T_{bind}/T) e^{-(1-R)T_{bind}/T}}$$

Detailed balance per site:

$$\frac{dP(T_{bind}, t)}{dt} = -\frac{P(T_{bind}, t)}{\tau_{emit}} + \frac{(1 - P(T_{bind}, t))}{\tau_{ads}}$$

Integration:

$$P(T_{bind}, t) = P(T_{bind}, 0)e^{-t/\tau} + P_{equil}(T_{bind})(1 - e^{-t/\tau})$$

where

$$\tau = \frac{\tau_{emit}\tau_{ads}}{(\tau_{emit} + \tau_{ads})}$$

and

$$P_{equil}(T_{bind}) = \frac{\tau_{emit}}{(\tau_{emit} + \tau_{ads})}.$$

Incremental outgassing rate of band of sites:

$$dJ_{out}(t) = n\sigma_0 \theta(T_{bind}) \left( \frac{dP(T_{bind}, t)}{dt} \right) \delta T_{bind}$$

Aside: for  $P(T_{bind}, 0) = 1$  and  $\tau_{ads} \rightarrow \infty$

$$J_{out}(t, T) = \left( \frac{2n\sigma_0 T}{tT_0} \right) \int_0^a b \ln(y/a) e^{-(b \ln(y/a))^2} e^{-y} dy$$

where

$$b = T/T_0 \quad a = t/\tau_0$$

## Computational algorithm (waterbakesm.f)

Step time:

$$\Delta t / \tau_s = f \quad \tau_s = V / F$$

Probability computation over 1024 binding energies  $0 \rightarrow 3T_0$

$$P(T_{bind}, t_{j+1}) = P(T_{bind}, t_j) e^{-f\tau_s/\tau_j} + P_{equil}(T_{bind}, t_j) (1 - e^{-f\tau_s/\tau_j})$$

Surface coverage:

$$\sigma(t_{j+1}) = n\sigma_0 \sum_0^{3T_0} \theta(T_{bind}) P(T_{bind}, t_{j+1}).$$

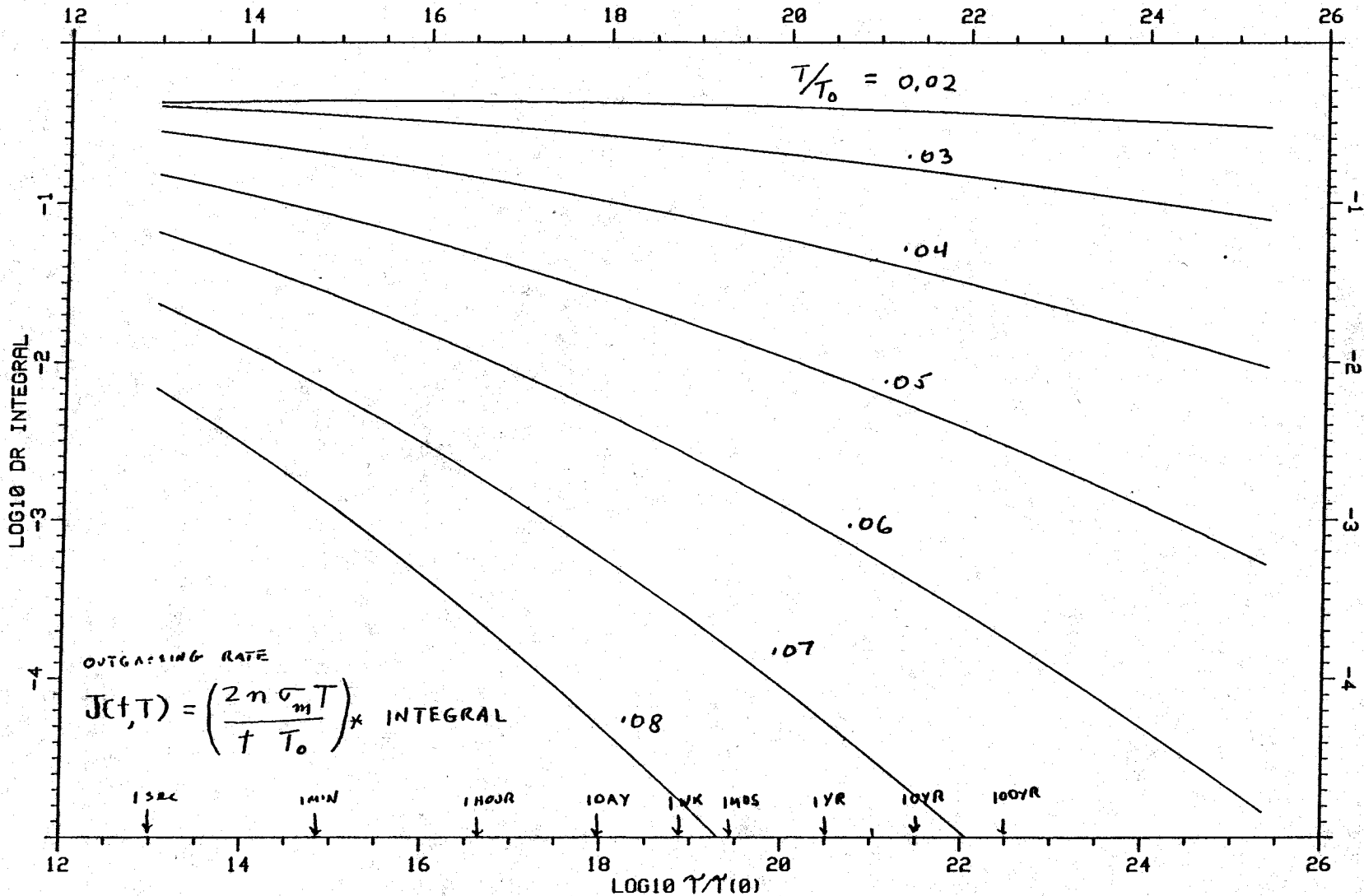
Outgassing rate:

$$J(t_{j+1}) = \frac{(\sigma(t_{j+1}) - \sigma(t_j))}{f\tau_s}$$

Pressure:

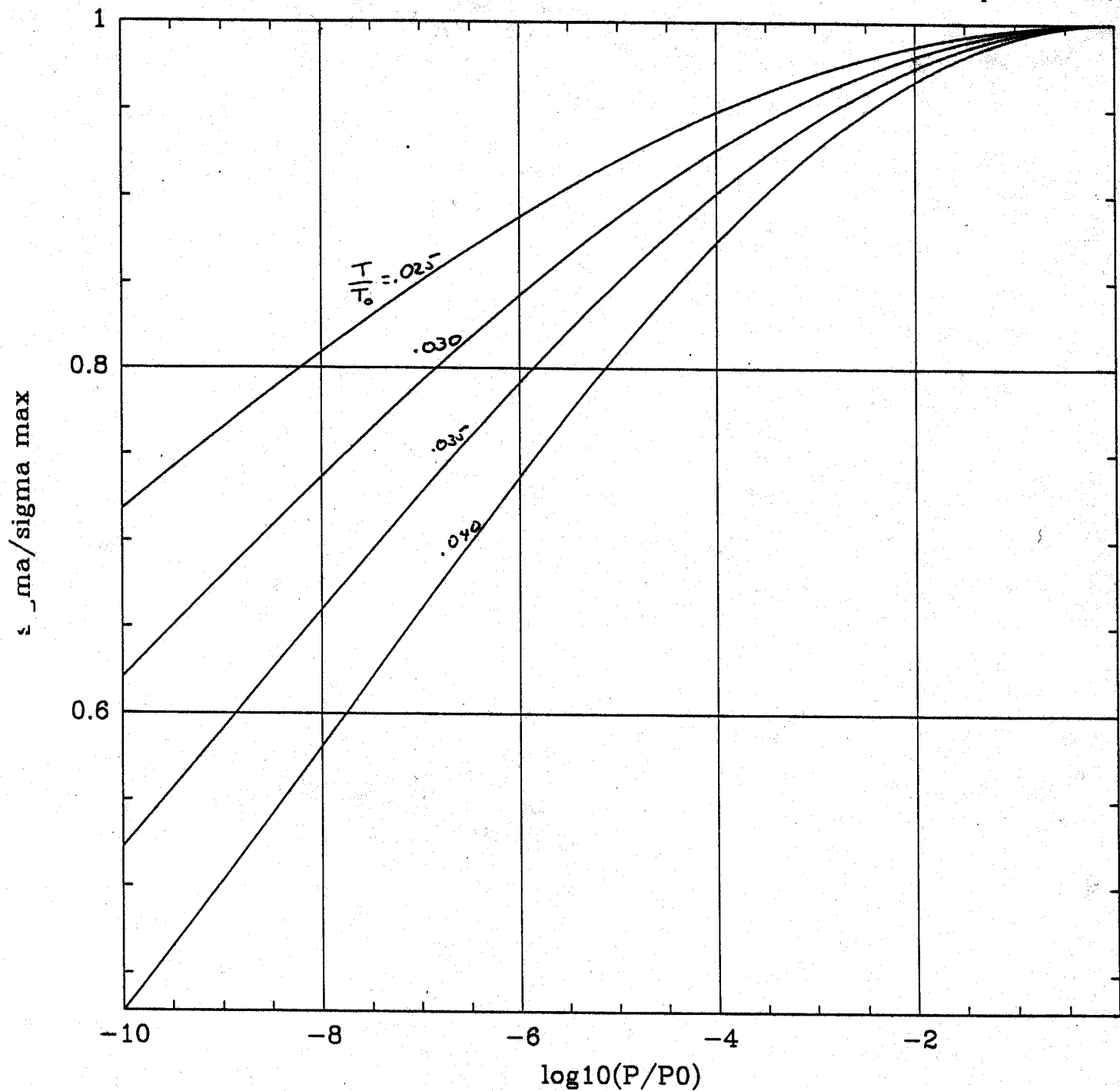
$$p(t_{j+1}) = p(t_j) e^{-f} + \left( \frac{J(t_j)A}{F} \right) (1 - e^{-f})$$

GO BACK AND DO IT AGAIN (new time and temperatures)



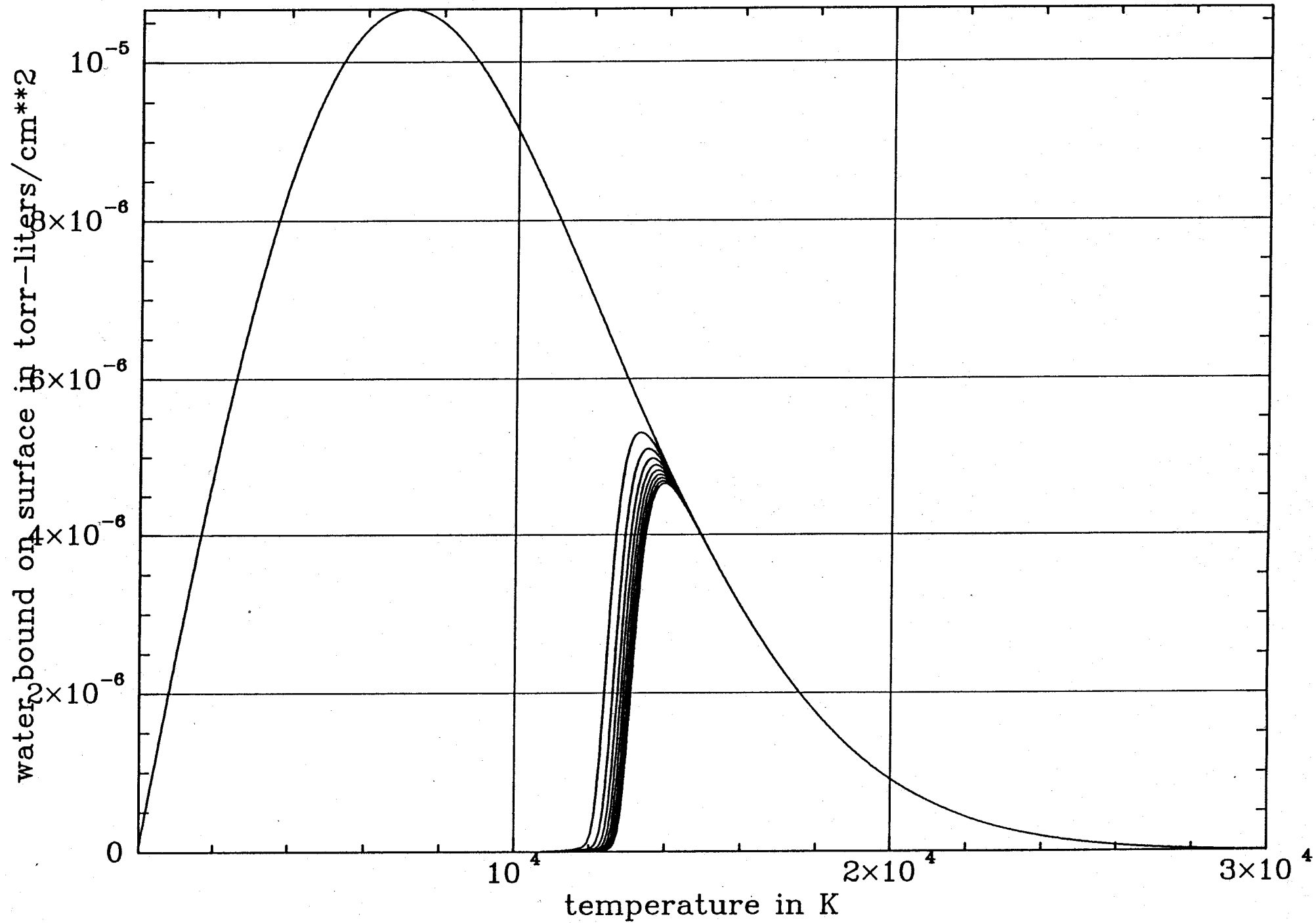
ASSUME  $\zeta_0 = 10^{-13}$  sec

DR INTEGRAL VS NORMALIZED PUMPING TIME



$$z_{\max} = \rho - \left(\frac{T}{T_0}\right)^2 \ln^2(P/P_0)$$

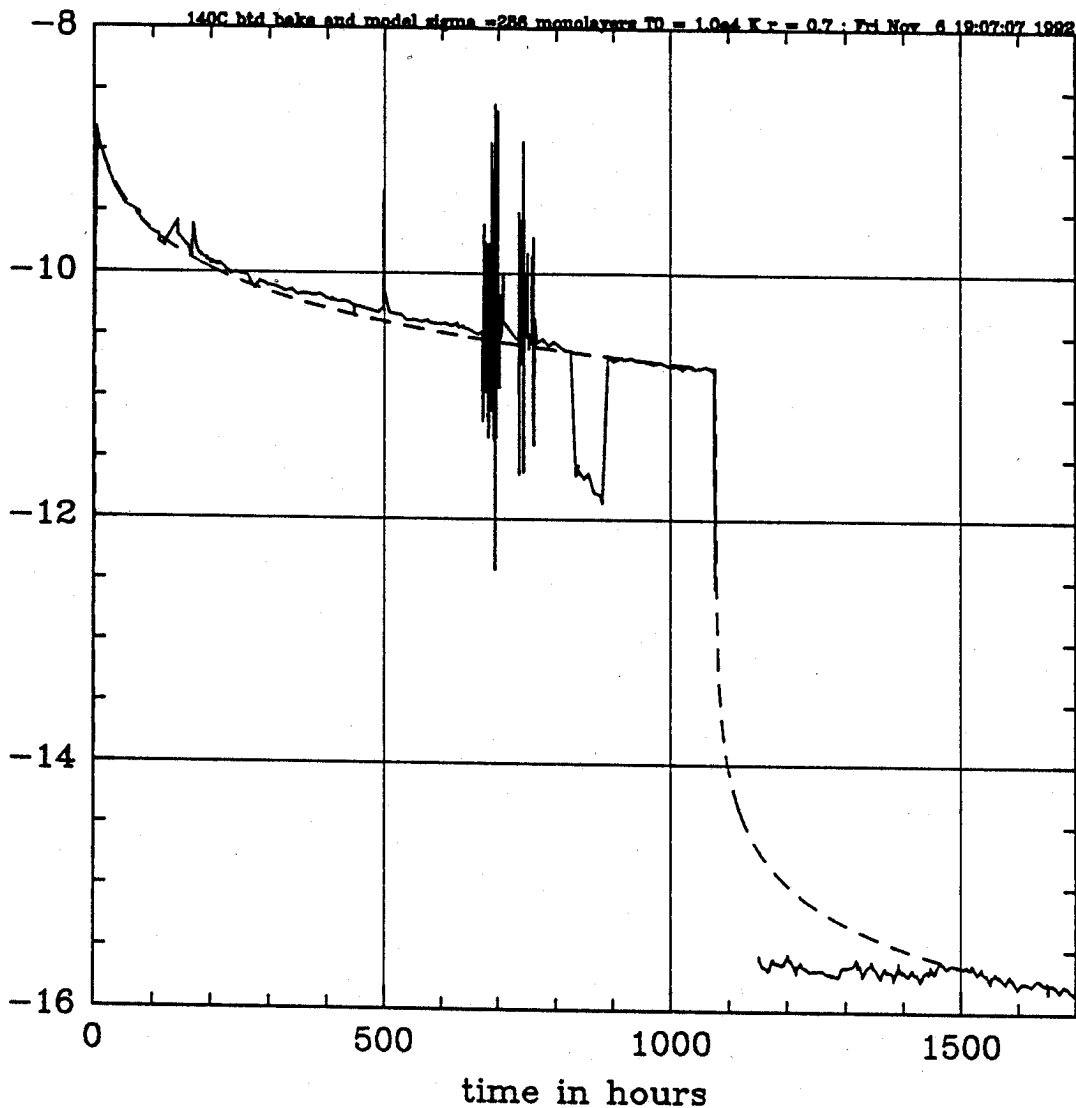
EQUILIBRIUM WITH SURFACE



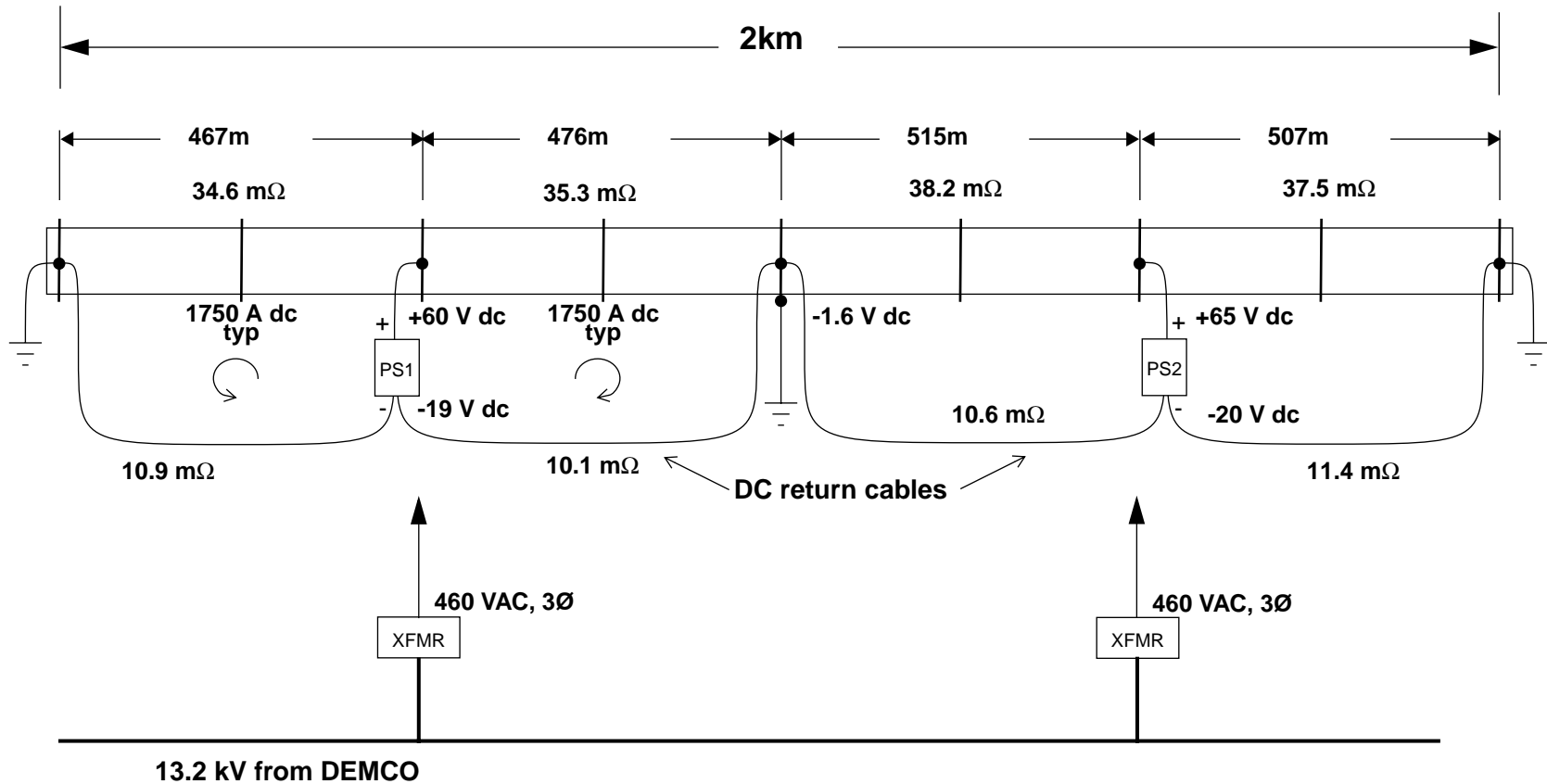


140C btd bake and model sigma = 285 monolayers T0 = 1.0e4 K r = 0.7 ; Fri Nov 6 19:07:07 1992

log<sub>10</sub>(H<sub>2</sub>O outgassing rate) torr lit/sec cm<sup>2</sup>



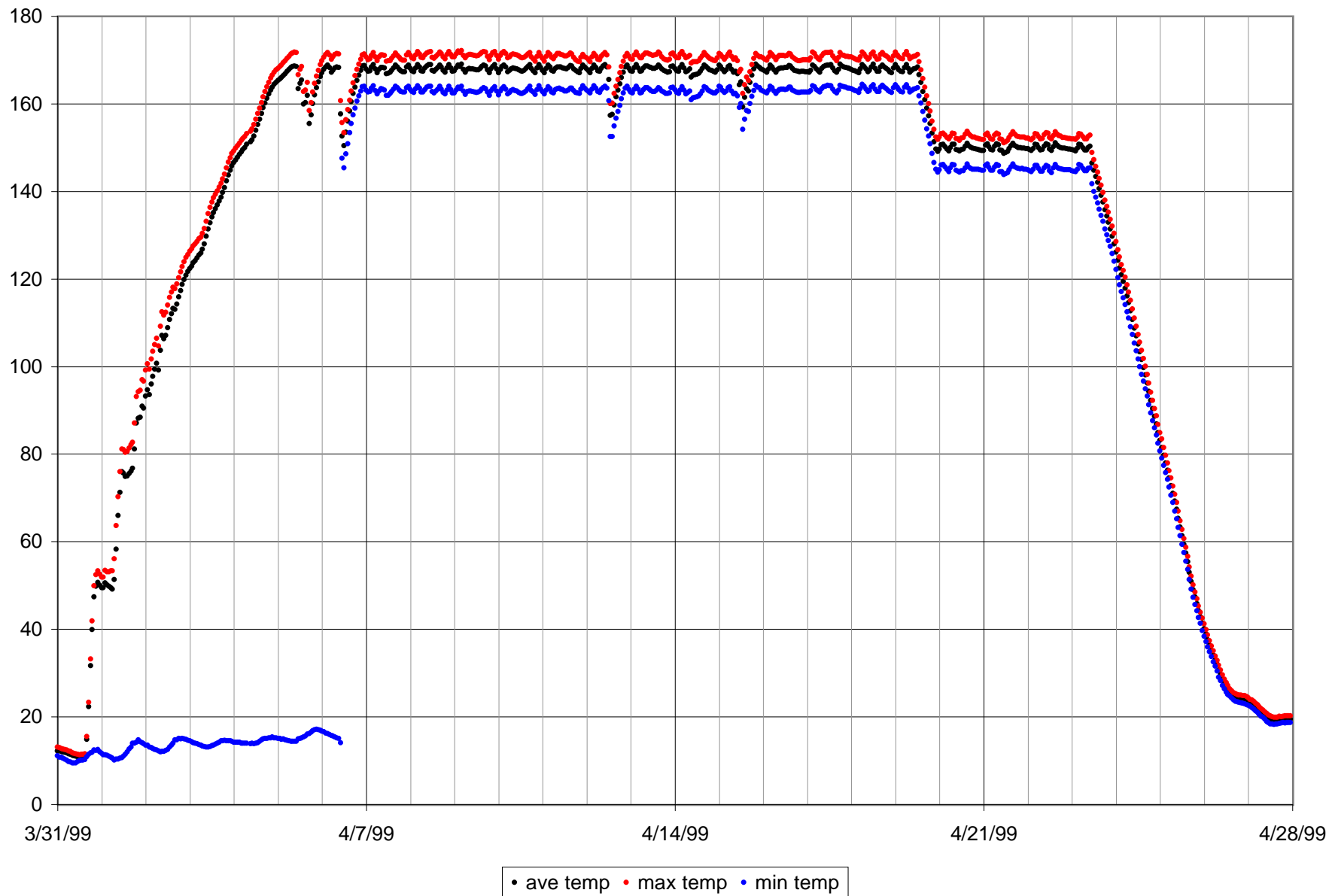
# BEAM TUBE BAKEOUT ELECTRICAL HEATING POWER



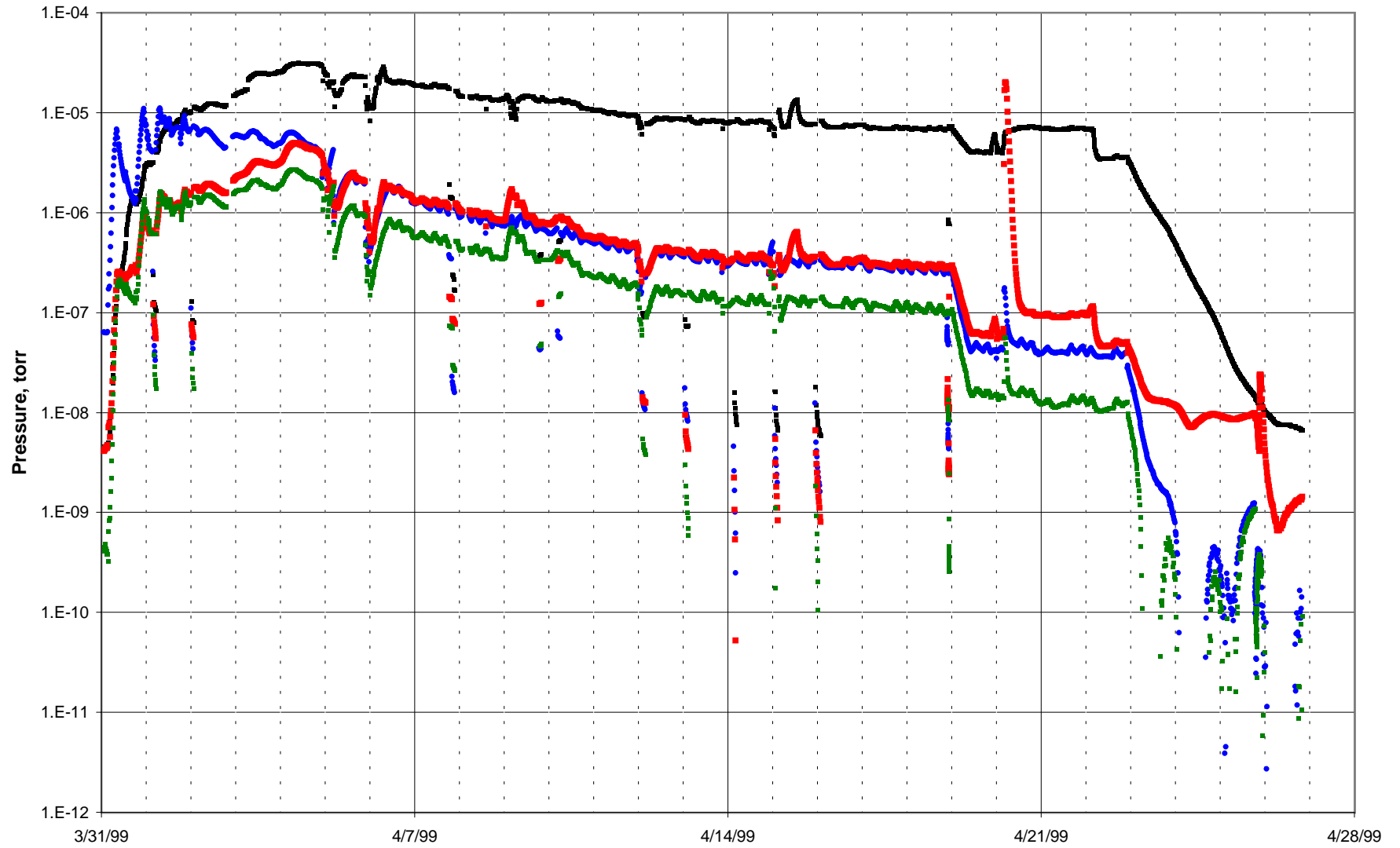
Legend: XFMR Power Transformer PS Low voltage, high current DC power supply







HX2 RGA PRESSURE, AMU 2 (blk), AMU 18 (blu), AMU 28 (red), AMU 44 (green)

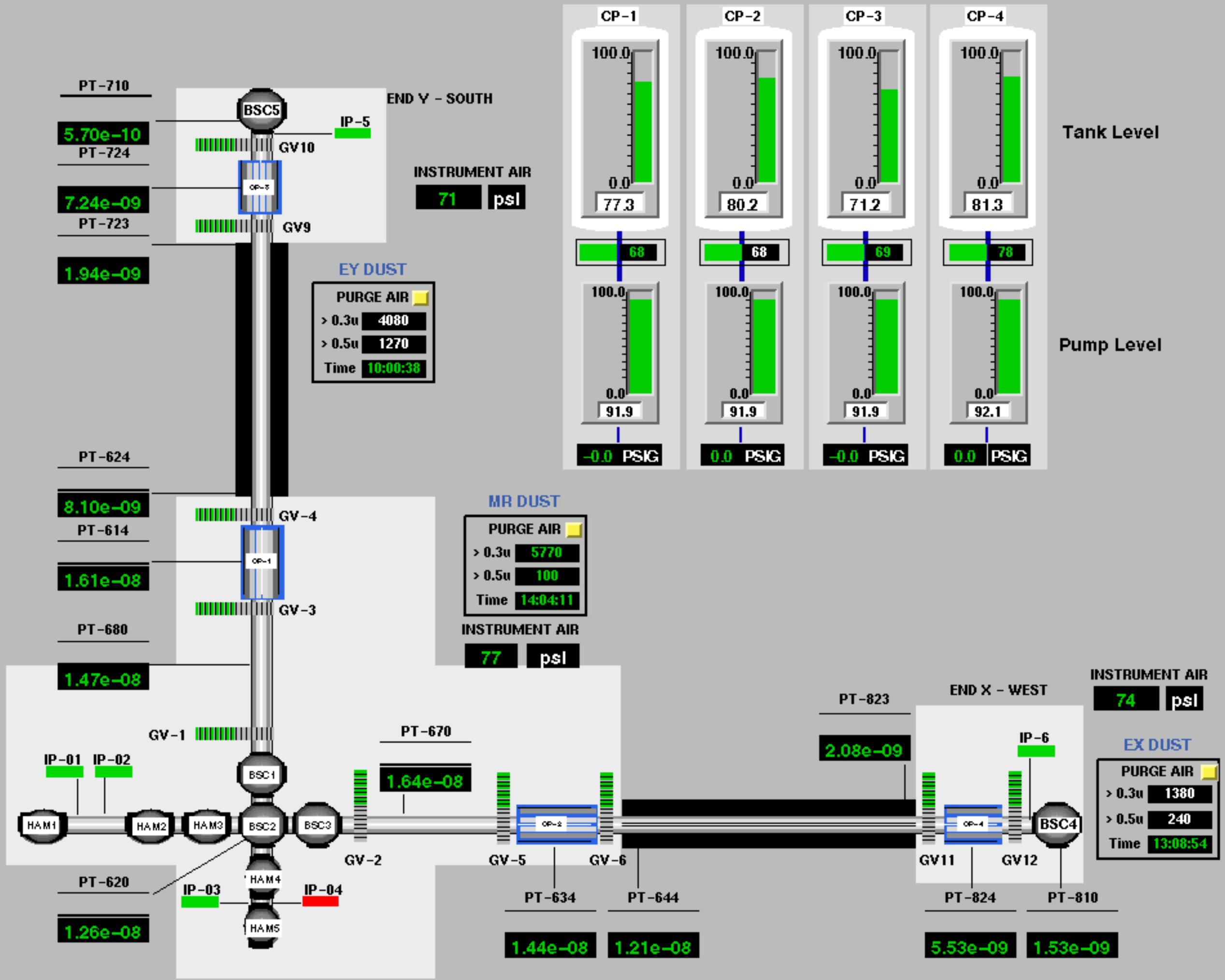


**2 km module post bake outgassing and leak rate**  
**Outgassing rate of selected gases in torr liters/sec/cm<sup>2</sup>@ 23 C**

molecule	Goal*	HY2	HY1	HX1	HX2	LY2	LY1	LX1	LX2	
<b>H<sub>2</sub></b>	4.7	4.8	6.3	5.2	4.6	2.6	3.4	6.6	4.3	x10 <sup>-14</sup>
<b>CH<sub>4</sub></b>	4800	< 90	< 22	< 0.9	< 10	< 24	< 3.9	< 3	< 4.0	x10 <sup>-19</sup>
<b>H<sub>2</sub>O</b>	1500	< 4	< 20	< 1.8	< 0.8	< 3	< 0.9	< 0.6	< 10	x10 <sup>-18</sup>
<b>CO</b>	650	< 14	< 9	< 5.7	< 2	< 5	< 10	< 8	< 5	x10 <sup>-18</sup>
<b>CO<sub>2</sub></b>	2200	< 40	< 18	< 2.9	< 8.5	< 10	< 6	1.1	< 8	x10 <sup>-19</sup>
<b>NO+C<sub>2</sub>H<sub>6</sub></b>	7000	< 2	< 14	< 6.6	< 1.0	< 1.9	< 3.6	< 1.1	< 1.1	x10 <sup>-19</sup>
<b>H<sub>n</sub>C<sub>p</sub>O<sub>q</sub></b>	50-2 #	< 15	< 8.5	< 5.3	< 0.4	< 20	< 25	< 1.9	< 4.3	x10 <sup>-19</sup>
<b>air leak</b> torr-liters/sec	10	< 2	< 1	< 0.4	< 1.6	< 10	23	< 3.5	< 0.7	x10 <sup>-10</sup>

\* Goal : maximum outgassing rate to achieve equivalent to 10<sup>-9</sup> torr H<sub>2</sub> with 2000 liter/sec pumps at only stations

# Goal for hydrocarbons depends on mass of parent molecule; range corresponds to 100 - 300 AMU



PT-710  
**5.70e-10**

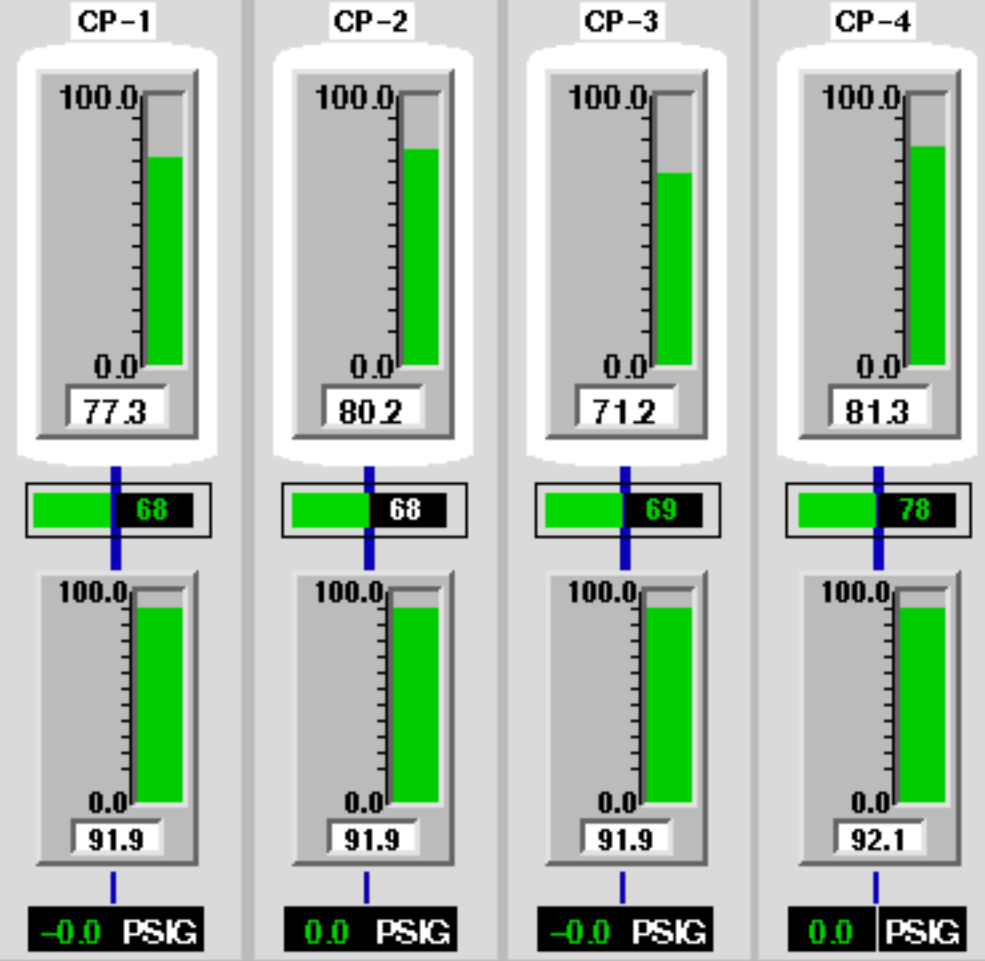
PT-724  
**7.24e-09**

PT-723  
**1.94e-09**

END Y - SOUTH

INSTRUMENT AIR  
**71** psl

EY DUST  
PURGE AIR   
> 0.3u **4080**  
> 0.5u **1270**  
Time **10:00:38**



Tank Level

Pump Level

PT-624  
**8.10e-09**

PT-614  
**1.61e-08**

PT-680  
**1.47e-08**

MR DUST  
PURGE AIR   
> 0.3u **5770**  
> 0.5u **100**  
Time **14:04:11**

INSTRUMENT AIR  
**77** psl

INSTRUMENT AIR  
**74** psl

EX DUST  
PURGE AIR   
> 0.3u **1380**  
> 0.5u **240**  
Time **13:08:54**

IP-01  
IP-02

PT-670  
**1.64e-08**

PT-823  
**2.08e-09**

END X - WEST

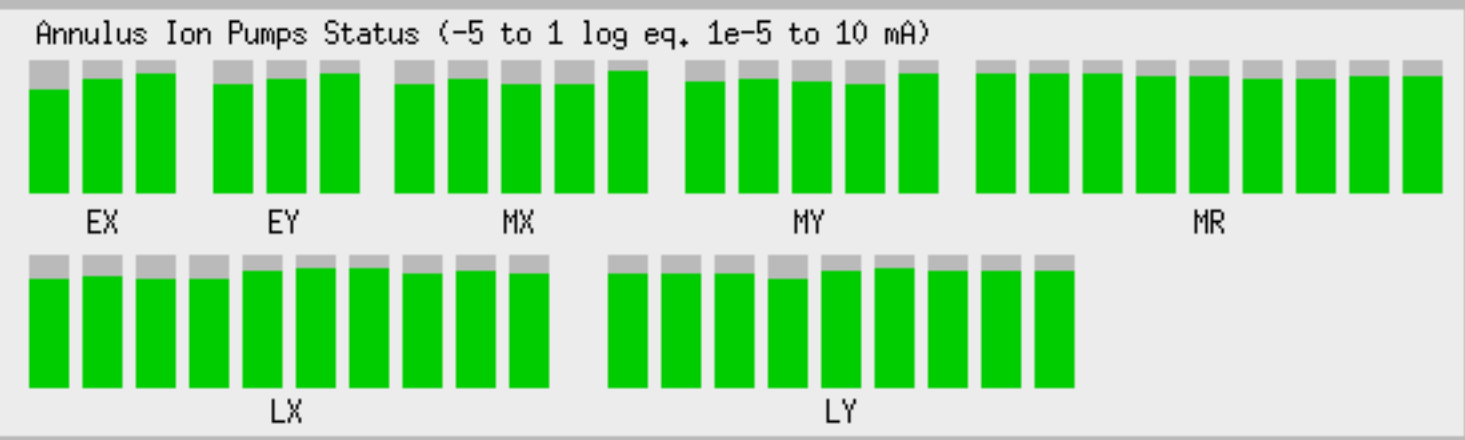
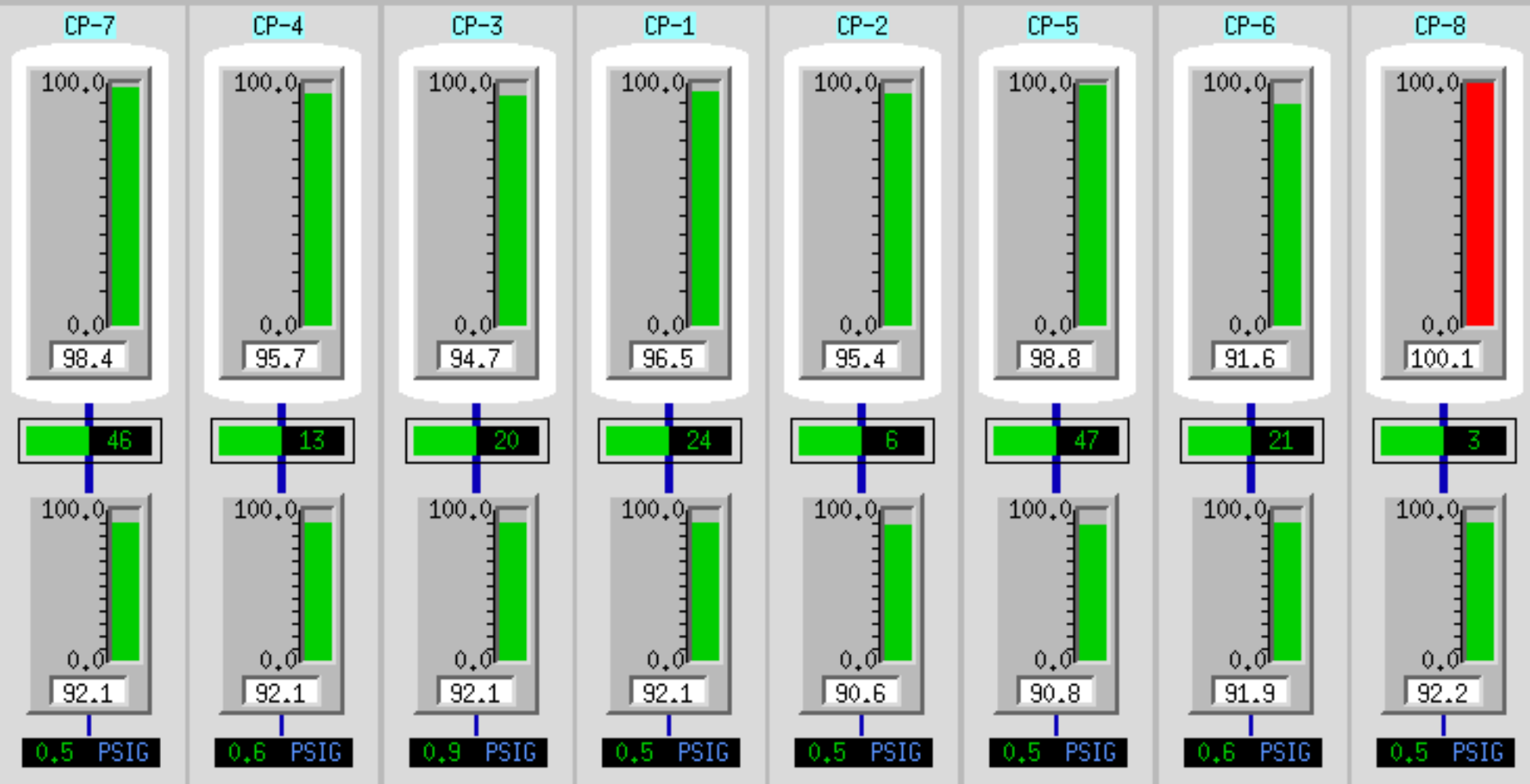
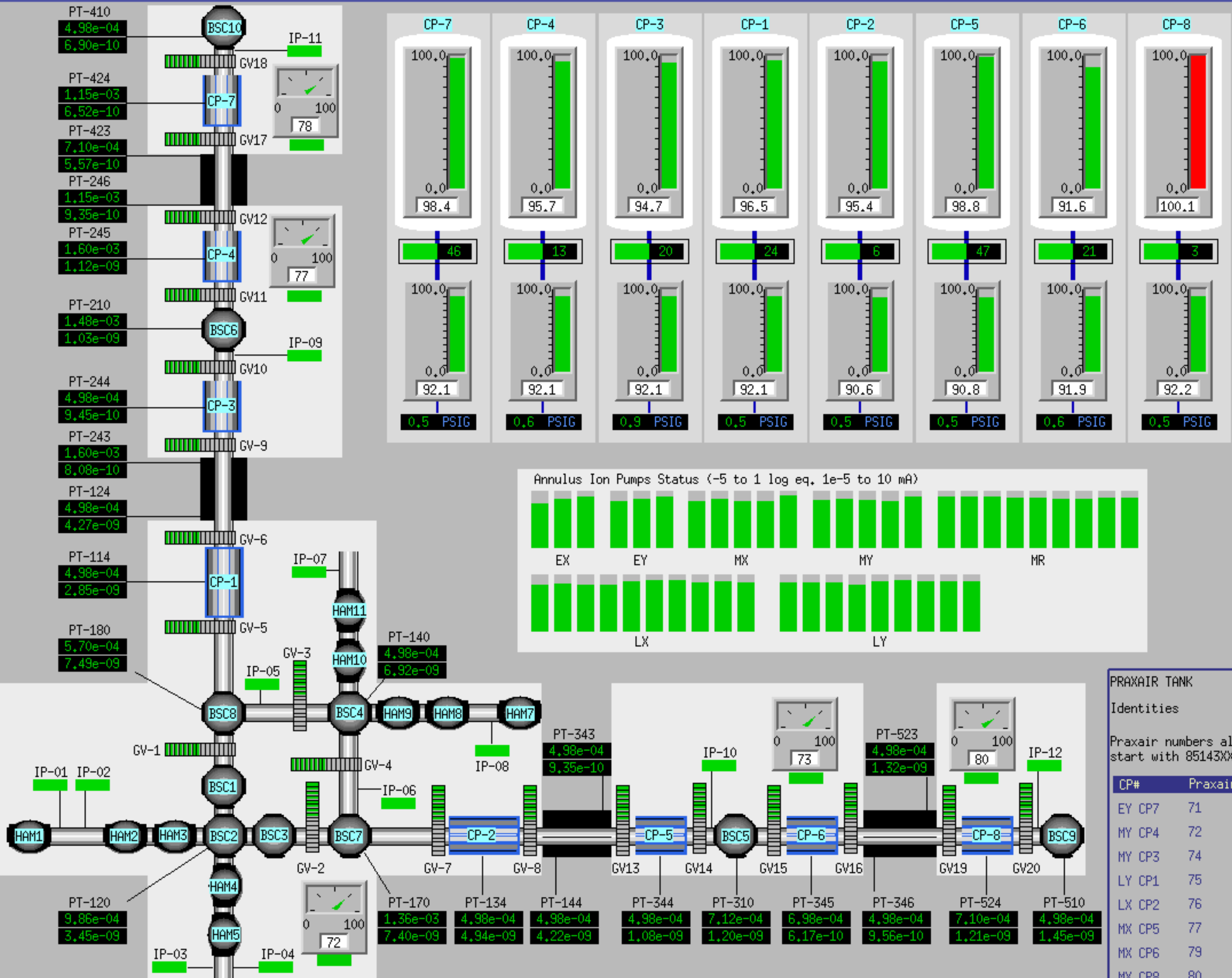
PT-620  
**1.26e-08**

PT-634  
**1.44e-08**

PT-644  
**1.21e-08**

PT-824  
**5.53e-09**

PT-810  
**1.53e-09**



PRAXAIR TANK

Identities

Praxair numbers all start with 85143XX

CP#	Praxair #
EY CP7	71
MY CP4	72
MY CP3	74
LY CP1	75
LX CP2	76
MX CP5	77
MX CP6	79
MX CP8	80