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NOV 1 1977

JOHN S. LAVALLE
Accounting Officer for Sponsored Accounting

CAMBRIDGE, MASSACHUSETTS 02139

MIT Reference #82958

National Science Foundation 1800 G Street, N.W. Washington, D.C. 20550

Attention: Mr. Joseph F. Carrabino Grants Manager, Area 1

Grants and Contracts Office

Gentlemen:

Massachusetts Institute of Technology submits herewith the Final Fiscal and Technical reports for the above referenced grant.

Please feel free to contact the undersigned if further information is required.

Thank you for your interest in and support of this Research Project.

Very truly yours,

John S. Lavalle

JSL/ms

cc: OSP Administrator Administrative Officer



NOV 1 1977

JOHN S. LAVALLE
Accounting Officer for Sponsored Accounting

CAMBRIDGE, MASSACHUSETTS 02139

MIT Reference #82958

Prof. Rainer Weiss Research Lab for Electronics MIT Room 20F-006

Dear Prof. Weiss:

The National Science Foundation has requested that we send them our Final Fiscal Reports when completed whether any of the Technical Reports have been forwarded to the Accounting Office or not. Current NSF Policy states that we should wait for the Summary of Completed Project (Form 98A) and the Final Technical Report (if the Principal Investigator elects) in order that they may all be submitted together. However, they have concluded that they would rather have only the Fiscal Report than none at all.

To our knowledge, there has not been a copy of the Final Technical Report or a Summary of Completed Project (Form 98A) submitted to the NSF Office of Grants and Contracts on the above referenced grant. The Foundation Policy requires that all Fiscal and Technical Reports be submitted within 90 days after expiration.

This is to advise you that the Final Fiscal Report has been submitted this date and request that the Technical Documents be submitted at your earliest convenience, a copy of your transmittal letter being sent to the Accounting Officer for Grants (Building E19-579).

Your reports should be submitted to:

National Science Foundation 1800 G Street, N.W. Washington, D.C. 20550

ATTN: Mr. Al Rice

Very truly yours,

John S. Lavalle

JSL/ms

cc: OSP Administrator
Administrative Officer

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139

September 19, 1977

MEMORANDUM

To:

J. Hanlon

From:

D.F. Duffy

Subject:

OSP 82958 - NSF Closeout of Account

Aug. 1977 Statement Balance

\$2,114.07

less RL 58312 - Invoice sent to Accounting Office for payment

on 9-15-77

1,620,00

Balance returned to NSF

\$ 494.07

No outstanding purchase orders remain against this account.

Faculty amount was proposed at 12% for 9 months and that was the actual charge to this grant. The overrun was due to a salary increase. This discrepency is allowed by NSF.

cc: R. Weiss

P. Wolff

M. Huguenin .



JOHN P. LEONARD

MR DONALD DUFFY

AUG 0 8 1977

ADMINISTRATIVE OFFICER

R.L. E.

M.I.T. Roum # 36-491

DEDR MR. DUFFY,

Attached is a notice of closeout action required under one of your recently terminated accounts. Due to contract/grant closeout requirements imposed by various sponsors, it is necessary that you advise us as to the actions you will take within the next thirty days, in order that we may submit the required report or invoice on a timely basis.

If your actions involve the transfer of specific charges, please indicate that detail when returning the Action Notice. If we can be of any assistance or if you need any additional detail, please do not hesitate to call the auditor who prepared the notice.

Your assistance in helping us to meet our contract/grant reporting requirements will be greatly appreciated.

Sincerely yours,

John P. Leonard

JPL/da

cc: John S. Lavalle
Roberta F. Burns/Robert J. Long
O.S.P. Administrator
C.A.O. File

Notice of Closeout Action Required

	Date:	AUG u	0 13// AUC	0819/
Consor: N.S.F.		Number:		. •
Department: R. L. E.	Administ	rator: V	N HYWES	
Supervisor: R WEISS			6-1-75	
Audited By: Jim HANZONROOM # E19-545			5-31-77	
	<u>. </u>			
				• •
An audit of the referenced account as of 6-3 follows. Please indicate the action you have to auditor by SEP 0.8 1977.	0-77 aken and ret	indicates urn this r	s that the sta notice to the	itus is as above
	Amount Requiring Action	Transfer Sent To	Account Transferred To	Amount of Transfer
Overexpended Balance - Direct Cost Indirect Cost				<i>,</i>
Unexpended Balance - Direct Cost Indirect Cost	7,165.77			
Ludget Deviation: Category Budget Actual FACULTY \$2,830.00 \$3,053.99	223.99			
Post-termination Date Charges (Detail Attached)	2.40			
Pre-effective Date Charges (Detail Attached)				
Purchase Order Commitments (Copies Attached)	6,580.00			
Other Items Outstanding (Detail Attached)				
Comments: ADJUSTMENTS IN PROCESS 8/17		0. (2.63))	a a fallen (fig. agraes a film) e e agraesta a figi
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		14.73	CREDIT	

cc: John S. Lavalle
Roberta F. Burns/Robert J. Long
O.S.P. Administrator
C.A.O. File

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TRIPLICATE to Massachusetts Institute of Technology Box 69 Cambridge, Massachusetts R. JISITION NUMBER

ITEM QUANTITY

Massachusetts Institute of Technology

Cambridge, Massachusetts

DATE March 18, 1977

OKCHASE OKUEK

PURCHASE ORDER NUMBER

This Number Must Appear on Invoices, B/L's, Shipping Memos and All Packages.

ACCOUNT NUMBER

82958

Schweber Electronics 213 Third Avenue Waltham, MA 02154

Peter Kramer SHIP TO reter kramer Research Lab of Electronics Room No. 20F-001 MASSACHUSETTS INSTITUTE OF TECHNOLOGY, Cambridge, Mass.

Deliver Material to Building 20 Receiving Room

PLEASE FURNISH THE FOLLOWING MATERIALS OR SERVICES: F. O. R. TERMS

SHIP VIA

-I Week

Your Del.

Our Lab.

DESCRIPTION

27 - 10Days

Confirmation

5047-5 Harris Electronics

\$8.70/ea.

\$34.80

PRICE

Transported to 26880 on 7-29-77

This order is exempt from Massachusetts Sales & Use Tax. Exemption Number E 042 103 594 M.I.T. is an equal opportunity employer and has an Affirmative Action Plan

TOTAL PRICE

\$34.80

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PAID NVOICE DATE DATE PROCESSED UNEXPENDED BALANCE AMOUNT

MAR 29 1911

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

AGENT

ACCOUNTING OFFICE COPY

Please Send Invoices In PURCHASE ORDER PURCHASE ORDER NUMBER TRIPLICATE Massachusetts Institute of Technology to Massachusetts Institute **58**296 Technology Box 69 Cambridge, Massachusetts Cambridge, Massachusetts This Number Must Appear on to-02139 B/L's, Shipping Memos and All Parc ACCOUNT NUMBER REQUISITION NUMBER May 26, 1977 82958 Peter Kramer SHIP TO reter kramer Research Lab of Electronics Interactive Radiation, Inc. 181 Legrand Avenue Room No. 20F-001 Northvale, New Jersey 07647 MASSACHUSETTS INSTITUTE OF TECHNOLOGY, Cambridge, Mass. Deliver Material to Building 20 Receiving Room PLEASE FURNISH THE FOLLOWING MATERIALS OR SERVICES: DATE REQUIRED SHIP VIA Best Way Pregaid-F. O. B. TERMS May 31, 1977 Add to Invoice Northvale, N. J. Net ITEM QUANTITY DESCRIPTION PRICE Confirmation Low Voltage Modulator 151-030 \$1,960.00/ea. \$1,960.00 Video Amplifier 1-050 2.850.00/ea. 2,850.00 Calcite Polarizer, Mounted 701-050 115.00/ea. 115.00 Pard in Aug RECEIVED F. H Mograry This order is exempt from Massachusetts Sales & Use Tax. Exemption Number E 042 103 594 M.I.T. is an equal opportunity employer and has an Affirmative Action Plan TOTAL PRICE \$4,925.00 PAID ICE DATE DATE PROCESSED UNEXPENDED BALANCE AMOUNT 1977 JUN 7 MASSACHUSETTS INSTITUTE OF TECHNOLOGY

ACCOUNTING OFFICE COPY

Please Send Invoices In. PURCHASE ORDER TRIPLICATE PURCHASE ORDER NUMBER Massachusetts Institute of Technology to Massachusetts Institute of Technology 58312 Box 69 Cambridge, Massachusetts Cambridge, Massachusetts This Number Must Appear on Involves, 02139 B/L's, Shipping Memos and All Packages, REQUISITION NUMBER ACCOUNT NUMBER DATE May 27, 1977 82958 SHIP TO Peter Kramer Research Lab of Electronics Valpey 1244 Highland Street TO Room No. 20F-001 P. O. Box 145 MASSACHUSETTS INSTITUTE OF TECHNOLOGY, Holliston, MA 01746 Cambridge, Mass. Attn: David Barnicle Deliver Material to Building 20 Receiving Room PLEASE FURNISH THE FOLLOWING MATERIALS OR SERVICES: DATE REQUIRED SHIP VIA Best Way Prepaid o.s. 5/31/77 TERMS Add to Invoice Holliston, MA ITEM QUANTITY Net DESCRIPTION PRICE Confirmation Mirrors \$1,620.00 1" thick 4" diameter Radius Rl 1 meter Plano Fine Ground R2 Reflectivity 5145 % 99% or greater 6328 A 95% or greater Hole 1.5 mm. in diam. at Radius of 1.500" + .010" Pard in 1 This order is exempt from Massachusetts Sales & Use Tax. Exemption Number E 042 103 594 M.I.T. is an equal opportunity employer and has an Affirmative Action Plan TOTAL PRICE \$1 620.00 CE DATE DATE PROCESSED UNEXPENDED BALANCE AMOUNT JUN 2 1977 MASSACHUSETIS INSTITUTE OF TECHNOLOGY Address all Correspondence AGENT ACCOUNTING OFFICE COPY

incipal Investigator R. Wryss

OSP 82958

6/1/75 thru 5/3/177

Status as of <u>5//9/72</u>

	Proposed	Revisions	Spent & Committed	Balance
Salaries and Wages	\$17,270	\$	5.14.963.	\$2,30 7 .
Fringe Benefits	.1,666	• • • • • • •	. 3,287.	(1621)
Overhead	10,707	• • • • • • • •	.10,9.33.	(226)
Materials and Services	.1.4.53.7.	•••••	11,500	3037
Computer Time	• • • • • •	• • • • • • •	• • • • • • •	• • • • • • •
Equipment	8,320	• • • • • • •	8,377	(57)
Travel	500			500
Total Costs	\$53,000	\$	\$ 49,060	\$ 3,940

Principal Investigator R Wees OSP <u>82958</u> 11/30/76 Sponsor ___NSF 6/1/75 thru 5/31/76 Status as of 7/21/76 Spent & Proposed Revisions Committed Balance Salaries and Wages \$.47.270 \$10, 34.8. \$6,9.27 Fringe Benefits ..2, 15.7. (...491.) Materials and Services 14,537 .4.05.0. 10,48.7 Computer Time

Direct Costs

Equipment

Travel

Indirect Costs 62%

Total Costs

\$ 42,293

\$ 10,707 \$ 53,000 21,926 20,367

. 5,376.

7022 3,685

.2.944

28,948 24,052

OSP 82958

NSF Sponsor

Prin. Inv. R. Weiss

Nov 30

June 1, 1975 - May 31, 1976

Salaries & Wages	Proposed Revisions	Spent & Committed Balance
R. Weiss Prof 12%- 9 Kramer B. Res Stabl	2,830	7.054. (. 224.)
D.K. Owens Res Asst 100%-12	8,640	8.6.90
R. Benford Tech Asst 25%- /2		4.850 (4.850)
RLE Shop c Smith lee	thru 1/1977	6 .1,047. (.1.047.)
Alloc. Proj. Level Costs	2,800	1930 1370
Total S&W	<u> 17,270</u>	10,848 6,927

FORM NO. CO-001 9/70

RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139

June 7, 1977

MEMORANDUM

To:

R. Weiss

From:

D.F. Duffy

Subject:

OSP 82958, NSF Grant MPS75-04033, "Interferometric Broad Band Gravitational Antenna"

This program terminated on May 31, 1977. According to N.S.F. policy a final technical report must be submitted within 90 days after the grant expiration date.

MASSACHUSETTS INSTITUTE OF TECHNOLOGY CAMBRIDGE MASS 02139

COMPTROLLER'S OFFICE

October 1, 1976

To: Project Supervisors of NSF Grants

From: Philip J. Keohan

The Institute has received Important Notice No. 62 from the National Science Foundation concerning the submission of final fiscal and technical reports.

In summary, the major requirements of this notice are as follows:

- 1.) Final technical and final fiscal reports must be submitted within 90 days after the grant expiration date.
- 2.) Final technical and final fiscal reports must be submitted together effective October 1, 1976.
- 3.) A Summary of Completed Project (NSF Form 98A) must also be submitted together with the technical and fiscal reports as noted above.

In order for us to comply with this NSF requirement and forward all reports as a single package, please forward your technical reports and completed project summaries to:

Mr. John S. Lavalle Room E19-579

Your cooperation in implementing these new requirements will be most appreciated.

PJK/da

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MASSACHUSETTS INSTITUTE OF TECHNOLOGY

RESEARCH LABORATORY OF ELECTRONICS

CAMBRIDGE 39, MASS.

February 11, 1977

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MEMORANDUM

To:

Prof. R. Weiss

From:

D.F. Duffy

AFD

Subject:

OSP 82958 N.S.F. Grant MPS75-04033

In your letter to N.S.F. of November 18, 1976 you stated that thought would be given to preparing a proposal for continuation of this work. As you know, N.S.F. usually likes about 6 months advance time on new proposals, and 4 months time on renewals for evaluation. Therefore, as your current grant expires 5/31/77 this would be an appropriate time to begin its preparation if you plan to submit.

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS

CAMBRIDGE, MASS. 02139

November 18, 1976

632-4302

Dr. Richard Isaacson National Science Foundation Washington, D.C. 20550

Dear Dr. Isaacson:

I am writing in regard to the N.S.F. Grant MPS75-04033 entitled "Interferometric Broad Band Gravitational Antenna". As you know this grant has been given a no-cost extension from June 1976 to the end of November 1976. At present there are about \$25K remaining in the grant which are not committed. How this has happend I will describe below. I am asking to have the grant extended for another 6 months and in addition during these 6 months will submit a grant renewal request.

In order that you might understand all of this, I have to tell you some of the history of this project. The idea that one could use free masses sensed interferometrically as a large baseline gravitational wave antenna has been evolving in my mind since 1971. At that time I had several undergraduates working on aspects of such a system, in particular senior theses were carried out on laser noise measurements and suspension design and testing. By 1972 a very good graduate student, Kingston Owens now at the Princeton Plasma Laboratory, began construction of a small interferometric antenna which was to become his Ph.D. thesis. The work at that time was supported by the military under the Joint Services Electronics Program. By the end of 1972, the military had lost interest in gravitational research and I applied to the N.S.F. for research support. The proposal to the N.S.F. was unfavorably reviewed at the time most likely because it was too big a step from acoustic gravitational wave detectors which still looked promising especially as the Weber experiments had not been convincingly confirmed or refuted. I made a request from the Sloan fund at M.I.T. which was granted. This money, about \$20K, was used to buy equipment but could not be applied to salaries. Kingston and I continued to work on the antenna through 1973 and evolved a second proposal to the N.S.F. which was approved in June 1975.

Before this time however Kingston's support had run out and I put him onto another project. In September of 1975 a new graduate student, supported by other funds, began working on the project; frankly he did not work out and left in January 1976. In the course of this year I have made numerous attempts at interesting other students in the experiment with little success. Gravitation research, although viewed as fascinating, is considered too hard, and unfortunately profitless not only by the average student but also by much of the physics faculty. In short, the atmosphere if not outright hostile to such research is certainly sceptical. Even I was becoming more timid and in fact was seriously considering returning the unspent funds in the N.S.F. grant and getting out of the gravitational radiation research business entirely.

Several factors have increased both my interest and optimism. First, in the course of running a N.A.S.A. sponsored study on the uses of space in experimental relativity, it dawned on both Peter Bender and me that interferometric systems using the large baselines in space afforded a real chance to look for gravitational radiation from slow objects such as stellar binaries. Although these measurements appear impossible from the ground; in space the dominant noise may well be the cosmic proton flux and a 1 kilometer baseline system, using laser interferometers loosely coupled to a frame, could measure the radiation from several binary systems with integration times of the order of a few months. Bender and I will study this further, hopefully with a small grant from N.A.S.A. The important thing is that aside from just setting better upper limits on the gravitational radiation flux, there is now an actual, albeit remote, goal to continue development of interferometric antennas. The second point is that I have found a good physicist, Peter Kramer now a post doc at Arizona, interested in working with me at M.I.T. on the prototype antenna. He would like to start working on the antenna as soon as possible. Finally, I hear from various colleagues that the transducer problem in the cryogenic high Q bar antennas is formidable and this is driving several groups toward interferometric sensing systems. In particular, Ron Drever has come to the same conclusion as I that interferometric large baseline systems are the most promising direction forthe future.

In short, this letter is intended to tell you that damn little actual progress on the prototype antenna has been made in the past year aside from some minor work on fast electronics for the fringe detection system. I know that on the basis of the experimental progress alone a renewal request at this time would not survive a review procedure. On the other hand some real progress in the theoretical developments has been made and that now with the active interest of another capable physicist, progress in the experimental work on the protytype antenna can be expected.

I would like the N.S.F. to continue the no-cost extension for another 6 months. Kramer can begin in February of 1977. About \$11K of the remaining funds would be used to support him; the rest, amounting to \$14K, used for materials and services, especially technician time and shop costs. During this period Kramer and I would formulate a renewal proposal to the N.S.F.

Sincerely yours,

Rainer Weiss

Professor

Department of Physics

cc: J. Carrabino/NSF

Endorsements

John J. Hynes/

Operations Coordinator

Office of Sponsored Programs

Date

Peter A. Wolf

Director

Research, Laboratory of Electronics

Date: Nov. 18, 1976

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE 39, MASS.

November 16, 1976

MEMORANDUM

To:

R. Weiss

From:

B. McCarthy

Subject:

OSP 82958 - N.S.F. Grant MPS75-04033

The above referenced grant will terminate on November 30, 1976. In order to take advantage of continuing this grant and spending the balance of funds remaining we must submit a written request to N.S.F. prior to that date. If the request is not made this account will be closed out and a final report of expenditures prepared by M.I.T.

If we can help in any way please let me know.

cc: J. Hynes

BORATORY OF ELECTRONICS CAMBRIDGE, MASS: 02139 July 7, 1976 Mr. Gaylord L. Ellis Grants Office National Science Foundation Washington, D.C. 20550 Reference: Grant MPS 75/04033 Dear Mr. Ellis: We request your permission to exceed the authorized faculty salary total by \$1,298. This increase is brought about mainly by charging 12% of my time during part of the flexibility period September 1, 1976 through November 30, 1976 and also because the actual charge during the original grant period exceeded the proposed by a small amount, \$300 due to a salary increase. Sincerely yours, Rainer Weiss Principal Investigator Endorsements John J. Hynes Reter A. Wolff Operations Coordinator Director Office of Sponsored Programs Research Laboratory of Electronics Date: Date:

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139

July 20, 1976

1 2/30/16 NS

MEMORANDUM

To:

Prof. R. Weiss

From:

Paul L. Smith

Subject:

Renewal Proposal OSP 82958

Your present NSF Grant MPS75-04033
terminates on November 30, 1976 . Most of the
government agencies like at least 6 months lead time to
consider new proposals. If you need a copy of the last
proposal, please let me know.

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MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139

June 2, 1976

MEMORANDUM

To:

J. Kosut

From:

H. J. Zimmermann

Subject:

OSP 82958

Please extend the expiration date on the above account from 5/31/76 to 11/30/76.

PLS/jg

cc: R. Weiss

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139 OFFICE OF SPOUSERED PROGRAMS OSP 82958 1107 - 0 1976 March 2 1976 Mr. Gaylord L. Ellis Grants Officer National Science Foundation Washington, D.C. 20550 Reference: Grant MPS 75ppdc39 Director for Atomic. Molecular and Plasma Privatory Dear Mr. Ellis: This note is a request to change some permanent equipment I would like to buy for the project "Interferometric Broad Band Gravitational Antenna" supported by N.S.F. In the original proposal for two years we were going to buy an instrumentation tape recorder in the first year for \$8,000 and a disk at \$5,000 for the PDP 11 computer in the second year.

We have been able to borrow an Ampex FR 1300 tape recorder for about one year and find need for the disk in both the design calculations and the data analysis. I request that we buy the disk now and use the difference in cost of recorder and disk, amounting to \$3,000, to purchase a high voltage broad band amplifier to drive the electro-optic modulators in the interferometer (specific vendor has not yet been determined).

Copy sent 3/16/76 to:

Dr. Weiss

Dr. Zimmermann

Ms. Kosut

NSF Grants Office

(PHY75-04033)

Sincerely yours,

Rainer Weiss Principal Investigator

Endorsements

Assistant to the Director Office of Sponsored Programs

Date: 3-3-76

lillic cive Henry J.

Director / (

Research Laboratory of Electron

Date: 2476

N. S. Zirnmeamann 3/22/16

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

RESEARCH LABORATORY OF ELECTRONICS

CAMBRIDGE, MASS. 02139

February 12, 1976

OSP 82958

Grant MPS75-04033

Professor Henry J. Zimmermann Room 36-419

Dear Henry:

This note is a request to change some permanent equipment I would like to buy for the project "Interferometric Broad Band Gravitational Antenna" supported by the NSF. In the original proposal for two years we were going to buy an instrumentation tape recorder in the first year for \$8000 and a disk at \$5500 for the DDP 11 computer in the second year.

We have been able to borrow an Ampex FR 1300 tape recorder for about one year and find need for the disk in both the design calculations and the data analysis. I request that we buy the disk now and use the difference in cost of recorder and disk, amounting to \$2500, to purchase a high voltage broad band amplifier to drive the electro-optic modulators in the interferometer.

Sincerely yours,

Rainer Weiss

RW:CFS

Date:

No final decision has been made as to the Vendor on the broad-band equipment.

Endorsements

Henry J. Zimmermann
Director
Research Laboratory of Electronics
Date: Jen 18,1976

Assistant to the Director
Office of Sponsored Programs

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NATIONAL SCIENCE FOUNDATION

WASHINGTON 1 1975 20550

Dr. Rainer Weiss Department of Physics Massachusetts Institute of Technology Cambridge, Massachusetts 02139

Dear Dr. Weiss:

I am pleased to learn that the Foundation has issued the official letter awarding Massachusetts Institute of Technology an NSF grant to support your research entitled "Interferometric Broad Band Gravitational Antenna," for a duration of 12 months. I enclose a copy of the official award letter.

The enclosed booklet, "Grants for Scientific Research," may be useful. In particular, I think that you will find the reporting requirements, as set forth therein, modest and not inconvenient. We greatly appreciate receiving brief notes descriptive of any particular striking or significant advances made by you. Such statements are of real value to us in our efforts to enhance the support the NSF can offer the scientific community. To the same end, it is important that appropriate acknowledgement of Foundation support be made in publications.

We are genuinely interested in following the progress of your work. Please do not hesitate to call upon us if we can be of assistance in any matter connected with this grant. My associates at the National Science Foundation join me in wishing you a successful period of research under your grant.

> Sincerely yours, Stuar L. Meyer

Stuart L. Meyer

Program Director for Intermediate

Energy Physics

Physics Section

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NATIONAL SCIENCE FOUNDATION WASHINGTON, D. C. 20550

MAY 2 1 1975

Dr. Jerome B. Wiesner, President Massachusetts Institute of Technology Cambridge, Massachusetts 02139

Proposal/Grant No. MPS75-04033

Dear Dr. Wiesner:

It is a pleasure to inform you that \$53,000 is granted to Massachusetts Institute of Technology for support of the project entitled "Interferometric Broad Band Gravitational Antenna" as outlined in the above-numbered proposal. This project is under the direction of Rainer Weiss, Department of Physics.

The funds provided by this grant are intended to assist in the support of the project at the agreed level of effort for approximately twelve months. The NSF share of such support is summarized in the attached budget. The grant is effective June 1, 1975 and, unless otherwise amended, will expire on November 30, 1976. The grant period includes the flexibility period described in Section 120 of NSF 73-26, "NSF Grant Administration Manual."

The provisions of FL 25, "Administration of MSF Project Award," stacked, are applicable to this grant.

Appropriate provisions of MSF 73-12, "Grants for Scientific Research," are applicable to the scientific or technical direction of the project and the preparation of technical reports.

Sincerely yours,

Grants Officer

Attachments

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a. Research Associates—Postdoctoral b. Non-Faculty Professionals			· . · · · · · · · · · · · · · · · · · ·	
2. Other Personnel (Non-Faculty)				
Sub-Total		. \$	2,830	\$
b. Faculty Associates				
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MUSELTS Inst. of Tech.	NSF PROGRAM	I	from 6/1/75	

PROJECT SUMMARY

MS75-04033

	DIRECTORY NAME)	ADDRESS OF IN	STITUTION (INCLUDE BRANCH/CAMPUS & COMPONENT)
chusetts	Institute of Technology	i	Massachusetts 02139
INVESTIGATOR	SOCIAL SECURITY NO.		
	Jaconiii No.	DIVISION (OFFIC	E) AND DIRECTORATE
piner Weiss	128-26-6401	Settlematics	al and Physical Sciences, AD/R
SAL NUMBER		Physics	
e UPS 			
		intermediat	e Energy Physics

"Interferometric Broad Band Gravitational Antenna"

SUMMARY OF PROPOSED WORK (LIMIT TO 22 PICA OR 18 ELITE TYPEWRITTEN LINES)

This proposal is for an NSF grant to continue the development of a broadband gravitational radiation antenna that used free masses as antenna elements. The masses are the mirror mounts of a laser illuminated Michelson interferometer which is used to massure the gravitationally induced strains in space. Although the proposed scheme is in some regards technically more difficult than resonant bar antennas, it holds the promise of extending bhe search for gravitational radiation to a sensitivity much that one may expect to detect the radiation from various astronomical sources. The first step is a small prototype interferometric antenna with 9 meter arms. This prototype is at least 1000 times more sensitive to a large class of astronomical sources of gravitational radiation than existing resonant bar imagined sources still indicate that the prototype antenna will only be able to set techniques developed can be smed in interferometric antennas with baselines of the order of a kilometer or more, since the sensitivity of this type of antenna increases with the mourae of the baseline.

DURATION GRANTED	AMOUNT GRANTED
one year	*********
	\$53,000

A copy of this summary has been sent to the Science Information Exchange at the Smithsonian Institution for reference and public records.



MASSACHUSETTS INSTITUTE OF TECHNOLOGY

77 MASSACHUSETTS AVENUE ROOM E19-702 CAMBRIDGE, MASS. 02139

OFFICE OF SPONSORED PROGRAMS

September 11, 1974

TELEPHONE (617) 253.

3907

National Science Foundation 1800 G Street, N.W. Washington, D.C. 20850

Attention: Dr. Richard Isaacson

Theoretical Physics Program

Division of Physics

Reference: Research Proposal

Gentlemen:

Massachusetts Institute of Technology submits herewith twenty (20) copies of a proposal for the research entitled "Interferometric Broad Band Gravitational Antenna" to be under the direction of Professor R. Weiss of M.I.T. Research Laboratory of Electronics.

This proposal is submitted at a total estimated cost of \$97,500 for a two year period January 1, 1975 through December 31, 1976. Included in this amount is an estimated cost of \$53,00 for the first year.

One copy has been signed by Professor Rainer Weiss; Henry J. Zimmermann, Director and George Dummer, Administrative

Very truly yours,

Jane Kosut Assistant to the Director

JK/JS BNC: 20

CC: R. Weiss

H.J. Ximmermann

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

RESEARCH PROPOSAL SUMMARY — Submission Data, Resource Use, and Approvals

Title of Proposal				Sub-Unit		Dept. No.
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Present DSR No.			· 		onsor expecting to	<u></u>
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Total Dollar Amount this I	Proposal	p (490)	First year amoun	nt <u>\$ 53,00</u>	30	
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Research Proposal Submitted to the National Science Foundation

Proposed Amount: \$ 97,500 Proposed Effective Date: January 1, 1975

Proposed Duration: 24 Months

Title:

"Interferometric Broad Band Gravitational Antenna"

Principal Investigator: Rainer Weiss

Social Security No.:

128-26-6401

Room Number:

20F-006

Make Grant to: Massachusetts Institute of Technology

submitted by

Massachusetts Institute of Technology Research Laboratory of Electronics 77 Massachusetts Avenue Cambridge, Massachusetts 02139

4	Endorsements	
Principal	Investigator	Laboratory Official
Name: $\frac{Ra}{0}$	Lang Wun	Henry J. Zimmermann
Title: Pr	rofessor	Director)
Dept.: Ph	ysics	Research Laboratory of Electronics
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Date:	5, 1977	Sept 5, 1974
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	Name: George H.	Dummer
	Signature:	

name:	George II. Dumier
Signature:	
Title:	Administrative Director
Dept:	Office of Sponsored Programs
Tel. No.:	(617) 253-2492
Date:	

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Appendix I. Thesis - Astrophysical Sources of Gravitational Radiation	Attached
Appendix II. Thesis - Spherical Mirror Delay Lines	Attached

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS, 02139

August 8, 1974

Proposal to National Science Foundation

"Interferometric Broad Band Gravitational Antenna"

Abstract

This proposal is for an NSF grant to continue the development of a broadband gravitational radiation antenna that uses free masses as antenna elements. The masses are the mirror mounts of a laser illuminated Michelson interferometer which is used to measure the gravitationally induced strains in Although the proposed scheme is in some regards technically more difficult than resonant bar antennas, it holds the promise of extending the search for gravitational radiation to a sensitivity such that one may expect to detect the radiation from various astronomical sources. The first step is a small prototype interferometric antenna with 9 meter arms. prototype is at least 1000 times more sensitive to a large class of astronomical sources of gravitational radiation than existing resonant bar antennas; however, any reasonable estimates of the source strengths of known and imagined sources still indicate that the prototype antenna will only be able to set upper limits on the gravitational radiation intensity. It is hoped that the techniques developed can be used in interferometric antennas with baselines of the order of a kilometer or more, since the sensitivity of this type of antenna increases with the square of the baseline.

Preliminary work has been going on at M.I.T. for several years with the support of the Joint Services Electronics Program and the M.I.T. Sloan Fund. The JSEP has terminated support for the project as of June 1974 as it cannot justify the relevance of gravitational research to its own program. The proposal to the NSF is for operations costs for two years, the installation of the antenna at an off campus site and for data acquisition equipment.

Introduction

It is probably safe to say that gravitational radiation has not been detected to date. This is unfortunate, for had the Weber experiments 1,2,3,4 been confirmed by others 5,6,7,8,9,10, gravitational wave astronomy would have opened up a new window into the universe as well as provided a handle to test relativistic theories of gravitation.

Facing cold realities after the considerable theoretical work engendered by the Weber experiments, it now seems that a legitimate search for gravitational radiation from astronomical sources will require a substantial improvement in detector sensitivity, possibly by a factor of 10^4 to 10^6 . A compilation of gravitational radiation sources and their hypothesized spectra is given in appendix 1.

At present there appear to be three approaches that may lead to gravitational wave astronomy with higher sensitivity, none of which is without problems. The first is the development of cooled, high Q bars. The assumption is that since the dominant noise in room temperature antennas is thermal noise, the overall system noise will scale with temperature. Even if this is true, cooled bars will require significant advances in

transducer technology to reach their ultimate potential. The second approach, complementary to the others, is to use many cross-correlated antennas, a scheme that gains sensitivity with the square root of the number of antennas. Thirdly and finally, is to use antennas employing large baselines to capitalize on the property that a gravitational wave creates a strain in space while the noise, is to first order independent of the baseline. For a given displacement noise, the minimum detectable gravitational wave intensity decreases with the square of the antenna baseline which is ultimately limited by the condition that the dimensions of the antenna must be less than or equal to the wavelength of the gravitational wave.

The basis of this proposal is the development of a small, interferometric antenna with 9 meter arms. Although the antenna is 1000 times more sensitive than existing gravitational wave detectors, it is viewed as a prototype of a much larger system with a baseline of a kilometer or more. The interferometric antenna is broad-band and therefore useful in detecting periodic, impulsive and broad-band gravitational radiation sources.

Theory of a Gravitational Wave Interacting with Free Masses

In his 1918 paper on gravitational waves Einstein (11) showed by a perturbation argument that a weak gravitational plane wave has an irreducible metric tensor in an almost Euclidean space. The total metric tensor is

$$g_{ij} = \eta_{ij} + h_{ij} \tag{1}$$

where

$$n_{ij} = \begin{pmatrix} 1 & 0 \\ -1 & 0 \\ 0 & -1 \\ -1 \end{pmatrix}$$
 (2)

is the Minkowski background metric tensor. h_{ij} is the perturbation metric tensor due to the gravitational wave and it is assumed that all components of this tensor are much smaller than 1. If the plane wave propagates along the x_1 direction, it is always possible to find a coordinate system in which h_{ij} takes the irreducible form

$$h_{ij} = \begin{pmatrix} 0 & 1 & 0 \\ ---- & 1 & ---- \\ 0 & 1 & 22 & h_{23} \\ & & 1 & 32 & h_{33} \end{pmatrix}$$
(3)

with $h_{22} = -h_{33}$ and $h_{23} = h_{32}$. The tensor components have the usual functional dependence $f(x_1 - ct)$.

To gain some insight into the meaning of a plane gravitational wave, assume that the wave is in the single polarization state $h_{23} = h_{32} = 0$ and furthermore let $h_{22} = -h_{33} = h$ sin $(kx_1 - \omega t)$. The interval between two neighboring events is then given by

$$ds^{2} = g_{ij}dx^{i}dx^{j} = c^{2}dt^{2} - [dx_{1}^{2} + (1 + h \sin(kx_{1} - \omega t))dx_{2}^{2} + (1 - h \sin(kx_{1} - \omega t))dx_{3}^{2}]$$
(4)

The metric relates coordinate distances to proper lengths. In this metric coordinate time is proper time; however, the spatial coordinates are not proper lengths. One can give some reality to the coordinates by placing free noninteracting masses at various points in space which then label the coordinates. The

proper distance between two coordinate points may then be defined by the light travel time between the masses. Let there be a light source at $x_2 = -\ell/2$ and a receiver at $x_2 = \ell/2$. For light the total interval is always zero so that

$$ds^{2} = 0 = c^{2}dt^{2} - (1 + h \sin(kx_{1} - \omega t))dx_{2}^{2}$$
 (5)

since h << 1

$$cdt = [1 + \frac{h}{2} \sin(kx_1 - \omega t)] dx_2$$
 (6)

If the light travel time, Δt , is much less than the period of the wave, the integral for Δt becomes simple and one gets

$$\Delta t = (1 - \frac{h}{2} \sin \omega t) \frac{\ell}{c}$$
 (7)

In the absence of the gravitational wave $\Delta t = \ell_0/c = \ell/c$, the coordinate distance becomes the proper length. The variation in Δt due to the gravitational wave is given by

$$\delta \Delta t = (\frac{h}{2} \sin \omega t) \frac{\ell}{C}$$
 (8)

This can be interpreted as though the gravitational wave produces a strain in space in the \mathbf{x}_2 direction of

$$\frac{\Delta \ell}{\ell_0} = \frac{h}{2} \sin \omega t = \frac{h_{22}}{2} \tag{9}$$

There is a comparable strain in the x_3 direction, however inverted in phase.

The intensity of the gravitational wave in terms of the plane wave metric tensor is given by Landau and Lifshitz 12 as

$$I_{g} = \frac{c^{3}}{16\pi G} \left[\frac{dh_{23}}{dt} \right]^{2} + \frac{1}{4} \left[\frac{dh_{22}}{dt} - \frac{dh_{33}}{dt} \right]^{2}$$
 (10)

For subsequent calculations, it is more useful to relate the power spectrum of the gravitationally induced displacement to the incident gravitational intensity spectrum.

$$x_g^2(\omega) = \frac{h^2(\omega) \ell_o^2}{4} = \frac{8\pi G \ell_o^2}{G^3 \omega^2} I_g(\omega)$$
 $\ell_o < \lambda_g$ (11)

where l_{o} is the separation of the masses.

The Antenna Design

The principle idea of the antenna is to measure the geodesic deviation of free masses by passing light signals between them. The notion is not new; it has appeared as a Gedanken experiment in F.A.E. Pirani's 13 studies of the measurable properties of the Riemann tensor. However, it became a practical idea only with the advent of lasers and the realization that interferometric distance measurements could be made to a much higher precision than the wavelength of light. The limit is determined by the quantum limited shot noise (Poisson noise) arising from the granularity of light and the statistics of the detection process. It was quickly realized that interferometric gravitational wave antennas had several unique properties; they are broad-band detectors, can be extended to the optimal size of the gravitational wavelength and are not loaded by the displacement detectors.

Initial work on such antennas began at M.I.T. in 1970 as part of several senior thesis projects following the development of an experiment in 1967 that demonstrated shot noise limited interrogation of fringes in a laser illuminated Michelson interferometer ¹⁴.

For the last two years, the design and construction of the prototype antenna has been the Doctor's thesis of Mr. D. K. Owens at M.I.T. who has contributed substantive ideas to the project.

Work began at Hughes Aircraft under the direction of Dr. R. Forward on an interferometric antenna design for use in space at the instigation of Dr. Philip Chapman then of N.A.S.A. Houston and a frequent visitor to M.I.T. in early 1970. The work at Hughes culminated in a premature publication which did not do the idea justice but nevertheless demonstrated again that laser interferometers operating at the Poisson limit were feasible. 15

A schematic drawing of the antenna being constructed at M.I.T. is shown in figure 1. Three masses are suspended on horizontal seismometer mounts in high vacuum (P < 10⁻⁷ torr). The three masses are the mirror mounts of an equal arm Michelson interferometer illuminated by a commercial 1 watt Argon ion laser. Each interferometer arm is a 9 meter long reentrant optical delay line comprised of dielectric coated spherical mirrors in a near confocal configuration. The laser beam is split by a 50 - 50 beam splitter and enters the delay lines through a hole in the spherical mirrors. The beam makes approximately 300 passes in each cavity before reemerging through the same hole by which it entered. The emerging beam passes through Pockel's cell phase shifters and is recombined by the beam splitter after which it is detected by a water cooled PIN Silicon photo diode.

The interferometer is held on a fixed point of a fringe by a servo system using the Pockel's cell phase shifters as controllers. The servo error signal is derived by modulating the optical

phase in oppositely polarized Pockel's cells in the two interferometer arms by $\pm \pi/4$ at a 10MHz rate. The fringe phase modulation is synchronously demodulated yielding an error signal which is applied to the Pockel's cells to maintain the fringe modulation symmetry. The error signal is proportional to the differential displacement of the end masses and is the output of the antenna. With the servo operated in this manner as a nulling device the laser amplitude noise at frequencies other than the modulation frequency is suppressed, provided the open loop gain is high enough.

The dynamic range of the Pockel's cells is limited to phase shifts equivalent to a few wavelengths motion of the end masses. Two approaches can be taken to increase the dynamic range of the interferometer to accomodate long term drifts due to ground noise and temperature changes. The first is to employ a slow, large dynamic range controller to move the end masses, for example an electrostatic force applied to the end masses, to hold the interferometer on a single fringe. The second approach, which we have adopted for the small antenna, is to let the interferometer jump from one fringe to an equivalent point on the neighboring fringe when the error signal has reached a predetermined value. The fringe jumps are counted in an updown counter, converted into analog signals and passed through a high pass filter. The low frequency cut off of this filter determines the low frequency response of the antenna. output of this filter is added to the continuous fringe output The fringe jumps signal and recorded as the antenna output. take place in a time determined by the time constant of the Pockel's cell which is of the order of 10 seconds, during this time the post mixer analog circuitry is reset as well. By properly setting the timing and the error signal amplitude at which the fringe jump occurs, it is possible to make the transients in the antenna output comparable to the Poisson noise.

We have measured the amplitude noise of a Spectra Physics model 165 Argon Ion laser at various power levels with the laser oscillating in both multi and single longitudinal modes. Figure 2 shows the results of these measurements with the laser oscillating in a single longitudinal mode. At frequencies below 300 kHz, the power spectrum of the amplitude noise is dominated by ion acoustic and plasma oscillations as well as spectral peaks at multiples of the power line frequency due to inadequate filtering in the power supply. At frequencies above 3MHz, the amplitude noise closely approaches the Poisson limit even at 1/2 watt output. The measurements were limited to a maximum of 1/2 watt because of the onset of space charge limited flow in the Silicon photodiode at higher power.

The frequency stability of the laser is not critical provided that the difference in optical delay in the two interferometer arms is less than the reciprocal of the oscillating laser line width. Typically, for the Argon laser a delay difference of 10^{-9} seconds (30cm) will contribute a displacement noise due to frequency instability that is less than 1/10 of the Poisson amplitude noise.

The multipass delay lines that comprise the interferometer arms are useful components in an interferometric antenna as long as the Poisson amplitude noise dominates the antenna noise budget and the delay line storage times remain less than 1/2 the period of the gravitational wave. For fixed laser power, the multi-pass arms increase the fringe phase sensitivity of the interferometer by the number of passes per arm. The number of passes is limited by the reflectivity and optical quality of the mirror surfaces.

As long as the Poisson amplitude moise is dominant, the optical delay line is equivalent to increasing the length of the antenna, however at those frequencies where noise sources,

such as thermal and ground noise, that physically move the end mass dominate, the only way to increase the signal-to-noise ratio is to actually increase the antenna baseline.

Optical delay linesusing spherical mirrors have been described by Herriott 16. D. K. Owens at M.I.T. has studied and constructed delay lines using spherical mirrors, a brief description of his results are given in appendix 2. He has discovered several interesting and useful properties of these delay lines. The most encouraging one is that the delay lines If the reentrant condition is satisfied, are easy to align. namely that the input and output beams pass through the same hole, the delay line behaves as though the beam is reflected by the back of the front surface of the mirror which has the coupling The position of the output beam is independent hole in it. of the transverse position and angle of the far mirror as long as the beam pattern does not spill off of the mirrors. discussed in appendix 2, (if the reentrant condition is satisfied) the time delay of the beam in the cavity is insensitive in first order to transverse motions and rotations of the far mirror.

The mirrors intheprototype antenna are 4 inches in diameter, have a radius of 9 meters, a reflectivity of 99.5% at 5145A and 6328A and are good to 1/10 of a wavelength over their entire surface. The coupling hole has a diameter of 1.5mm.

The design of the suspensions for the antenna masses has defied a simple, elegant and economical solution. The suspensions have to satisfy several conditions. First they must have a high Q to reduce the coupling to thermal fluctuations. Second they must provide isolation from ground and acoustic noise. What makes the problem difficult is the inevitable collection of normal modes of motion of a mechanical system which cross-couple and by parametric conversion transfer energy between each other. In other words, the isolation calculated for a long period suspension

is never realized in practice because the suspension structure has its own resonances that couple into the principle mode of the suspension. This is a problem that has long been recognized in the design of seismometers and gravimeters 17. A rule of thumb to minimize problems in suspensions is to keep them simple and to force the resonances of the structural members toward high frequencies.

A possible answer to the suspension problem is to use a diamagnetic superconducting suspension or other field suspension such as servoed electrostatic or magnetic supports. We have made analyses of such systems and in fact constructed a prototype electrostatic suspension. However, for a first attempt at testing the design of the entire antenna, it seems prudent to make an imperfect compromise which has the virtue of simplicity.

The masses are 10kg aluminium blocks suspended as pendula by 4mm diameter fused quartz rodsl meter long. The fundamental period of the suspension is 2 seconds and has a Q in excess of 10⁶. The Q is determined by the internal losses in the quartz but only 5% of the energy of the oscillator is stored in the quartz. The remainder is stored in the gravitational field of the earth, so that the total Q is higher than the internal Q of quartz. The principle problem associated with this suspension is the normal modes of vibration of the quartz rod which occur at approximately 250Hz intervals.

Since the interferometer is insensitive to transverse motion and rotation of the far mirrors, the isolation provided by the suspension is most critical for motion along the lengths of the interferometer arms.

For diagnostic purposes as well as to measure the ground noise contribution to the antenna output, each of the suspended

masses is the inertial member of a horizontal seismometer. The motion of the ground relative to the antenna masses is measured by using capacitive displacement transducers attached to flanges in the vacuum housing. The ground noise measured by the seismometers can be subtracted from the antenna output as described in the following scheme.

The suspension is characterized by the transfer function

$$T(\omega) = x_m(\omega)/x_g(\omega)$$

where $\mathbf{x}_{m}(\omega)$ is the Fourier component of the displacement of the suspended mass in inertial space when driven by a ground motion $\mathbf{x}_{g}(\omega)$, also referred to inertial space. $\mathbf{x}_{g}(\omega)$ is composed of seismic noise as well as the motion of the earth induced by the gravity wave. The interferometer measures the displacement of the masses relative to each other. The relative motion of the masses, $\Delta \mathbf{x}_{m}(\omega)$ is

$$\Delta \mathbf{x}_{\mathrm{m}} \ (\omega) \ = \ \Delta \mathbf{x}_{\mathrm{GW}}(\omega) \ + \ \mathbf{T}_{1} \ (\omega) \, \mathbf{x}_{\mathrm{g1}} \ (\omega) \ - \ \mathbf{T}_{2}(\omega) \, \mathbf{x}_{\mathrm{g2}}(\omega)$$

where $\Delta x_{GW}(\omega)$ is the motion due to the gravitational wave and the subscripts 1 and 2 refer to the two suspensions involved in a single arm of the interferometer. The seismometer measures the motion of the earth relative to the position of of the suspended mass. At one end of the interferometer arm the seismometer output is

$$\Delta x_{R1}$$
 (ω) = $\frac{\Delta x_{GW}(\omega)}{2}$ + (T_1 (ω) - 1) x_{g1} (ω)

while at the other endit is

$$\Delta x_{R2} (\omega) = -\frac{\Delta x_{GW(\omega)}}{2} + (T_2(\omega) - 1)x_{g2}(\omega)$$

The contribution due to the gravitational wave in terms of the measured quantities is given by

$$\Delta \mathbf{x}_{\text{GW}} = \frac{\Delta \mathbf{x}_{\text{m}} (\mathbf{T}_{1} - 1) (\mathbf{T}_{2} - 1) + \Delta \mathbf{x}_{\mathbf{R}_{2}} \mathbf{T}_{2} (\mathbf{T}_{1} - 1) - \Delta \mathbf{x}_{\mathbf{R}_{1}} \mathbf{T}_{1} (\mathbf{T}_{2} - 1)}{[1 - 1/2 (\mathbf{T}_{1} + \mathbf{T}_{2})]}$$

For T_1 and $T_2 << 1$

$$\Delta \mathbf{x}_{GW} = \Delta \mathbf{x}_{m} + \Delta \mathbf{x}_{R_{1}}^{T_{1}} - \Delta \mathbf{x}_{R_{2}}^{T_{2}}$$

The ground noise subtraction scheme looks promising if the suspension transfer functions are small, in other words, there is already substantial isolation of the ground motion and the non-linearities that may make the transfer functions amplitude dependent are small as well.

Noise Sources in the Antenna

The power spectrum of the noise from various sources in an antenna of the design shown in Figure 1 is estimated below. The power spectra are given in equivalent displacements squared per unit frequency interval.

1) Amplitude Noise in the Laser Output Power

The ability tomeasure the motion of an interferometer fringe is limited by the fluctuations in amplitude of the photo current. A fundamental limit to the amplitude noise in a laser output is the shot noise in the arrival rate of the photons, as well as the noise generated in the stochastic process of detection. At bestalaser can exhibit Poisson amplitude noise. This limit has been approached in single mode gas lasers that are free of plasma oscillations and in which the gain in the amplifying medium at the frequency of the oscillating optical line is saturated.

The equivalent spectral noise displacement squared per unit frequency interval in an interferometer of the design in Figure 1 illuminated by a Poisson noise limited laser and using optimal signal processing is given by

$$x^{2}(f) \geq \frac{hc\lambda}{\pi^{2} \epsilon Pb^{2} e^{-(b-1)(1-R)}}$$

h is Planck's constant, c the velocity of light, λ the wavelength of the laser light, ϵ the quantum efficiency of the photodetector, P the total laser output power, b the number of beams in each interferometer arm, and R the reflectivity of the spherical mirrors. The expression has a minimum value for

$$b = 2/(1 - R)$$

As an example, for a 1/2 watt laser at 5000 A° and a mirror reflectivity of 99.5% using a photodetector with a 50% quantum efficiency, the minimum value of the spectral noise power is

$$x^{2}(f) \ge 2x10^{-32} cm^{2}/Hz$$

2) Laser Phase Noise or Frequency Instability Phase instability of the laser is transformed into displacement noise in an unequal path length interferometer. In an ideal laser the phase noise is produced by spontaneous emission which adds photons of random phase to the coherent laser radiation field. The laser phase performs a random walk in angle around the noise-free phase angle given by $\phi_{\rm O}=\omega_{\rm O}t$. The variance in the phase grows as $(\overline{\Delta \phi})^2=t/{\rm st}_{\rm C}$ where s is the number of photons in the laser mode, $t_{\rm C}$ the laser cavity storage time and t the observation time. This phase fluctuation translates

into an oscillating frequency width of the laser given by

$$\delta = \frac{1}{4\pi t_{C}}$$

Armstrong (18) has made an analysis of the spectral power distribution in the output of a two-beam interferometer illuminated by a light source in which the phase noise has a Gaussian distribution in time. Using his results, the equivalent power spectrum of displacement squared per unit frequency in the interferometer is given by

$$_{x}^{2}(f) = \frac{16}{3} \frac{\lambda^{2} \delta^{2} \tau^{3}}{b^{2}}$$

in the case where ft << 1 and $\delta\tau$ << 1. τ is the difference in light travel time between the two paths in the interferometer.

The main reason for using a Michelson interferometer in the gravity antenna is that τ can be made small, if necessary equal to zero, so that one does not have to make excessive demands on the laser frequency stability. In most lasers δ is much larger than that due to spontaneous emission, especially for large τ . However, for small τ , δ does approach the theoretical limit. In a typical case δ might be of the order of 10 Hz and τ approximately 10^{-9} seconds, which gives

$$x^{2}(f) \le 2 \times 10^{-38} cm^{2}/Hz$$

3) Mechanical Thermal Noise in the Antenna

Mechanical thermal noise enters the antenna in two ways. First there is a thermal motion of the center of mass of the masses on the horizontal suspensions and second there is thermal excitation of the internal normal modes of the masses about the

center of the mass. Both types of thermal excitation can be handled with the same technique. The thermal noise is modeled by assuming that the mechanical system is driven by a stochastic driving force with a spectral power density given by

$$F^2(f) = 4kT\alpha$$
 dynes²/Hz

where k is Boltzmann's constant, T the absolute temperature of the damping medium and α the damping coefficient. α can be expressed in terms of the Q, the resonant frequency $\omega_{_{\mbox{O}}}$ of the mechanical system and the mass

$$\alpha = m\omega_{O}/Q$$

The spectral power density of the displacement squared due to the stochastic driving force on a harmonic oscillator is

$$x^{2}(f) = \frac{1}{m^{2}\omega_{Q}^{4}} \frac{1}{(1-z^{2})^{2}+z^{2}/Q^{2}} \frac{4kT\omega_{Q}^{m}}{Q}$$

where

$$z = \omega/\omega_{o}$$

The seismometer suspension should have a resonant frequency much smaller than the frequency of the gravitational wave to be detected; in this case z >> 1 and Q >> 1, giving

$$x^2(f) = 4 \frac{\omega_0}{\omega^4} \frac{kT}{mQ}$$

On the other hand, the lowest normal mode frequencies of the internal motions of the masses including the mirrors and the other suspended optical components should be higher than the gravitational wave frequency. Some care has to be taken to make the entire suspended optical system on each seismometer mount as rigid as possible. For the internal motions $z \ll 1$ and Q >> 1, so that

$$x^{2}(f) = \frac{4kT}{\omega_{O}^{3}mQ}$$

If the internal Q is 10^5 , the mass 10 kg, and the lowest frequency resonance in the mass 10 kHz, the thermal noise due to internal motions at room temperature for frequencies less than 10 kHz is

$$x^{2}(f) \sim 10^{-35} \text{ cm}^{2}/\text{Hz}$$

The thermal noise due to center of mass motion on the suspension for a Q \sim 10 6 and a resonance frequency of 5 x 10 $^{-1}$ Hz becomes

$$x^{2}(f) \sim \frac{10^{-25}}{f^{4}} cm^{2}/Hz$$

for frequencies larger than the resonance frequency of the suspension.

4) Radiation Pressure Noise due to the Laser Light
Fluctuations in the output power of the laser can drive
the suspended masses through the radiation pressure of light.
In principle if the two arms of the interferometer are completely symmetric, both mechanically and optically, the
interferometer output is insensitive to these fluctuations.
Since complete symmetry is hard to achieve, this noise source
must still be considered. An interesting point in pondering

this noise is that although one might find a high modulation frequency for the servo system where the laser displays Poisson noise, it is the spectral power density of the fluctuations in the laser output at the lower frequency of the gravitational wave which excite the antenna. In other words, if this is a serious noise source the laser has to have amplitude stability over a wide range of frequencies.

The radiation pressure noise can be treated in the same manner as the thermal noise. If the laser does display Poisson noise, the spectral power density of a stochastic radiation pressure force on one mirror is

$$F_{rad}^{2}(f) = \frac{4bhP}{\lambda c} dynes^{2}/Hz$$

b is the number of beams in each interferometer arm and P the average total laser power. Using the same sample parameters for the suspension as in the calculation of the thermal noise, and those for the laser in the discussion of the amplitude noise, the ratio

$$\frac{F^{2}_{rad}(f)}{F^{2}_{thermal}(f)} \sim 5 \times 10^{-9}$$

5) Seismic Noise

If the antenna masses were firmly attached to the ground, the seismic noise, both through horizontal and tilt motions of the ground, would be larger than any of the other noise sources considered so far. The seismic noise on the earth at frequencies higher than 5 Hz has been studied by several investigators 19,20,21,22 at various locations both on the surface and at different depths.

In areas far from human industrial activity and traffic, the high frequency noise can be characterized by a stationary random process. The noise at the surface appears higher than at depths of 1 km or more; however, an unambiguous determination of whether the high frequency noise is due to Rayleigh or body waves has not been carried out. Measurements made in a zinc mine at Ogdensburg, New Jersey, (19) at a depth of about 1/2 km and in Jamestown, California (22) yield the smallest

published values of seismic noise. In the region between 10 to 100 Hz, the power spectrum is approximated by

$$x_{\ell}^{2}(f) \sim \frac{3 \times 10^{-14}}{f^{4}} \text{ cm}^{2}/\text{Hz}$$

The spectrum has not been measured at frequencies higher than 100 Hz; however, it is not expected to decrease more slowly with frequency at higher frequencies.

By mounting the antenna masses on horizontal seismometer suspensions, the seismic noise entering the interferometer is substantially reduced. The isolation provided by a single degree of freedom suspension is given by

$$\left|\frac{x_{m}(f)}{x_{\ell}(f)}\right|^{2} = \frac{\left[(1-z^{2}) + (2/Q)^{2}\right]^{2} + (z^{3}/Q)^{2}}{\left[(1-z^{2})^{2} + (z/Q)^{2}\right]^{2}}$$

where $z = f/f_0$, and f_0 is the resonant frequency of the suspension. $x_m(f)$ is the displacement of an antenna mass at frequency frelative to an inertial frame; $x_k(f)$ is the motion of the earth measured in the same reference frame.

At frequencies for which $z \gg 1$, the isolation ratio is

$$\left|\frac{x_{m}(f)}{x_{\ell}(f)}\right|^{2} \sim \left(\frac{f_{o}}{f}\right)^{4} + \left(\frac{f_{o}}{f}\right)^{2} \frac{1}{o^{2}}$$

For the sample suspension parameters given previously, the estimated seismic noise entering the antenna becomes

$$x^{2}(f) > \frac{2 \times 10^{-14}}{f^{8}} cm^{2}/Hz$$
 10 < f < 10 kHz

At frequencies higher than 180 Hz, the seismic noise is smaller than the Poisson noise due to the laser amplitude fluctuations. If the ground noise subtraction scheme described earlier can be made towork to a precision of 1%, the laser noise remains dominant down to 50 Hz.

6) Thermal Gradient Noise

Thermal gradients in the chamber housing the suspension produce differential pressures on the suspended mass through the residual gas molecules. The largest unbalanced heat input into the system occurs at the interferometer mirror where after multiple reflections approximately 1/10 of the laser power will be absorbed.

The excess pressure on the mirror surface is approximately

where n is the number of gas molecules per cc, k Boltzmann's constant and ΔT the difference in temperature between the mirror surface and the rest of the chamber. The fluctuations in ΔT can be adequately calculated by solving the one-dimensional problem of thermal diffusion from the surface into the body of the mirror and the associated antenna mass which are assumed to be at a constant temperature.

The mirror surface temperature fluctuations T(f), driven by incident intensity fluctuations I(f), is given by

$$T(f) = \frac{\Delta I(f)}{4\epsilon\sigma T_{O}^{3} + (\pi c_{V}^{\rho k_{t}})^{1/2} f^{1/2}}$$

The first term in the denominator is the radiation from the surface; ϵ is the emissivity, σ the Stefan-Boltzmann constant, and T_O the ambient temperature. The second term is due to thermal diffusion from the surface into the interior; c_V is the specific heat, ρ the density and k_t the thermal conductivity of the mirror.

If the laser exhibits Poisson noise the spectral force density on the antenna mass becomes

$$F^{2}(f) = \frac{2(nk)^{2}}{f(\pi c_{v}^{\rho k_{t}})} \frac{hc}{\lambda} \overline{P} dynes^{2}/Hz$$

Radiation is neglected as it is much smaller than the thermal diffusion. Using the following parameters for glass, $c_v^{-10^6}$ ergs/sec cm 0 K, an average laser power of 1/2 watt and a vacuum of 1 x 10^{-8} mm Hg, the ratio between the thermal gradient noise to the thermal noise to the thermal noise forces in the sample suspension is

$$\frac{F_{T,G}^{2}(f)}{F_{th}^{2}(f)} \sim \frac{1}{f} 10^{-15}$$

7) Cosmic Ray Noise

The principal component of the high energy particle background both below and on the earth's surface are muons with kinetic energies larger than 0.1 Bev. (23) A muon that passes through or stops in one of the antenna masses imparts momentum to the mass, resulting in a displacement given by

$$\Delta x = \frac{\Delta E \cos \theta}{m\omega_{o}c}$$

AE is the energy loss of the muon in the antenna mass, 0 the angle between the displacement and the incident muon momentum, m the antenna mass and ω_{0} the suspension resonant frequency.

The energy loss of muons in matter is almost entirely through electromagnetic interactions so that the energy loss per column density, k(E), is virtually constant with energy for relativistic muons. A 10^{-1} Bev muon loses 3 Mev/gm/cm², while a 10^4 Bev muon loses \sim 30 Mev/gm/cm².

The vertical flux of muons at sea level with an energy greater than 10^{-1} Bev is approximately 10^{-2} particles/cm² sec steradian. For energies larger than 10 Bev, the intergrated flux varies as $\sim 10^{-1}/\text{E}^2$ (Bev).

Since the flux falls off steeply with energy and the energy loss is almost independent of energy, the bulk of the muon events will impart the same momentum to the suspension. Using the following sample suspension parameters, m $\sim 10^4$ grams, f $_{\rm O}$ $\sim 5 \times 10^{-1}$ Hz, $\rho \sim 3$ and typical linear dimensions ~ 10 cm, the average energy loss per muon becomes $\sim 10^{-1} {\rm Bev}$. At sea level the antenna mass might experience impulsive displacements $\sim 10^{-18}$ cm occurring at an average rate of once per second. An event due to the passage of a 10^4 Bev muon results in a displacement of 10^{-17} cm at a rate of once per year.

Although the shape of the antenna mass can be designed to somewhat reduce the effect and frequency of muon interactions, especially by taking advantage of the anisotropy of the muon flux, the best way of reducing the noise is to place the antenna masses underground. The pulse rate at depths of 20 meters, 200 meters, and 2 km is approximately 3×10^{-2} , 10^{-4} , 10^{-9} pulses/sec.

If the antenna output is measured over times that include many muon pulses, as would be the case in a search for pulsar radiation, the noise can be treated as a stationary distribution. Assuming that the muon events are random and for

ease of calculation that the magnitude of the momentum impacts is the same for all muons, the spectral power density of displacement squared of the antenna mass is

$$x^{2}(f) = \frac{4N(\Delta E/c)^{2}}{(2\pi)^{4}m^{2}f^{4}}$$
 cm²/Hz

for $f \gg f_0$.

N is the average number of pulses per second, $\Delta E/c$ the momentum imparted to the mass per pulse, and m the antenna mass. For the sample suspension parameters at sea level

$$x^{2}(f) \sim 10^{-40}/f^{4}$$
 cm²/Hz

8) Gravitational Gradient Noise

The antenna is sensitive to gravitational field gradients -- differential gravitational forces exerted on the masses of defining the ends of the interferometer arms. No data are available concerning the naturally occurring high frequency gravitational gradients on or near the surface of the earth. There are two effects which can make gravitational gradient noise; first, time dependent density variations in both the atmosphere and the ground and second, motions of existing inhomogeneities in the mass distribution around the antenna.

An estimate for the two effects can be made with a crude model. Assume that one of the antenna masses is at the boundary of a volume that has a fluctuating density. The amount of mass that can partake in a coherent density fluctuation at a frequency f and exert a force on the mass is roughly that included in a sphere with a radius equal to half the acoustic wavelength, λ , in the ground. The fluctuating gravitational force on the mass is

$$\frac{\mathbf{F}_{\mathbf{g}}(\mathbf{f})}{\mathbf{m}} \sim \frac{2}{3} \pi \lambda \Lambda \rho(\mathbf{f}) \mathbf{G}$$

where $\Delta \rho(f)$ is the density fluctuation at frequency f and G the Newtonian gravitational constant. The density fluctuations driven by ground noise in the sphere are

$$\rho(f) = 3 < \rho > \frac{x_{\varepsilon}(f)}{\lambda}$$

where $\langle \rho \rangle$ is the average density of the ground and $x_{\epsilon}(f)$ the ground noise displacement. If f is larger than the resonant frequency of the suspension, the ratio of the suspension, the ratio of the displacement squared of the mass to that of the ground motion is given by

$$\frac{x_{m}^{2}(f)}{x_{e}^{2}(f)} = \left[\frac{\langle \rho \rangle G}{2\pi f^{2}}\right]^{2}$$

For the earth, this isolation factor is

$$\frac{x_{\rm m}^2(f)}{x_{\rm e}^2(f)} \sim \frac{10^{-14}}{f^4}$$

which is much smaller than the isolation factor for the attenuation of direct ground motion by the sample suspension.

A comparable approach can be used in estimating the effect of motions of inhomogeneities in the matter distribution around the antennawhich are driven by ground noise. Assuming the extreme case of a complete inhomogeneity, for example, an atmosphere ground interface, the mass that partakes in a coherent motion x(f) could be $m \sim \lambda^3 < \rho >$. The fluctuating force on the nearest antenna becomes

$$\frac{F_{g}(f)}{m} = \frac{2}{3}\pi G < \rho > x(f)$$

The isolation factor is

$$\frac{x_{m}^{2}(f)}{x_{e}^{2}(f)} \sim \frac{G < \rho >}{6\pi f^{2}}^{2}$$

which is comparable to the isolation factor due to density fluctuations. These factors become smaller if the distance between the masses is smaller than λ .

9) Electric and Magnetic Field Noise

Electric fields in dielectric-free conducting vacuum chambers are typically 10^{-3} volts/cm. These fields are due to variations in the work function of surfaces and occur even when all the surfaces in a system are constructed of the same material, since the work function of one crystal face is different than that of another. Temporal fluctuations in these fields are caused by impurity migrations and variations in absorbed gas layers. Little is known about the correlation time of these fluctuations except that at room temperature it seems to be longer than a few seconds and at cryogenic temperatures it is possible to keep the fields constant to better than 10^{-2} volts/cm for several hours. (24)

The electric force on a suspended antenna mass is

$$F_e \sim \frac{1}{4\pi} \epsilon^2 A$$

where A is the exposed antenna surface and ϵ the fluctuating electric field at the surface. Assuming that the power spectrum of the field fluctuations is similar to that of the flicker effect in vacuum tubes or the surface effects in semiconductors, which are both due to large scale but slow changes in the

surface properties of materials, the electric force power spectrum might be represented by

$$F_e^2(f) \sim \frac{\frac{2}{\pi} \langle F_e^2 \rangle 1/\tau_o}{(1/\tau_o)^2 + (2\pi f)^2}$$

 τ_{o} is the correlation time of the fluctuations and $\langle F_{e}^{2} \rangle$ is the average electric force squared.

If the gravitationalwave frequency is much larger than $1/\tau_{_{\hbox{\scriptsize O}}}$ and also higher than the resonant frequency of the suspension, the power spectrum of the displacements squared becomes

$$x^{2}(f) = \frac{\langle \epsilon^{4} \rangle A^{2}}{32\pi^{6} m^{2} \tau_{O} f^{4}} cm^{2}/Hz$$

For m $^{\circ}$ 10 4 gm, A $^{\circ}$ 10 2 , ϵ $^{\circ}$ 10 $^{-5}$ stat volts/cm and τ_{o} $^{\circ}$ 1 sec,

$$x^{2}(f) \sim 10^{-38}/f^{4}$$
 cm²/Hz

Although this noise is a good deal less than that due to the Poisson noise of the laser, some care has to be taken to electrostatically shield the mirror surfaces, which are dielectrics.

Geomagnetic storms due to ionospheric currents driven by the solar wind and cosmic rays create fluctuating magnetic fields at the earth's surface. The smoothed power spectrum of the magnetic field fluctuations in mid-latitude regions at frequencies greater than 10^{-3} Hz is approximately

$$B^2(f) \sim B_0^2/f^2 \text{ gauss}^2/Hz$$

with B_o $^{\circ}$ 3 x 10⁻⁸ gauss. (25) Large pulses with amplitudes $^{\circ}$ 5 x 10⁻³ gauss are observed occasionally; the rise time of these pulses is of the order of minutes. (26)

Fluctuating magnetic fields interact with the antenna mass primarily througheddy currents induced in it or, if it is constructed of insulating material, in the conducting coating around it required to prevent charge buildup. The interaction, especially at low frequencies, can also take place through ferromagnetic impurities in nonmagnetic materials. Magnetic field gradients cause center of mass motions of the suspended mass. Internal motions are excited by magnetic pressures if the skin depth is smaller than the dimensions of the antenna mass.

An extreme model would be to assume that the fluctuating magnetic fields are completely excluded by the antenna mass and that the field changes over the dimensions of the mass are equal to the fields. The magnetic forces are

$$F_{m} = \frac{1}{4\pi} B^{2}A$$

The power spectrum for center of mass motions, if f >> $f_{_{\hbox{\scriptsize O}}},$ becomes

$$x^{2}(f) = \frac{A^{2}B_{0}^{4}}{16\pi^{3}m^{2}f^{4}}$$
 cm²/Hz

For the sample suspension using the smoothed power spectrum of magnetic field fluctuations,

$$x^{2}(f) \sim 10^{-36}/f^{4} \text{ cm}^{2}/Hz$$

The displacements due to internal motions driven by magnetic pressures at frequencies smaller than the internal

resonant frequency, for are given by

$$x^{2}(f) = \frac{A^{2}B_{O}^{4}}{16\pi^{3}m^{2}f_{Oint}^{2}} cm^{2}/Hz$$

Although the disturbances due to the smoothed power spectrum do not appear troublesome relative to the other noise sources, the occasional large magnetic pulses will require that both conducting and high μ magnetic shields be placed around the antenna masses.

^{*} It is not inconceivable that Weber's coincident events may be caused by pulses ingeomagnetic storms, if his conducting shielding is inadequate. It would require a pulse of 10^{-2} gauss with a rise time $\sim 10^{-3}$ seconds to distort his bars by $\Delta \ell / \ell \sim 10^{-16}$. M. Gordon has measured naturally occurring pulses of this length and amplitude as part of senior thesis project in physics at M.I.T.

The Detection of Gravitational Radiation By a Broad-Band Interferometric Antenna

The fundamental limit for the detection of gravitational radiation by an intraferometric antenna is determined by the Poisson amplitude noise of the laser and photodetection process. It appears that this limit can be reached in the prototype antenna at frequencies greater than 150 Hz. The minimum detectable gravitational radiation spectral intensity is

$$I_{g_{\min}}(f) = \left(\frac{hc^4}{\pi G}\right) \left(\frac{\lambda}{\eta P_{Q}}\right) \frac{f^2}{\ell^2 b^2 c^{-(b-1)(1-R)}} = Af^2 \frac{\text{watts}}{cm^2 Hz}$$
(1)

where

h is Planck's constant

c velocity of light

G Newtonian gravitational constant

 λ wavelength of the laser

n quantum efficiency of the photo detector

 P_{O} output power of the laser

f frequency of the gravitational wave

length of the interferometer arms

b the number of beams per arm

R reflectivity of the cavity mirrors

The prototype 9 meter antenna has the limit

$$I_{g_{\min}}(f) = 3.2 \times 10^{-6} f^2 \text{ watts/cm}^2 \text{ Hz}$$

for frequencies less than 200 KHz. The high frequency limit is determined by the cavity storage time which is 9 $\mu sec.$

The length or cavity storage time for the optimum antenna satisfies the condition

$$\frac{\text{lb}}{\text{c}} = \tau/2$$

where $\boldsymbol{\tau}$ is the period of the gravitational wave. The minimum detectable spectral intensity for the optimum antenna is

$$I_{g_{\min}}(f) = \left(\frac{4hc^2}{\pi G}\right) \left(\frac{\lambda}{\eta P_O}\right) = f^4 = Bf^4$$

For comparison, using the same laser power and photo detection efficiency as is the prototype, the minimum detectable spectral intensity would be

$$I_{g_{\min}}(f) = 2.3 \times 10^{-16} f^4$$
 watts/cm²Hz

The detection limits for periodic, broad-band and impulsive sources are described separately.

I. Periodic Sources

Periodic sources of well known frequency such as pulsars and binary systems would be synchronously detected and a narrow bandwidth would be achieved by post mixer digital integration. The gravitational radiation spectrum intensity from a periodic source is a narrow line which wanders in frequency due to the Doppler effect from the varying relative motion of the Earth and source. This frequency spread can be accommodated by adjusting the frequency of the local oscillator. The minimum detectable intensity is

$$I_{\min} = \frac{I_{g_{\min}}(f_o)}{2t_{\inf}}$$

where t int is the post-mixer integration time.

As an example, the upper limit of the 60.4 Hz gravitational radiation from the Crab Pulsar NP0532 incident at the Earth is estimated at 10⁻¹³ watts/cm² (Appendix 1). Using the 9 meter prototype antenna, an integration time of 3700 years would be necessary to detect this radiation with a signal-to-noise ratio of 2. A multi-pass interferometric antenna with the same parameters as the protytype antenna, but 1 km long would require 3.6 months to detect the NP0532 upper limit. A space antenna of the optimal length, 2500 km, with single pass arms would require 8.5 hours of integration. The search for gravitational radiation could be extended to lower frequencies to include slower pulsars and binary star systems.

II. Broad-band sources

A search for broad-band gravitational radiation from discrete astronomical sources is carried out with the interferometric antenna used as a gravitational radiation radiometer and using the Earth's rotation as a modulator. If there is a discrete source of broad-band gravitational radiation, the detected signal will be a maximum each time one of the interferometer arms is perpendicular to the line joining the Earth and the source. A detection scheme for this process is shown in Figure 3. The antenna output is square-law detected and then cross-correlated with an oscillator which has a period of 1/4 of a sidereal day. In order to detect radiation from sources lying in any quadrant of the sky, the antenna output is also cross-correlated with a 90° phase-shifted output of the oscillator.

The minimum detectable signal is calculated by using the

effective noise bandwidth of the signal processing given by

$$\Delta f = \left(\frac{\Delta f_{ant}}{2t_{int}}\right)^{1/2}$$

where $\Delta f_{\rm ant}$ is the bandwidth of the antenna and post-detection filtering, and $t_{\rm int}$ is the observing time. The gravitational radiation signal appears as a component with a period of 1/4 of the sidereal day.

The minimum detectable signal depends on the nature of the source spectrum. If the source has a flat spectrum over the bandwidth of the antenna, the minimum detectable spectral intensity is

$$I_{g_{\min}}(f) = A \left(\frac{f_h f_1}{\Delta f_{ant}}\right) \frac{1}{2} \frac{1}{(2t_{int})} \frac{1}{2}$$
 watts/cm²Hz

where \mathbf{f}_1 and \mathbf{f}_h are the low and high frequency cut-offs of the antenna and A is defined in equation 1 of this section.

As an example, if one extends a search from 100 Hz to 1 KHz using the 9 meter prototype antenna, the minimum detectable intensity (S/N = 2/1) after 1 month of integration is 1×10^{-5} watts/cm²Hz.

If the source really had a flat spectrum, it would be best to use as low a frequency and as narrow a bandwidth as possible within the constraints that the antenna be Poisson noise limited.

If the source spectrum is a power law such as a thermal spectrum

$$I(f) = \alpha f^2.$$

the minimum detectable α , which can be related to an antenna

brightness temperature, is

$$\alpha_{\min} = A \left(\frac{\Delta f_{\text{int}}}{\Delta f_{\text{ant}}} \right)^{1/2} = A \left(\frac{1}{2t_{\text{int}}\Delta f_{\text{ant}}} \right)^{1/2}$$

In terms of an antenna brightness temperature

$$T_{ant_{min}} = \frac{\alpha_{min}c^2}{2k}$$

Using the maximum bandwidth in the present prototype antenna design of 200 KHz, and an integration time of 1 month,

$$\alpha_{\min} \sim 3 \times 10^{-12}$$
 watts/cm²Hz³

Although this may appear to be a small number, it corresponds to an appallingly high temperature of $T_{ant} \sim 10^{32} \, \rm sk.$ A truly thermal process will most likely not be detected with this antenna.

III. Impulsive Sources

The detection of impulsive events is difficult to analyze in detail because the sensitivity of the antenna depends somewhat on the shape of the pulse and the signal processing. We consider a pulse which lasts for a time t and has a maximum strain amplitude $\Delta \ell/\ell$. It is assumed that the pulse does not oscillate many times and that the time dependent Riemann tensor has zero mean. Aside from numerical factors of order unity which depend on the detailed shape of the pulse, the gravitational radiation energy surface density (Joules/cm²) that passes through the antenna is approximately

$$E/A \sim \frac{c^3}{8\pi G} \frac{\left(\Delta \ell/\ell\right)^2}{t}$$

The criterion for detectability is that pulse induced strain in the antenna exceed the noise induced strain. The optimal post-detection filter has a time constant short enough to fully develop the pulse but long enough to integrate the Poisson noise. The optimal filter, a matched filter, has a time constant approximately equal to the length of the pulse. For a matched filter, the minimum detectable strain is given by

$$\left(\frac{\Delta \ell}{\ell} \text{ (t)}\right)^2 = \frac{hc\lambda}{\pi^2 \eta P_0 b^2 \ell^2 e^{-(b-1)(1-R)}} \frac{1}{t}$$

and the minimum detectable pulse surface energy density is

$$\left(\frac{E}{A}\right)_{\min} = \frac{c^3}{8\pi G} \left(\frac{\Delta \ell(t)}{\ell}\right)^2 \frac{1}{t}$$

For the prototype antenna this is

$$(E/A)_{min} = \frac{4 \times 10^{-8}}{t^2}$$
 Joules/cm²

Comparison of the prototype interferometric antenna with existing acoustically coupled bar antennas

The table below summarizes the published performance of several acoustic bar gravitational antennas. The first column

gives the mass of the antenna, the second the length, the third the resonant frequency, the fourth is the post-detection bandwidth, the fifth gives the mechanical Q of the bar, the sixth column gives the pulse detection limits in terms of the minimum energy observable relative to the thermal noise in the These limits are expressed as minimum detectable strain amplitudes in the seventh column. The eighth column gives the minimum detectable energy surface density which is for pulses that last approximately the period of the bar. The last column gives the minimum observable spectral intensity if square-law detected and integrated for one second. The last two rows give two examples using the prototype interferometric antenna. The first example shows the estimated performance if the antenna has post-detection filtering to match Tyson's antenna. The second example is an estimate of the performance of the prototype antenna as a broad-band instrument at the lowest frequencies where Poisson noise is still expected to dominate.

The minimum observable spectral intensity of broad-band gravitational radiation that can be detected in an acoustically coupled detectors has not been discussed in the literature. In the calculations used to generate the last column of the table, it is assumed that the signal processing is done as in figure 3; however, at a modulation rate rate of 1/2 the sidereal period and it is also assumed that the dominant noise in the system is the thermal noise in the acoustically coupled structure. For these conditions, the minimum detectable gravitational spectral intensity in the vicinity of the structures resonance frequency is given by

$$I(\omega_{O}) > \frac{c^{3}KT}{\pi G \omega_{O}^{3/2} 1^{2} MQ^{1/2} t_{int}^{1/2}}$$

8.5x10 ⁻³	4×10 ⁻⁴ 8.	1.6x10 ⁻¹⁸	1	I	100	'n	900	30	Interferometric antenna Ex. 2
.02	.04	5x10 ⁻¹⁸	1	t	1000	.71	900	30	Interferometric antenna Ex. 1
22	35	1.4x10 ⁻¹⁶	<u>1</u> 50	2.2x10 ³	800	1. 1	155	300	Drever 6
L	008	3.3×10 ⁻¹⁶	10	1.3x10 ⁴	21	1.695	150	118	Levine ⁵ Garwin
.07	1.4	3.5×10 ⁻¹⁷	1 30	2.2x10 ⁵	2	0.71	357	3630	Tyson ⁷
ហ	25	1×10 ⁻¹⁶	101	7.7×10 ⁴	2	1.6	153	1300	Weber ^{1,2,3,4}
I _g (fo) watts/cm ² Hz	E/A I	$\left(\frac{\Delta \mathcal{L}}{\mathcal{L}}\right)_{ exttt{min}}$	limit	Q kī	Bandwidth Hz	Center freq. kHz	length cm	mass Kg	Experiment
									Table 1
				-			-	- - - -	

FIGURES

Figure 1

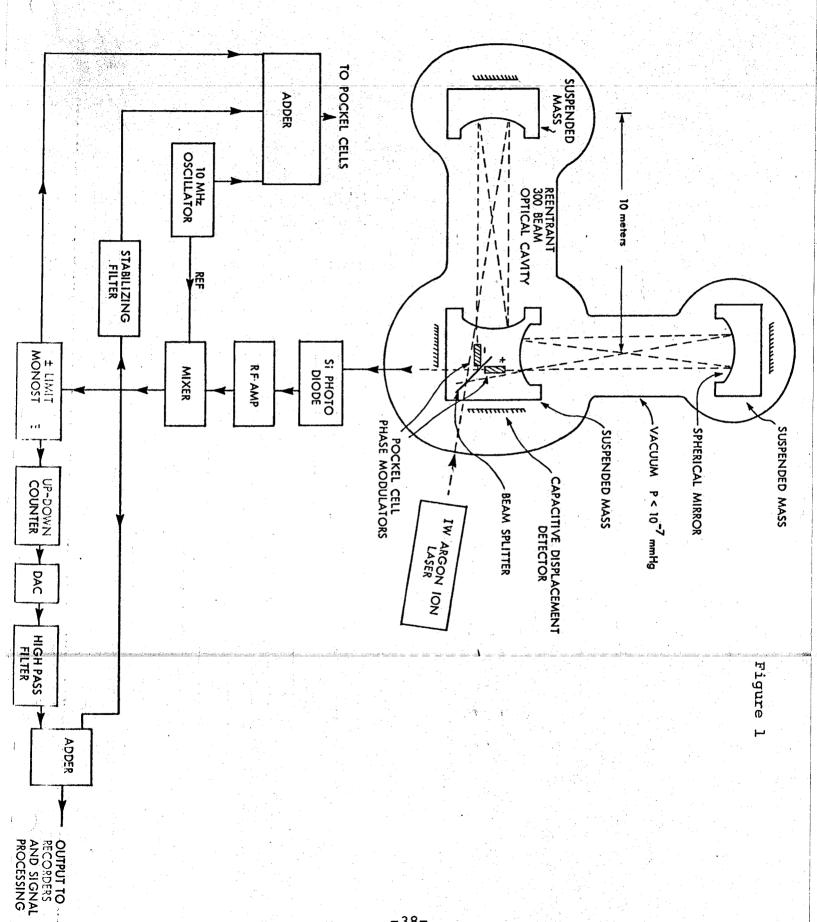
Schematic drawing of the antenna being constructed at M.I.T.

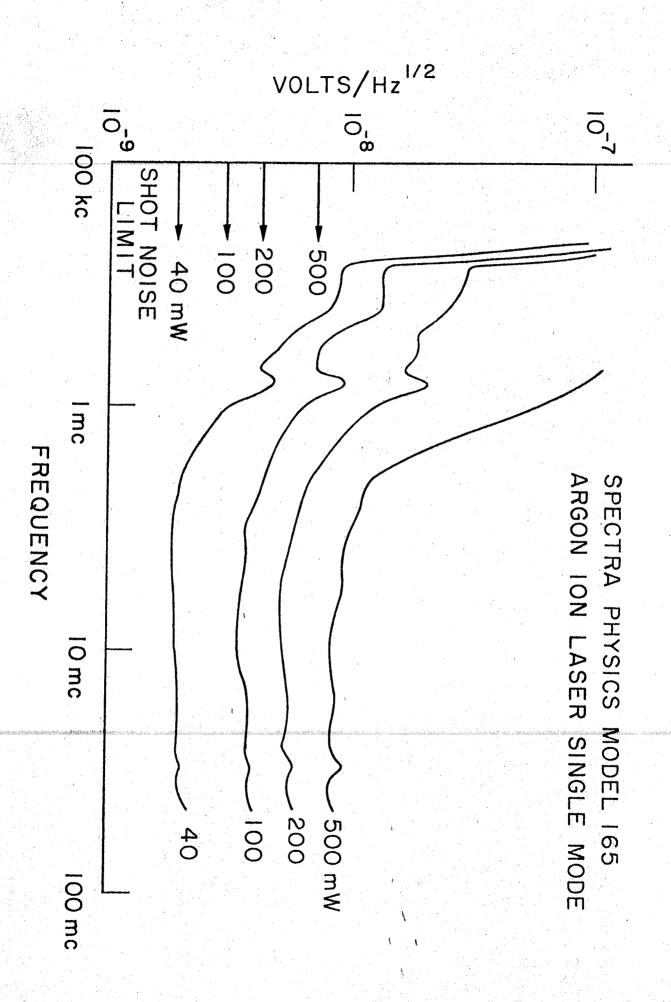
Figure 2.

Amplitude noise in a Spectra Physics Model 165 Argon Ion Laser operating in a single longitudinal mode.

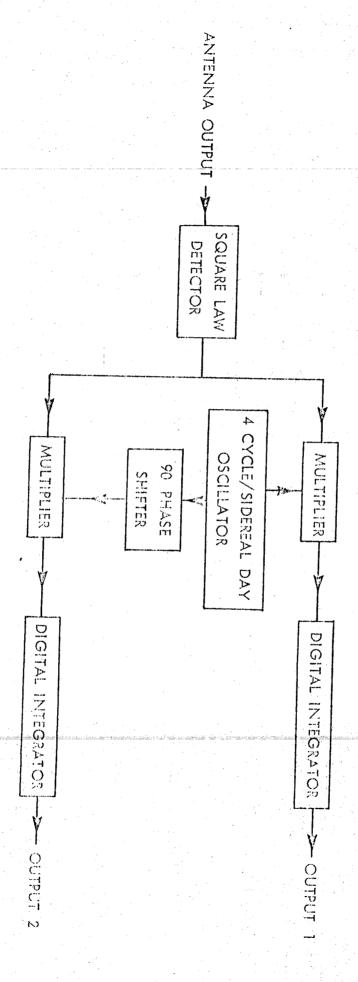
Figure 3.

Detection scheme for localized broad-band sources.





Figure



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Biographical Sketch

Rainer Weiss

Date of Birth: September 29, 1932 Title: Professor of Physics

Place of Birth: Berlin, Germany

Citizenship: U.S.A.

Education

Massachusetts Institute of Technology B.S. 1955
Massachusetts Institute of Technology Ph.D. 1962

Professional Experience

1973 - Present	Professor of Physics, M.I.T.
1967 - 1973	Associate Professor of Physics, M.I.T.
1964 - 1967	Assistant Professor of Physics, M.I.T.
1962 - 1964	Research Associate in Physics, Princeton University
1961 - 1962	Assistant Professor of Physics, Tufts University
1960 - 1961	Instructor of Physics, Tufts University

Publications

- 1. "Magnetic Moments and Hyperfine Structure Anomalies of Cs 133 , Cs 135 , and Cs 137 ," Phys. Rev. $\underline{105}$, p. 590 (1957), with H. H. Stroke, V. Jaccarino, and D. S. Edmonds.
- 2. "Molecular Beam Electron Bombardment Detector," Rev. Sci. Instr., 32, 397 (1961).

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Present Support and Proposals Pending

- National Aeronautics and Space Administration Grant NGR 22-009-526 Title: "Astronomy in the Region between 1 mm and 0.1mm Wavelengths" \$ 49,200 for year 10/31/73 - 9/30/74 Principal Investigator: Rainer Weiss

Proposals Pending

Renewal of (1) above, National Aeronautics and Space Administration Grant NGR 22-009-526 in the amount of \$50,000 for year 10/1/74 - 9/30/75.

Proposal to the National Aeronautics and Space Administration in the amount of \$10,000 entitled "The Charter & Budget for FY75 of a Sub-Panel on Experimental Relativity and Gravitation" for one year.

The renewal of (2) above, U.S. Army Electronics Command contract is anticipated but there has been no amount determined at this time.

This proposal is being submitted only to the National Science Foundation.

MASSACHUSETTS INSTITUTE OF TECHNOLOGY RESEARCH LABORATORY OF ELECTRONICS CAMBRIDGE, MASS. 02139

August 28, 1974

Research Grant Proposal Budget 2 years beginning January 1, 1975

		1 .	F Fun			lst year	2nd year
Α.	SALARIES AND WAGES		Acad			Amount	Amount
	1. Senior Personnel:						
	a. Principal Investigator R. Weiss (12%-18 mos)		2		\$	2,830	\$ 3,000
	2. Other Personnel:						
	a. Graduate Student 1 Research Asst. (100%-24 mos) D. Kingston Owens		18	6		8,640	9,000
	b. Technical 1 Technical Asst. (25%-24 mos) R. Benford	6				3,000	3,200
	c. Allocated Proj. Level Costs (See p. 49)				· · · <u></u>	2,800	3,000
	Total Salaries & Wages	6	20	6	\$	17,270	\$ 18,200
В.	FRINGE BENEFITS (18.4% of S&W except	Res.	Asst	•)	. <u></u>	1,587	1,692
C.	TOTAL S & W and FRINGE BENEFITS	(\$	18,857	\$ 19,892
D.	PERMANENT EQUIPMENT					8,320	5,000
Ε.	EXPENDABLE SUPPLIES AND EQUIPMENT					14,500	7,025
F.	TRAVEL (domestic)					500	500
G.	PUBLICATIONS COSTS				. •	-0-	500
н.	COMPUTER COSTS				*	-0-	-0-
£.,	OTHER COSTS (freight, phone, etc.)		· ·	1		116	299
	TOTAL DIRECT COSTS				\$	42,293	\$ 33,216
К.	INDIRECT COSTS (62% of S&W)					10,707	11,284
L.	TOTAL COSTS PER YEAR				\$	53,000	\$ 44,500
М.	TOTAL TWO YEARS					¢07 F	0.0

-46-

Estimated Equipment Needs

			Year l	Year 2
1	Direct and FM instrument tape recorder Ampex FR 1300 used but reconditioned		\$ 8,000	
1	Disk drive for PDP 11/20 compute DEC RK05	r		\$ 5,000
1	Beam steering device Spectra Physics # 383		150	
1	Beam director Spectra Physics # 384-8 with two # 384C dielectric coated mirrors		170	
	Total		\$ 8,320	\$ 5,000

Estimated Expendable Supplies and Equipment

		Year l	Year 2
1	Replacement discharge tube for Spectar Physics #165-03 laser		\$ 2,125
4	Replacement 4" diameter spherical mirrors 99.5% reflectivity		2,400
	Miscellaneous optical components \$ such as AR coated windows and lenses	1,000	
-	Materials and shop time for assembly of vacuum system, suspensions, welding, etc.	5,000	
	Site preparation at off campus location, power, water and concrete posts	6,000	
	Small electronic components integrated circuits, modular power supplies	2,000	2,000
	Operations costs, power, water, etc.	500	500
	Total \$	14,500	\$ 7,025

Allocated Project Level Costs

Project Level Costs apply to research performed within the Research Laboratory of Electronics and include such items as:

- (i) Salaries and Wages of R.L.E. administrative personnel, foremen, stock clerks, etc. (Overhead is applied to these costs).
- (ii) Office supplies, common small value consumables, etc.
 (No overhead is applied to these costs).

An allocation is made monthly to distribute these costs to the active projects in proportion to the amount of salaries and wages incurred by each project during the month.

This treatment is in accordance with ASPR Section 15-304 which defines direct costs as "those costs that can be identified specifically with a particular research project, an instructional activity, or any other institutional activity, or which can be directly assigned to such activities relatively easily with a high degree of accuracy".

The Defense Contract Audit Agency performs continuous reviews of the M.I.T. accounting system, including Allocated Project Level Costs, and has not taken an exception to the Allocation method.

APPENDIX 1

Appendix I

Astrophysical Sources of Gravitational Radiation

The astrophysical sources of gravitational radiation discussed here are collisions, pulsars, neutron stars, and binary stars. Exotic phenomena such as 10 8 Me black holes in the Galactic center will not be considered. Collisions between collapsed objects, or matterfalling into collapsed objects could produce considerable amounts of gravitational radiation; however, it appears that direct collision is a rare occurrence. Supernovae, and the formation of neutron stars could also be strong sources of gravitational radiation but the expected mean time between events of 5 to 50 years does not make these sources very attractive. The two remaining sources of gravitational radiation, pulsars and binary stars, are believed to be continuous emitters and are probably the best candidates for future studies of gravitational radiation. these sources will be difficult to observe. Pulsars emit in a favorable frequency range of 1 to 60 Hz but the strain induced at the detector is very small. Binary stars produce substantial strains at the antenna but at frequencies less than 4×10^{-4} Hz. There are undoubtedly other sources of gravitational radiational not listed in Table 2; however, it is hoped that the sources and formulas listed are representative enough to give some idea of the events which could be detected by gravitational wave antennas to be built in the near future.

To get some idea of the collision rate for collapsed objects, some estimate must be made of the number of these objects in the Galaxy. Peebles (1) notes that between ten and twenty percent of the mass in the Galaxy resides in stars of

mass greater than 2 Me. A 2 Me exhausts its fuel in about 2 x 10⁹ years and since the Galaxy is about 10¹⁰ years old, perhaps ten or twentypercent of the mass of the Galaxy is contained in collapsed objects. The mass of the Galaxy is about 2 x 10¹¹ Me and if ten percent of this mass goes into 2 Me collapsed objects, then we can estimate that there are roughly 10¹⁰ collapsed objects in the Galaxy. Ostriker, Rees, and Silk (2) note that 10⁹ neutron stars moving through the interstellar plasma could produce an X-ray flux comparable to the X-ray luminosity of the Galaxy. For the following, it will be assumed that ten percent of the stars in any region of the Galaxy are collapsed.

The total collision rate of type 1 objects onto type 2 objects in a volume V, can be estimated using

$$R = \frac{N_1 N_2}{V} < v_{re1} > \sigma_{12}$$

for the rate and

$$\sigma_{12} = \pi (R_1 + R_2)^2 \left[1 + \frac{2G(M_1 + M_2)}{(R_1 + R_2) < v_{rel}^2} \right]$$

for the direct collision cross-section. N_1 and N_2 are the number of type 1 and type 2 objects, V is the volume of the interaction region, $\langle v_{rel} \rangle$ is the average relative speed at large seperation, R is the radius and M themass of the objects, and G is the gravitational constant. Table 1 shows the mean time between collisions for various objects in the globular cluster M92 and in the Galactic center. For M92 the central density is about 6000 stars pc⁻³, there are about 10⁵ stars and $\langle v_{rel} \rangle$ 5 kmsec⁻¹. For the Galaxy the central density is about 10^6 stars pc⁻³, there are about 5 x 10^8 stars and $\langle v_{rel} \rangle$

 \simeq 200 kmsec $^{-1}$. For the stars, we assume M = 1M0 , R = 1R0 and for the collapsed objects M = 1.5M0 and R = 10km.

Table 1: Mean time between collisions

	M92	Galactic center
Stars on stars	$3.4 \times 10^6 y$	160y
Collapsed stars on stars	5.4 x 10 ⁷ y	2500y
Collapsed stars on collapsed stars	$1.6 \times 10^{13} \text{y}$	$7.4 \times 10^{8} \text{y}$

The foregoing analysis only considered collisions between free objects; however, it should be pointed out that the collision rate could be considerably larger if the collapse of multiple star systems is considered. The stars in a binary system could evolve to a neutron star and a black hole, for instance, and then spiral together. One can speculate that there are many old binary systems in the Galaxy consisting of collapsed members and that these systems are only now spiralling together in considerable numbers. With no evidence to support this speculation, we will use the rates presented in Table 1.

We can make some estimate of the mean time between large bursts of gravitational radiation from stellar collapse. The most optimistic position is to assume that every star of mass greater than 1.5M@evolves into a neutron star or a black hole and emits a large amount of gravitational radiation in the final collapse. The rate at which stars reach the endpoint in their

evolution is estimated to be about once every five years in the Galaxy (3). Pulsars provide a lower limit to the rate of gravitational bursts. If neutron stars are formed rapidly in a stellar collapse, they will probably emit considerable amounts of gravitational radiation. Since pulsars are generally agreed to be rotating neutron stars, we can say that the neutron star formation rate is at least as large as the pulsar formation rate which is about once every 30 years (4). It is clear that some supernovae produce neutron stars, for example NP0532; however, some models of supernovae leave no star remnants behind. If we assume though, that all supernovae produce a burstof gravitational radiation, then another limit can be set on the mean time between bursts in the Galaxy. Various estimates of the supernova rate based on observations of other galaxies (5), calculations of stellar evolution (6), and radio measurements at 1GHz (7) all yield a supernova rate of one every 17 to 50 years. An estimate of the mean time between large bursts of gravitational radiation in the Galaxy is between 5 and 50 years.

MEAN TIME BETWEEN EVENTS	Perhaps once every 5-50 years in the Galaxy sec)
T OF ATIONAL TION TED	-dE/dt(ergs/ 1.2 x 10 48 1.2 x 10 51 2.9 x 10 51 2.6 x 10 51 3.9 x 10 48 7.0 x 10 50 7.0 x 10 50 1.1 x 10 48 1.1 x 10 53 1.6 x 10 53 1.9 x 10 53 1.9 x 10 51
A MOUNT OF CRAVITATIONAL RADIATION EMITTED	-AE(ergs) 7.8 x 1048 2.8 x 1050 3.6 x 1049 2.6 x 1048 8.9 x 1046 8.9 x 1052 1.7 x 1052 1.5 x 1052 1.5 x 1052
TABLE 2 Comment Comments	A neutron star could form in a highly excited and distorted state with the non-radial modes excited The power radiated and the energy stored in a mode are proportional to $\left(\frac{\delta R_2}{\delta R}\right)$ the awaraged square of the relative equation of state surface. H-W refers to the Harrison-Wheeler of state to the Harrison-Wheeler of state to the Eavinger-Simmons-Tsuruta-Cameron equation of state T is the damping time for the energy in the mode W/MC f(kHz) τ (sec) H-W .682 3.2 .1 8.3 .65 H-W .682 3.2 .1 11.1 12 Vy .677 1.5 .85 Vy 1.954 2.7 .11
Eguations	A neutron star constited and distortadial modes excited and distortadiate in a mode are proton amplitude of the equation of state VY refers to the equation cameron equation is the damping mode
ovace	<pre>leutron Star Jon-radial wlsations .efs. 8</pre>

EQUATIONS + COMMENTS

eutron Star

triaxial ellipsoid) n_the_form of a acobi ellipsoid apidly rotating

efs. 9,10,11

deformed, rapidly rotating state, possibly in the form of a Jacobi ellipsoid, Chau and Srulovicz A neutron star could form in a highly neutron star to assume the figure conclude that it is possible for of a rotating Jacobi ellipsoid.

$$\frac{dE}{dt} = \frac{32G}{125c^5} M^2 (a_1^2 - a_2^2)^2 \omega^6$$

a₁, a₂, a₃ are the triaxial radii, here rotation is about a₃ axis, $a_1a_2a_3 = const.$

 $-dE/dt=4 \times 10^{51} \text{ ergs}/$

then $-\Delta E = 9 \times 10^{50}$

lα

assuming

spectrum peaks around

£ = 320 Hz

$$1-a_2/a_1$$
 $e^{-\tau/b}$ τ in units of $\frac{25}{18} \left(\frac{\overline{a}}{RS}\right)^3 \left(\frac{\overline{a}}{\overline{c}}\right)^3 \left(\frac{\overline{a}}{\overline{c}}\right)$

$$\omega_{m}^{*-}\omega_{ve}^{-2\tau/b}$$
 b = 16.039
$$\overline{a} = (a_{1}a_{2}a_{3})^{1/3}$$

$$R_{\rm S} = 2GM/c^2$$

 $\omega_{\rm m}^* = .6117 (\pi {\rm Gp})^{1/2}$

(a₁=a₂) to which the Jacobi ellipsoid the non-radiating McLaurin Ellipsoid is the limiting rotation rate for evolves increases but only by a small amount,

note: $\omega < \omega_m$, the rotation rate

7% for the case considered here

ME/ 1 TIME BETWEEN HMOUNT OF GRAVITATIONAL RADIATION EMITTED

EVENTS

every 5-50 years in the Galaxy

Assume a Jacobi ellipsoid with maximum distortion,

 $|\omega| = .5329 (\pi G \rho)^{1/2}$ $|a_2/a_1| = .4322$

if all the pulsars are formed ellipsoids then at least once as Jacobi

every 30y. = 20 km, M = 1M©

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2

EQUATIONS & COMMENTS

Neutron Star

Pulsar

refs.12,13,14,

Gravitational radiation emitted:

$$\frac{dE}{dt} = \frac{32}{125} G/c^5 M^2 \omega^6 (a_2^2 - a_1^2)^2$$

$$a_1, a_2 \text{ radii perpendicular to}$$

$$\text{rotation axis,} \omega = \text{pulsar rota-tion rate,} \text{ assuming } a_2 - a_1 = \varepsilon R$$

$$R = \text{average radius}$$

spectrum is monochromatic at 200

 $\frac{dE}{dE} = \frac{128}{125} \frac{G}{G^5} M^2 _6 R^4 _6 ^2$

quadrupole radiation and that Assuming pulsar looses energy only by emission of electroε ≈ const. for recent times magnetic and gravitational

$$\frac{\mathrm{d}E}{\mathrm{d}\tau_{\mathrm{GQ}}} = -\left[\left(\frac{\mathrm{d}p}{\mathrm{d}\tau} \right)^{-1} \frac{\mathrm{d}^2p}{\mathrm{d}\tau^2} + \frac{\mathrm{d}p}{\mathrm{d}\tau} \right] \frac{\mathrm{I}\omega^2}{2}$$

P is pulsar period, I is moment of inertia

AMOUNT OF GRAVITATIONAL MEAN IME RADIATION EMITTED EVENTS

about once every 30 years. After initial damping about $10^6 \, \mathrm{years}$ Pulsars formed formation and radiation for oroduction of gravitational continuous

For NP0532, the Crab pulsar, pulsar agree with the known Ostriker and Gunn assume ε is fixed by requiring that the calculated age of the constant for the entire history of the pulsar. $I = 1.4 \times 10^{45} \text{gm-cm}$ distance = 1700 pc For NP0532: $M = 1.4 M\odot$ = .033sage.

$$dP/dt = 420 \times 10^{-15}$$

 $d^2P/dt = -100 \times 10^{-25}sec^{-1}$
then $\epsilon = 3 \times 10^{-4}$

so
$$-dE/dt = 1.5 \times 10^{38}$$
 ergs/sec from the second derivative

(-dE/dt)_{GQ} measurement

$$\frac{(-dE/dt)_{GQ}}{(-dE/dt)_{total}} = .44$$

second derivative of the period about 1/4 for this ratio. The whereas Ostriker and Gunn get is rather uncertain.

SOURCE

EGUATIONS + COMMENTS

The crust of a neutron star shifts releasing energy which can be . radiated away as gravitational radiation. Assume that all of the released energy goes into one of the non-radial oscillation modes of the neutron

Pulsar starquake

refs. 16

Neutron Star

$$-\underline{z} = 4 \left(\frac{\mathrm{I} \omega^2}{2} \right) \frac{\delta \omega}{\omega}$$

= rotation frequency of the

the lowest mode with a frequency frequency due to starquake. Taking the V_{\star} model with $M/M \mathcal{C} = 1.95$ from K. Thornes study and δω = change in the pulsar

$$\left(\frac{E}{\left(\frac{\delta R}{R}\right)^2}\right)^2 = 1.7 \times 10^5 4 \quad \text{so}$$

$$-\frac{dE}{dt} = 37.6 \left(\frac{I\omega^2}{2}\right) \frac{\delta \omega}{\omega}$$

AMOUNT OF GRAVITATIONAL MEAN TIME BETWEEN RADIATION EMITTED

every few years to be expected from the Crab

EVENTS

the Sept. 1969 speedup of NP0532 Assuming a pulsar radius of 10 km and $M=1.4M\odot$ a pgriod of .033s, $\delta\omega/\omega=2.5 \times 10$ from

$$-dE/dt = 1.5 \times 10^{38} ergs/sec$$

$$-\Delta E = 1.6 \times 10^{37} \text{ ergs}$$

$$\tau = .11 sec$$

able to the expected gravitational radiation at 60 Hz. The power output is compar-

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EQUATIONS + COMMENTS

AMOUNT OF CRAVITATIONAL RADIATION EMITTED

MENY TIME BETWEEN EVENTS

greater than every 10 years at the Galactic

center

Particle falling radially into a Schwarzshild black hole

refs. 17,18,19

A particle of mass m falls into a non-rotating black hole of mass M (m<<M).

$$-1E = .0104 \text{ mc}^2 \left(\frac{m}{M} \right)$$

Spectrum peaks at a frequency

$$z = .32 c^3/GM$$

The event lasts a time

$$\approx 2 \times \frac{2\pi}{3}$$

Assume a .5MC neutron star falls into a 5 MC black hole. A realistic calculation should take into account tidal disruption of the neutron star

 $-\Delta E = 9.4 \times 10^{51} \text{ ergs}$ $-dE/dt = 9.4 \times 10^{54} \text{ ergs/sec}$

spectrum peaks around 2 kHz

$$\tau \approx 10^{-3} \text{ se}$$

EGUATIONS + COMMENTS

Black holes collision

Two plack holes collide and coalesce

refs. 20,21,22

black hole, expect the spectrum From the paper by Gibbons and radiation which is one or two cycles of a sinusoidal wave train. From the spectrum of Hawking, expect a pulse of a particle falling into a to peak around

$$\omega = c^3/GM$$

radius of the black hole. Expect which is essentially the orbital frequency of a photon in orbit near the Schwarzshild the event to last a time

The total possible energy radiated is 29.3% of the rest mass for non-rotating black holes and 50% of the rest mass for extreme Kerr black holes.

AMOUNT OF CARVITATIONAL MEN TIME RADIATION EMITTED

DETWEEN

EVENTS

greater than assuming 10% of the stars in the core onge every 10 years, are black

Assume two 2 Me non-rotating black

 $-dE/dt = 1.7 \times 10^{58} ergs/sec$

 $-\Delta E = 2.1 \times 10^{54} \text{ ergs}$

spectrum peaks around
8 kHz

 1.2×10^{-4}

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	EQUATIONS + COMMENTS
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	8

Particle spiralling into a black hole

refs. 23,24

Total energy radiated before the the last stable orbit. Spectrum is essentially monochromatic at at multiples of the fundamental hole is the binding energy of particle falls into the black twice the orbital frequency. Elliptical orbits will emit frequency but will quickly Typical power radiated is become circular.

$$-\frac{\text{dE}}{\text{dt}} \approx \frac{32G}{5|\text{c}^5} \left(\frac{\text{mM}}{\text{m}+\text{M}}\right)^2 R^4 \omega^6$$

and typical time is

$$= -\Delta E / - \frac{dE}{dt}$$

A) Non-rotating black hole of mass M, particle of mass m

$$-\Delta E = .0572mc^2 \omega_{max} (GM/R_3)^{1/2}$$

$$\lambda = 6 (2GM/c^2)$$

particle orbiting in the same B) Exteme Kerr black hole, direction as black hole rotation

$$-\Delta E = 4226 mc^2 \omega_{\text{max}} = \frac{1}{2} (GM/R^3)^{1/2}$$

$$R = 2GM/c^2$$

C) Extreme Kerr black hole, retrograde

$$-\Delta E = .0377 \text{mc}^2 \omega_{\text{max}} = 1.038 (GM/R^3) \frac{1/2}{1}$$

greater than 10 years in years in the Galactic center

Realistic example difficult to taken into account. For this radius) neutron star spirals calculate since tidal forces on the small mass should be example assume a 1 MS (10km into a 5M& (14.8 km radius) black hole

Roche Limit =
$$2.45 \left(\frac{\rho BH}{\rho NS} \right)^{1/3} \times ^{R}_{BH}$$

$$= 42 \text{ km}$$

source at Galactic center For

B)
$$-\Delta E = 7.6 \times 10^{53} \text{ ergs}$$

 $-dE/dt = 3.2 \times 10^{55} \text{ ergs/sec}$
spectrum peaks at 2.3kHz
C) $-\Delta E = 6.8 \times 10^{52} \text{ ergs}$
 $-dE/dt = 4.3 \times 10^{52} \text{ ergs/sec}$

spectrum peaks at 176 Hz,
$$\tau = 1.6s$$

$$= .0377 \text{mc}^2 \text{ max} = 1.038 (GM/F)$$

$$= 9 \times (2GM/c^2)$$

		AMOUNT OF CHANTATION A	PAVITATION	76	A TIME
SWACE	EGUATIONS + COMMENTS	RADIATION !	EMITTED		
Masses in Keplerian orbits	The maximum power radiated by Keplerian orbits (at closest	some examples of c	close binary s	systems (e=0	
	ch)	star period(days)) Ml M2 in M©	-dE/dt deerqs/sec	listance pc
refs. 25,26,27	$\frac{dE}{dt} = \frac{32}{5} \frac{G^2}{c^5} \cdot \frac{1.2}{5} \cdot \frac{1.12}{5} \times \frac{1.12}{5}$	i Boo .268	1	3.6x10 ³⁰	12
	$\frac{(1+e)^6}{(1-2)^5}$	UV Leo .6	1.4 1.3	7.2×10^{29} 6.6×10 ³¹	68 390
	where a = semimajor axis (minimum separation is		0.00	•	42
	naximum is	WU Ma .33	1.3 .65	.4x10	L9
	e = eccentricity of orbit	WZ Sge 81 min	.56 .19	1.5×10 ³¹	26
	power averaged over one orbit			······································	
	ŋ			•	
	$\left[1 + \frac{73}{24} e^2 + \frac{37}{96} e^4\right]$				
	for e<.2, the energy is				
	(a)(x, x, y) 1/2				
	$\omega = \frac{G(M_1 + M_2)}{3}$				
	in terms of the initial	·			
	ditions, the	v		· · · · · · · · · · · · · · · · · · ·	
	actoliat tactac				
	Topic Section (Section Section				

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APPENDIX 2

The optical delay line to be discussed consists of two concave spherical mirrors having the same radius of curvature (1). One of the mirrors has a small hole in it through which the beam enters and exists (Fig. 1). Other possible configurations use a small mirror or light pipe to deflect the beam into and out of the cavity. Slightly astigmatic mirrors have also been used to utilize more of the mirror surface and increase the total delay (2). The purpose of this appendix is to present some of the properties of spherical-mirror optical delay lines including the stability of the cavity and the change in delay time for small rotations and translations of one of the mirrors.

In Fig. 2, two spherical mirrors have been placed in a delay line configuration with mirror B slightly rotated. There is a unique line called the optical axis of the delay line which passes through the mirrors at points labelled P_A and P_B . The optical axis is defined by the condition that the line which runs through P_A and P_B be parallel to the mirror normal at P_A and P_B . The optical properties of the cavity are invariant for rotations about the optical axis. In the paraxial ray limit ($\sin \theta \approx \theta$, $\cos \theta \approx 1$) it is possible to derive an expression for the points on the mirrors where the beams are reflected. In the coordinate system defined by the optical axis

where
$$\tan \alpha = \sqrt{\frac{2R}{L} - 1} / \left(1 + \frac{RX'_{O}}{X_{O}}\right)$$

 $\cos \phi = 1 - L/R$

$$A^2 = \frac{2R}{2R-L} \left[x_0^2 + Lx_0^2 x_0' + \frac{RL}{2} x_0'^2 \right]$$

L is the cavity length, R is the radius of curvature of the mirrors, X_O is the entry point of the initial ray, and X_O' is the x-component of the angle that the ray makes to the optical axis. A similar expression holds for Y_D . Even n gives the position on mirror A and odd n gives the position on mirror B. If L and R are chosen such that

 $2r\phi = 2m\pi$ where m is an integer and

 $1 \le m \le r - 1$ and sm/r is not an integer for $1 \le s \le r-1$, then there will be r reflections on each mirror (counting the hole as a reflection) and the beam will exit through the hole in mirror A as if reflected from the back of that mirror. This is called the reentrant condition.

If mirror B is moved and the cavity length changes, the output beam will shift with respect to the hole in mirror A. We will assume that the motion of mirror B is small enough so that the beam still exits through the hole in mirror A. A rough estimate of the allowed motion of mirror B will be made in the next paragraph. Since the number of beams in the cavity is assumed constant, the change in delay time can be calculated. To a good approximation, the total beam length is just the number of beams in the cavity times the distance between points P_A and P_B in Fig. 2, and can be calculated in terms of L, R, the translation (X,Y,Z), and the rotation (θ_X , θ_Y) about θ_B . Denoting the delay time by t, the number of beams by N and the speed of light by c the following formulas result

$$\frac{\partial t}{\partial x} = -\frac{N}{C} \frac{x}{2R-L}, \quad \frac{\partial t}{\partial y} = -\frac{N}{C} \frac{y}{2R-L}, \quad \frac{\partial t}{\partial z} = \frac{N}{C}$$

$$\frac{\partial t}{\partial \theta_{x}} = \frac{N}{C} \frac{R(R-L)}{(2R-L)} \theta_{x}, \quad \frac{\partial t}{\partial \theta_{y}} = \frac{N}{C} \frac{R(R-L)}{(2R-L)} \theta_{y}$$

These formulas are in excellent agreement with computer calculations using the geometrical optics approximation to the delay line.

In order to estimate the allowed motion of mirror B we will assume that the reentrant condition has been satisfied and that the initial ray has been chosen so that there is a circular pattern of reflection points on each mirror. In this case φ is the angle between consecutive reflections (Fig. 3). The configuration is stable for small motions of mirror B if the beam continues to exit through the hole in mirror A and the number of reflections remains constant. Using the relation

 $\cos \phi = 1-L/R$, the change in ϕ per reflection is

$$\delta \phi = \delta L/(R \sin \phi)$$

Stability requires that

$$N \mid \delta \phi \mid d_1 < d_2$$

where N is the number of beams, d_1 is the radius of the pattern and d_2 the radius of the hole. Substituting

$$|\delta L| < \frac{d_2}{d_1} \frac{R|\sin \phi|}{N}$$

For the cavity we plan to use R = 900cm cos ϕ = 0, N = 302, d_2 = .075cm d_1 = 3.81cm so

If this $|\delta L|$ were caused by a translation transverse to the optical axis, then the translation would be of the order of 1/2cm. For a rotation the angle would be about $1/2^{\circ}$. We have built and tested a delay line and find that the reentrant condition remains satisfied for all movements of mirror B which keep the beam within the cavity. The output beam is not observed to move.

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Figures

Figure 1

Spherical mirrors in delay line configuration.

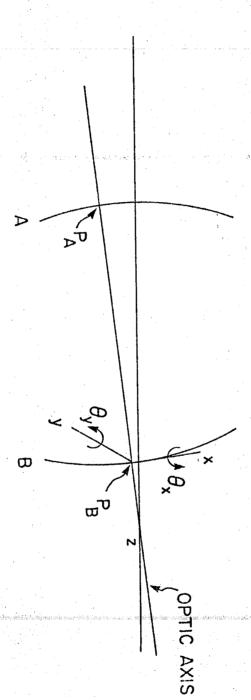
Figure 2

Spherical mirrors in delay line configuration with mirror B slightly rotated.

Figure 3

 $\boldsymbol{\varphi}$ is the angle between consecutive reflections.

Figure 1



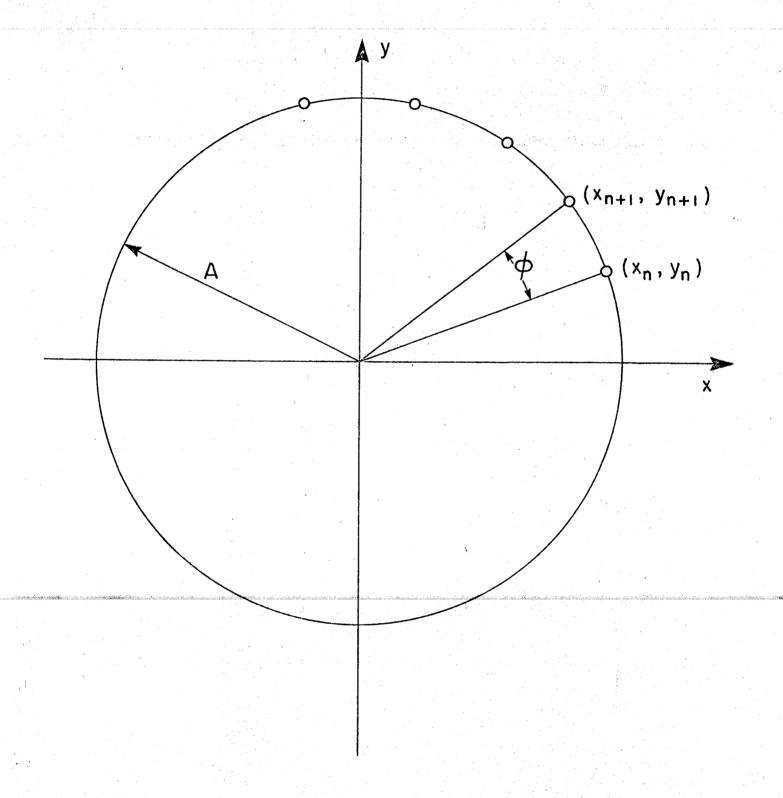


Figure 3